

Representing convection in models - How stochastic does it need to be?

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Convection in large-scale models

$$\frac{\partial(\bar{\rho}\bar{s})}{\partial t} = -\frac{\partial(\bar{\rho}\bar{u}\bar{s})}{\partial x} - \frac{\partial(\bar{\rho}\bar{v}\bar{s})}{\partial y} - \frac{\partial(\bar{\rho}\bar{w}\bar{s})}{\partial z} - \frac{\partial(\bar{\rho}\bar{u}'s')}{\partial x} - \frac{\partial(\bar{\rho}\bar{v}'s')}{\partial y} - \frac{\partial(\bar{\rho}\bar{w}'s')}{\partial z} + \bar{\rho}Q$$

resolved terms
sub-grid horizontal fluxes
sub-grid vertical flux
sources

To parametrize:

$$-\frac{\partial(\bar{\rho}\bar{w}'s')}{\partial z} \quad \text{sub-grid vertical flux} \quad +\bar{\rho}Q = +\bar{\rho}(Q_{rad} + C + E)$$

sources
radiation
condensation
evaporation

Surrogate for convective heating:

$$Q_1 = Q_{rad} + L(c - e) - \frac{1}{\bar{\rho}} \frac{\partial(\bar{\rho}\bar{w}'s')}{\partial z} \quad \text{Apparent heat source}$$

Convection in large-scale models

Decide on **existence and type** (e.g., deep vs. shallow) of
convection

—————→ **Trigger model**

Predict **vertical distribution** of heating, moistening and
momentum changes

—————→ **Cloud model**

Predict the **overall amount** of the energy release

—————→ **Closure**

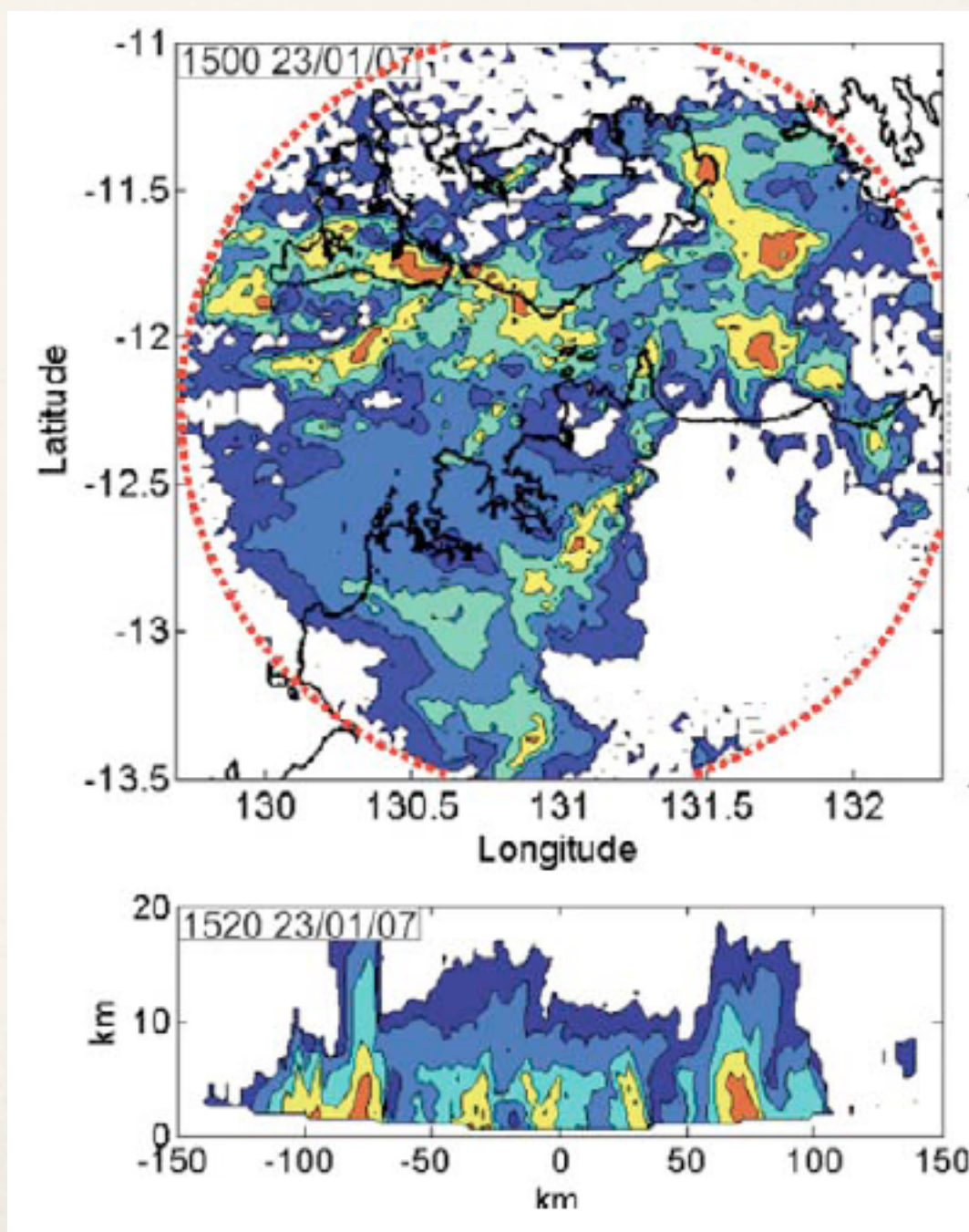
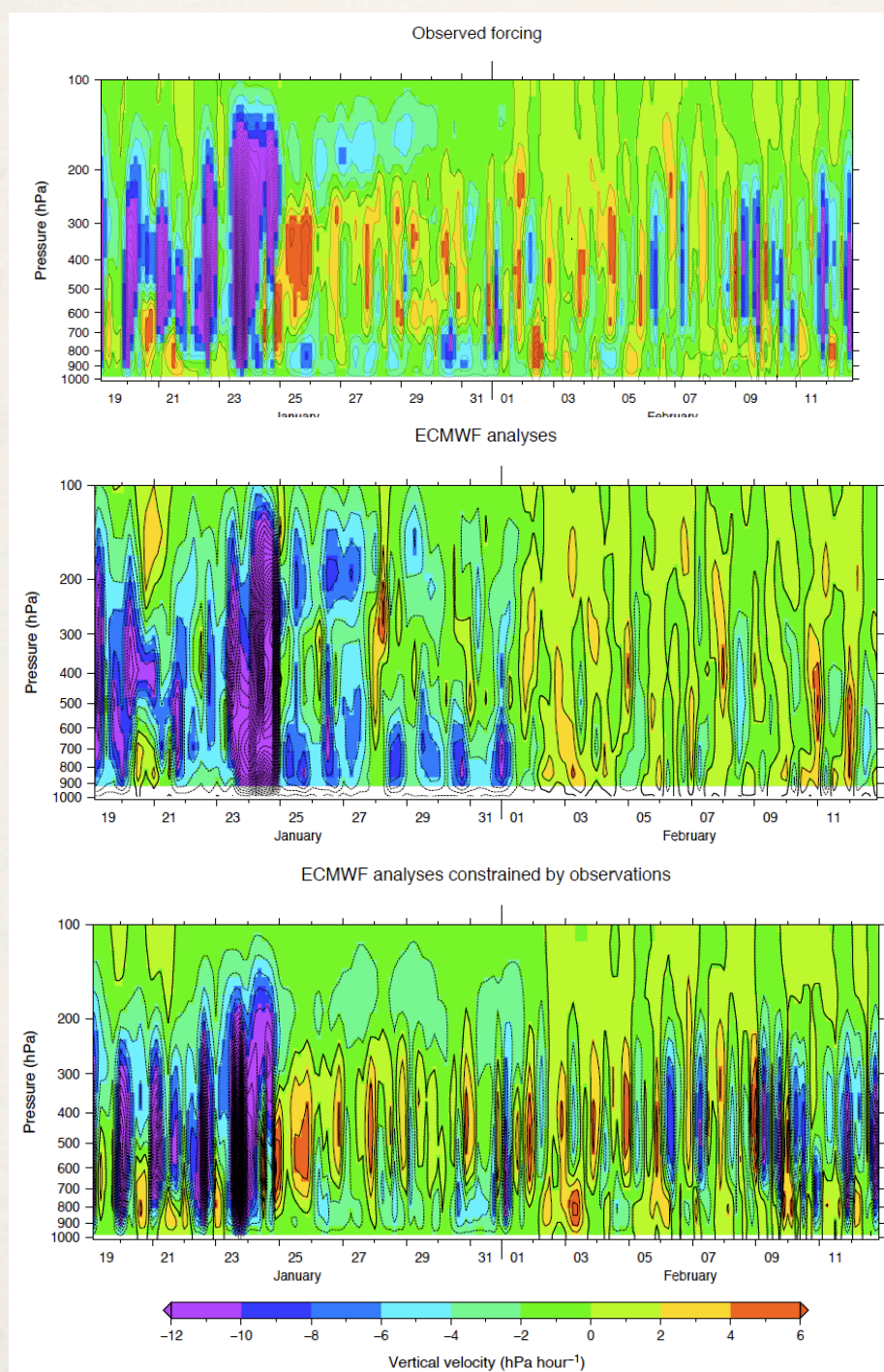
Real data to explore the problem

- ❖ Most if not all the research into the stochasticity of convection has relied on the use of models
- ❖ While justifiable to some extent, ultimately it is the real world we wish to represent
- ❖ It is timely to explore observations and make them useful to the discussion
- ❖ To do so requires frequent concurrent observations of the large and small scales in a convecting atmosphere

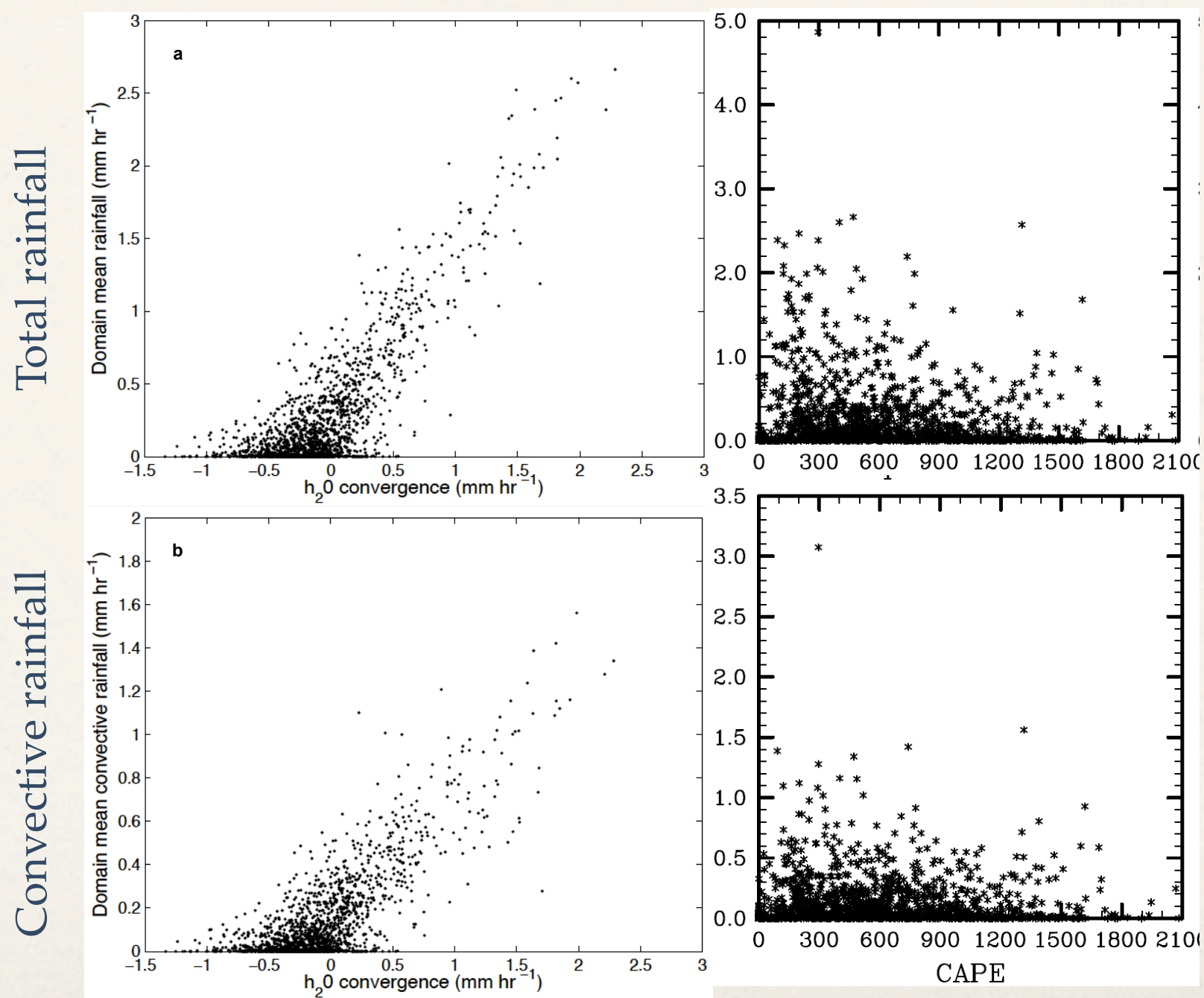
The data set - Construction

Large Scales

Small Scales



Some basic relationships

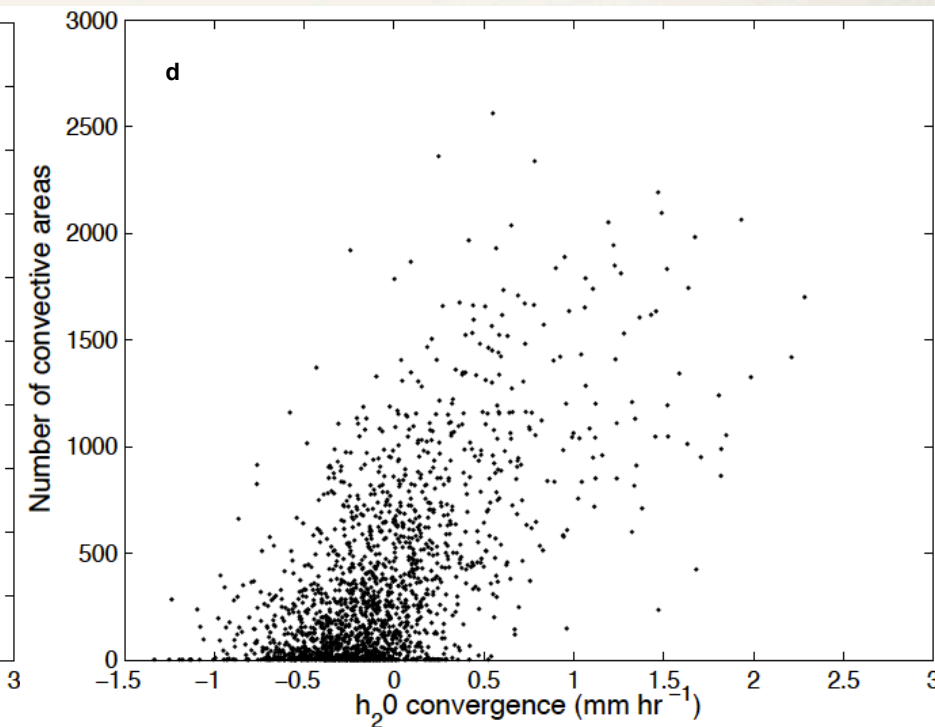
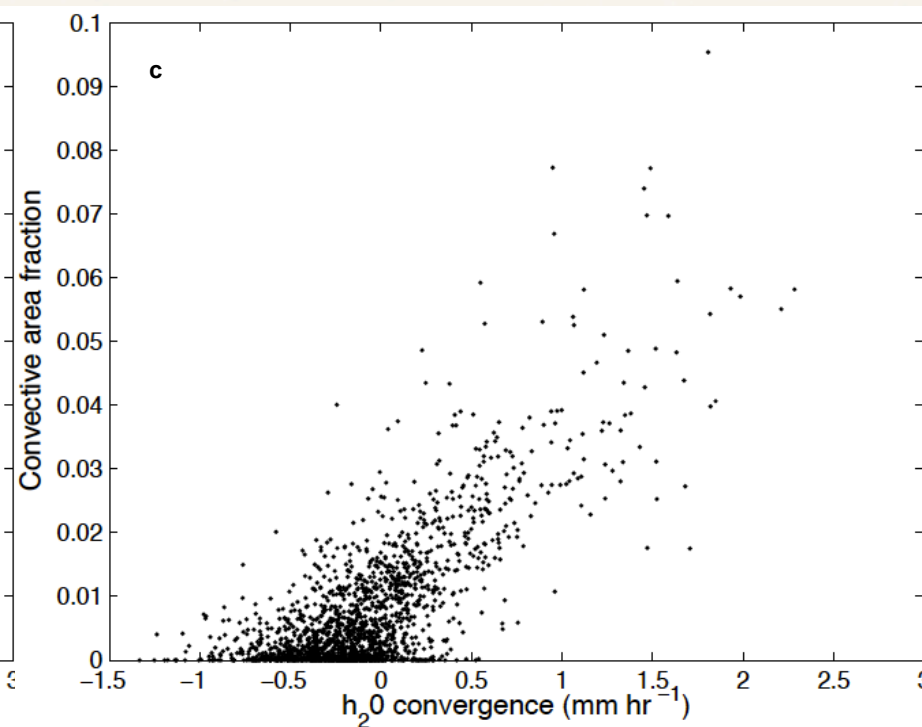
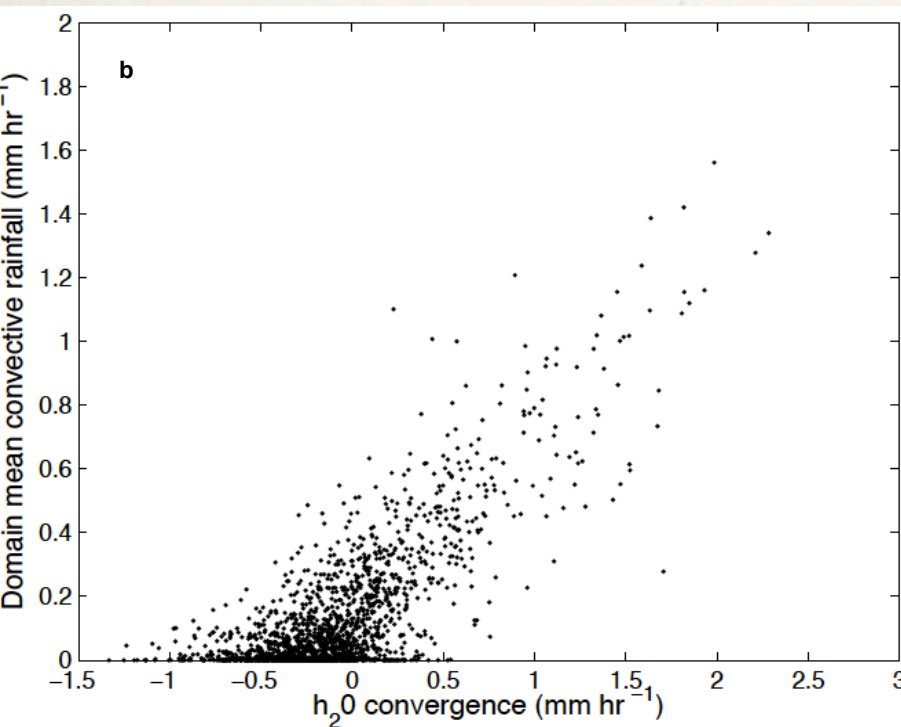


Large-scale q-convergence

CAPE

Some basic relationships

Relationship to large-scale q -convergence

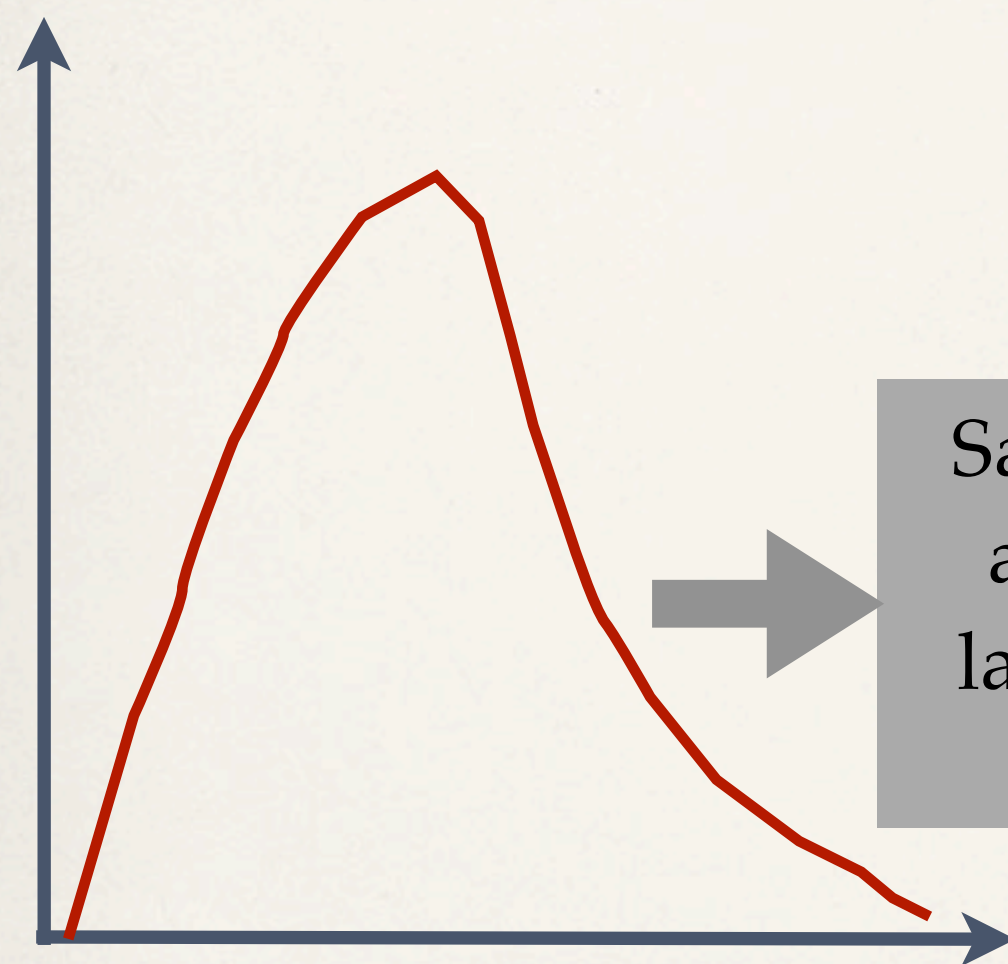


Domain-mean convective rainfall

Convective area fraction

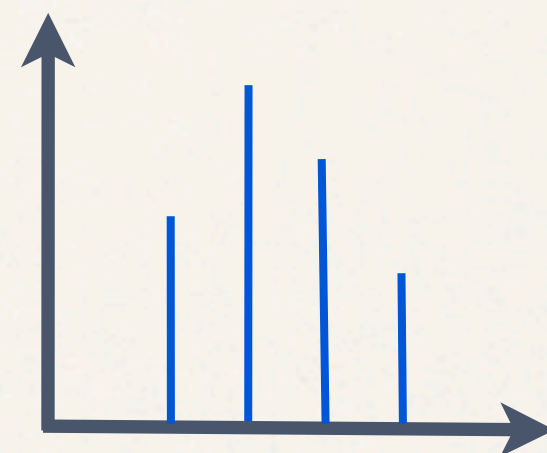
Number of convective cells

What do we mean by “stochastic”?

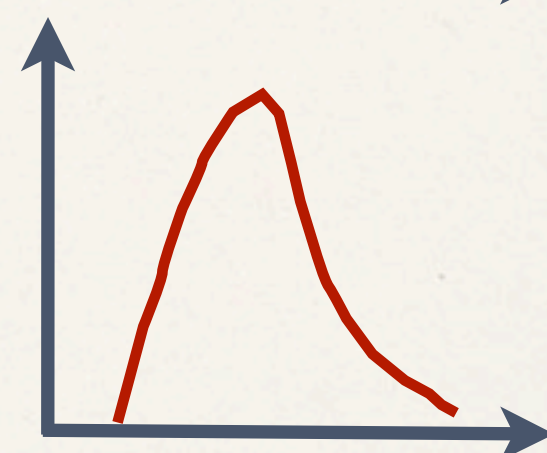


Heating / Precipitation PDF

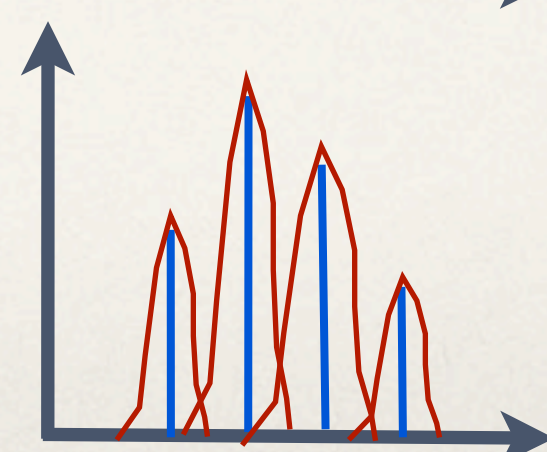
Sample for arbitrary large-scale states



Deterministic



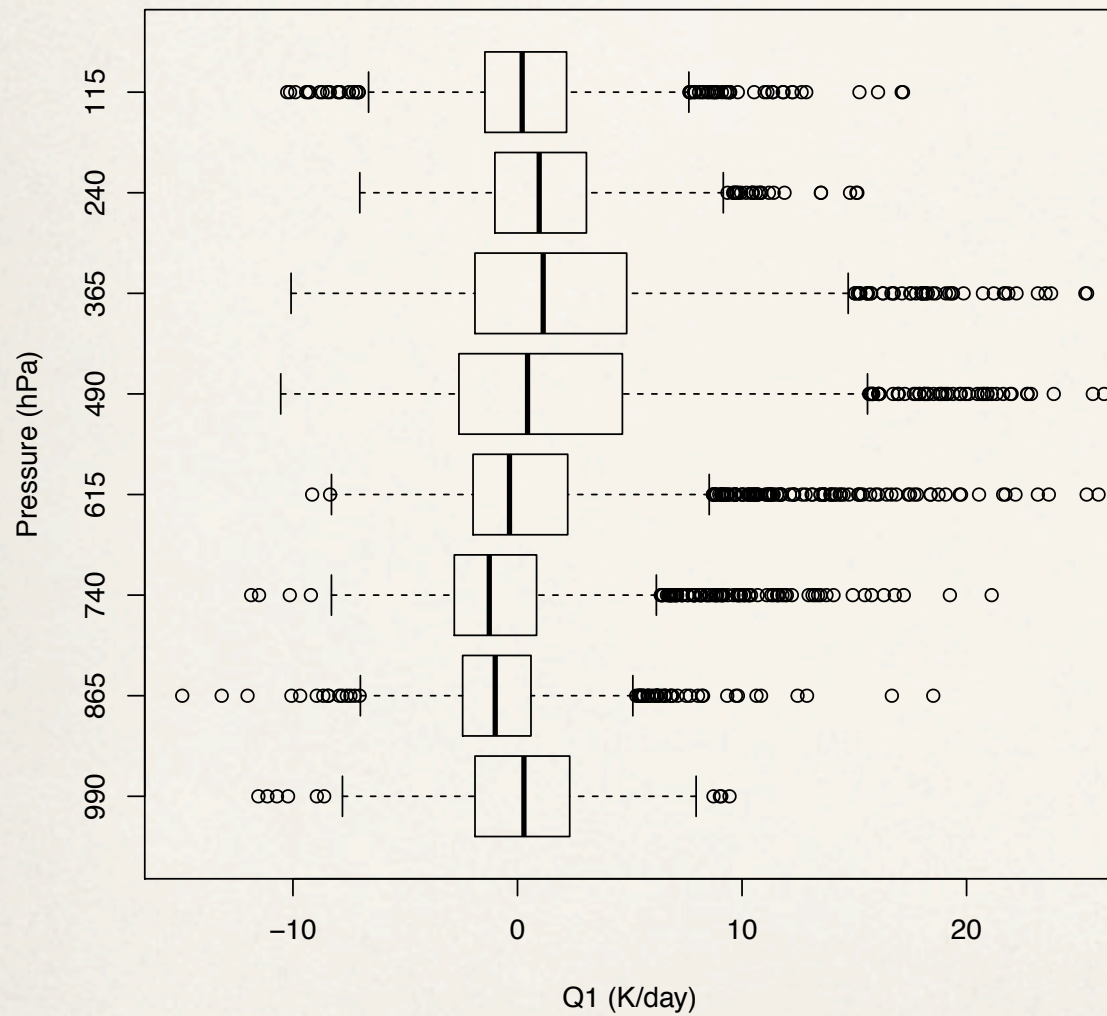
Stochastic



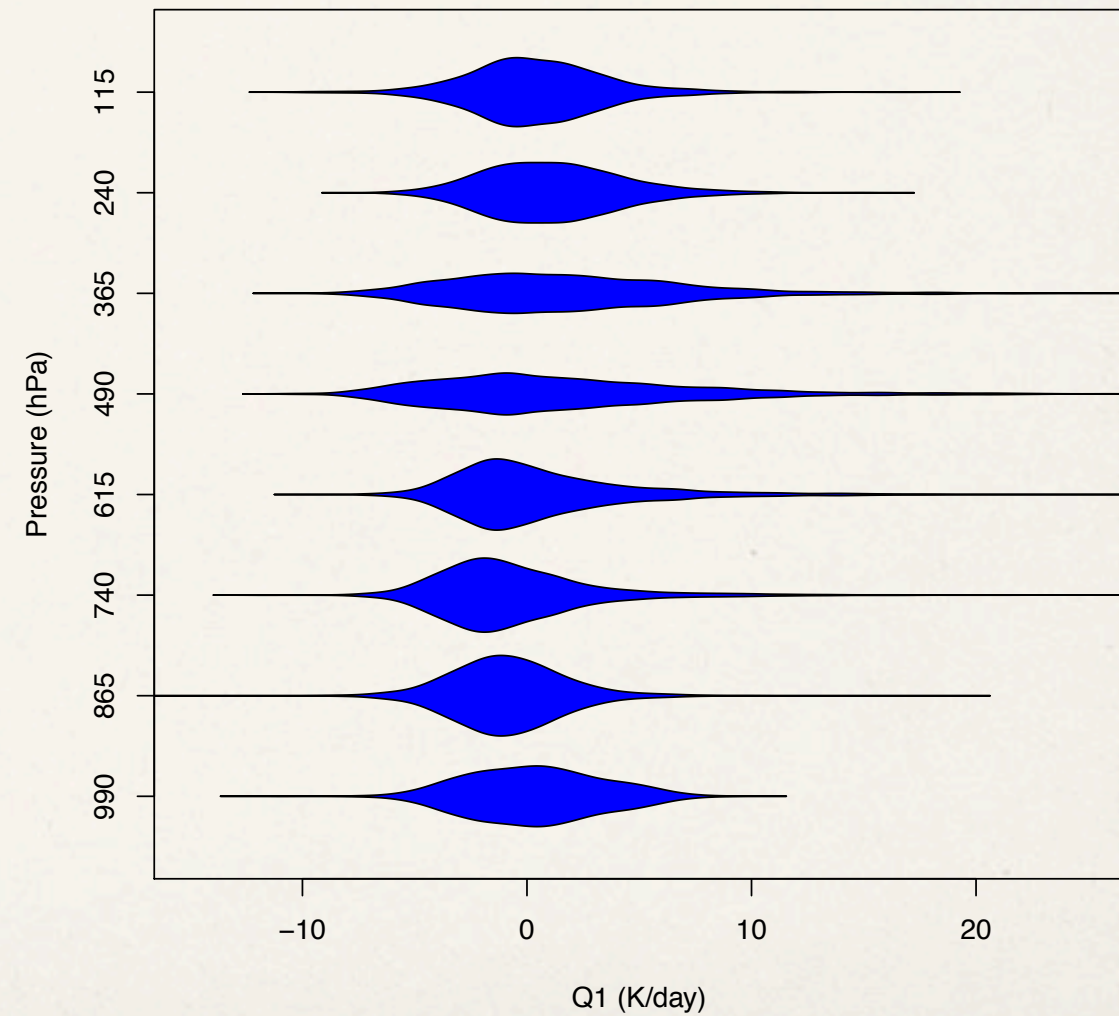
A bit of both

A “new” kind of plot

Distribution of Q1 for the entire data set

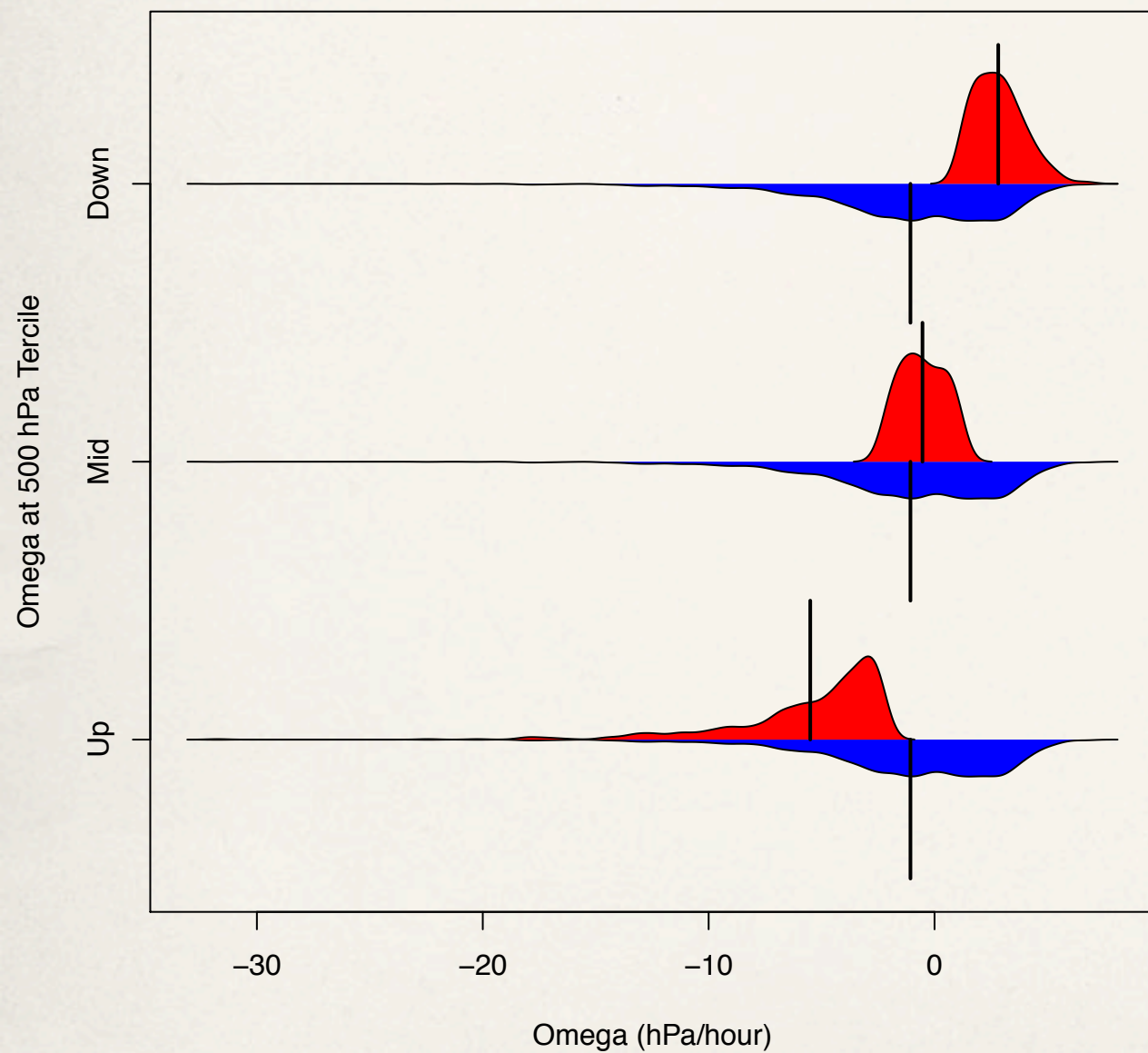


Box Plot

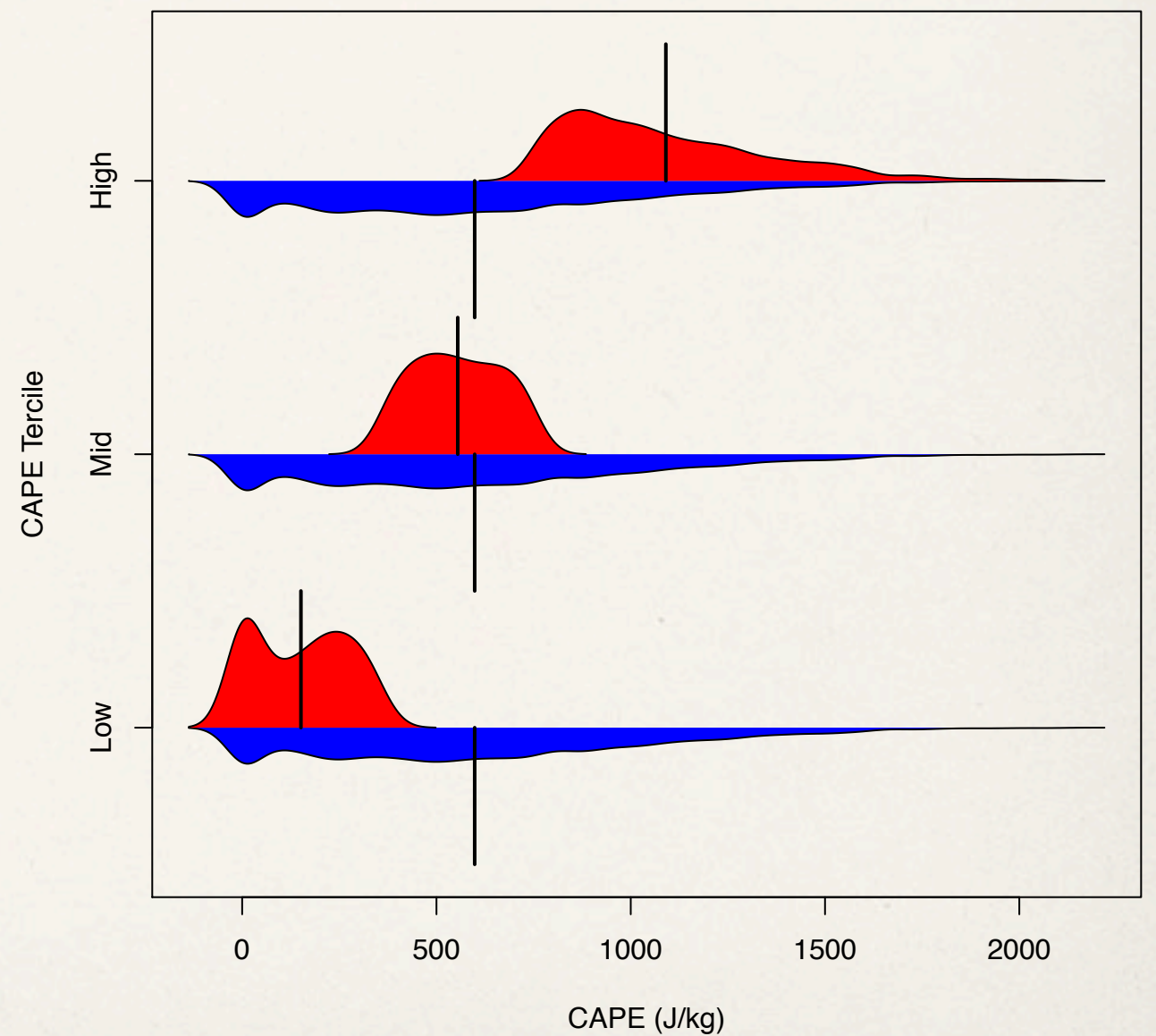


Bean Plot

A “new” kind of plot

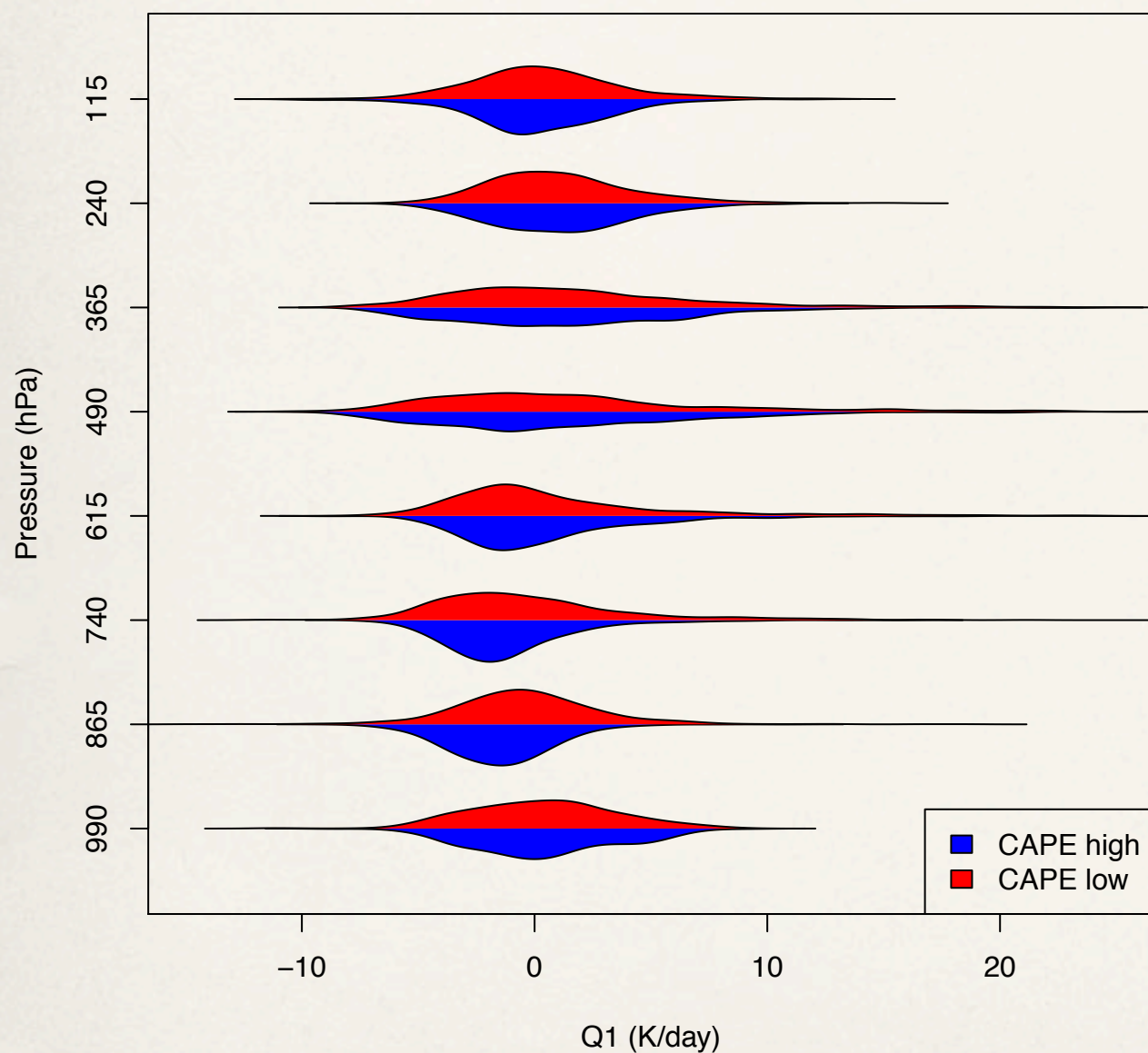


Omega at 500 hPa Terciles

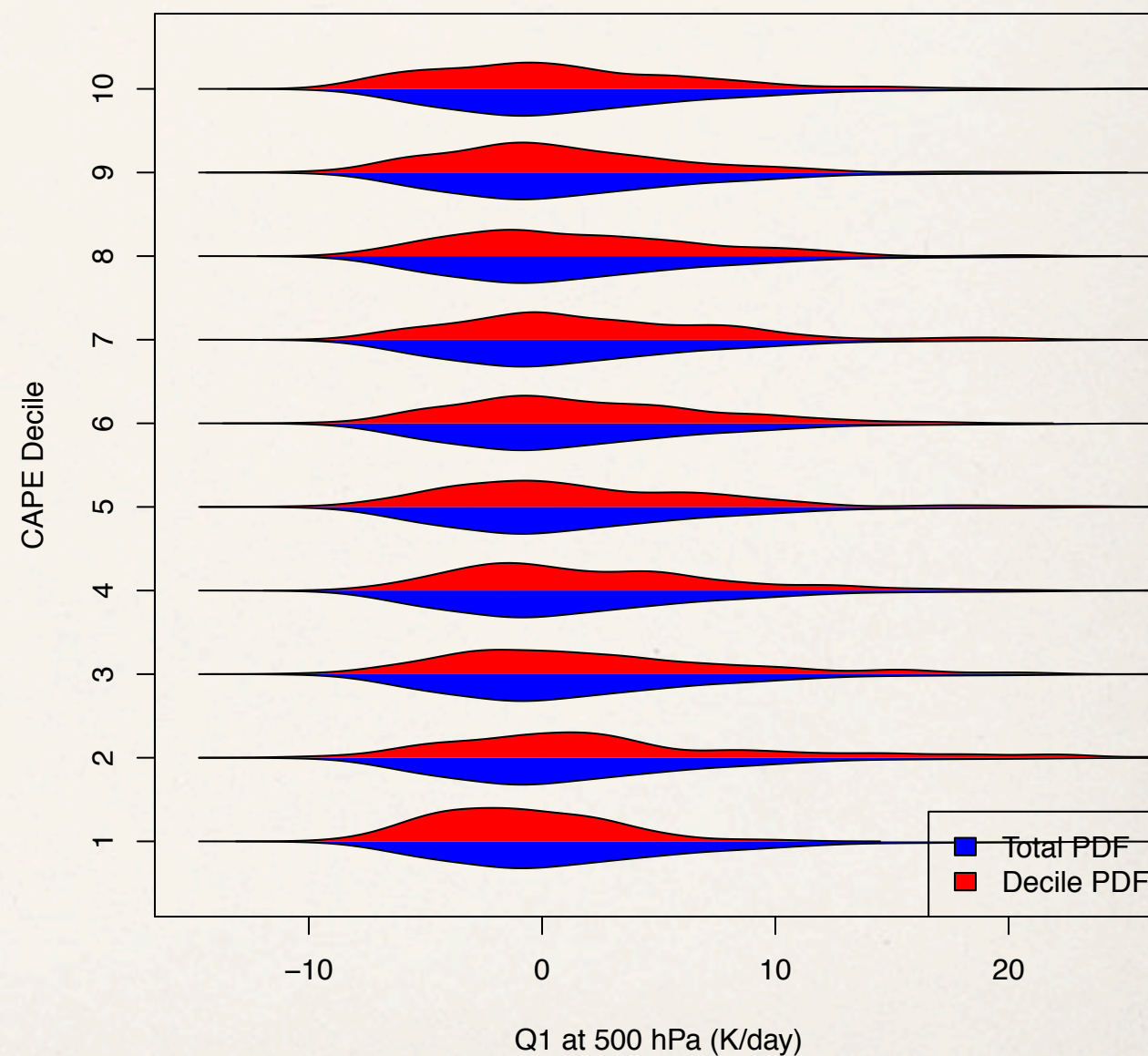


CAPE Terciles

How stochastic is it? - Lets wear CAPEs

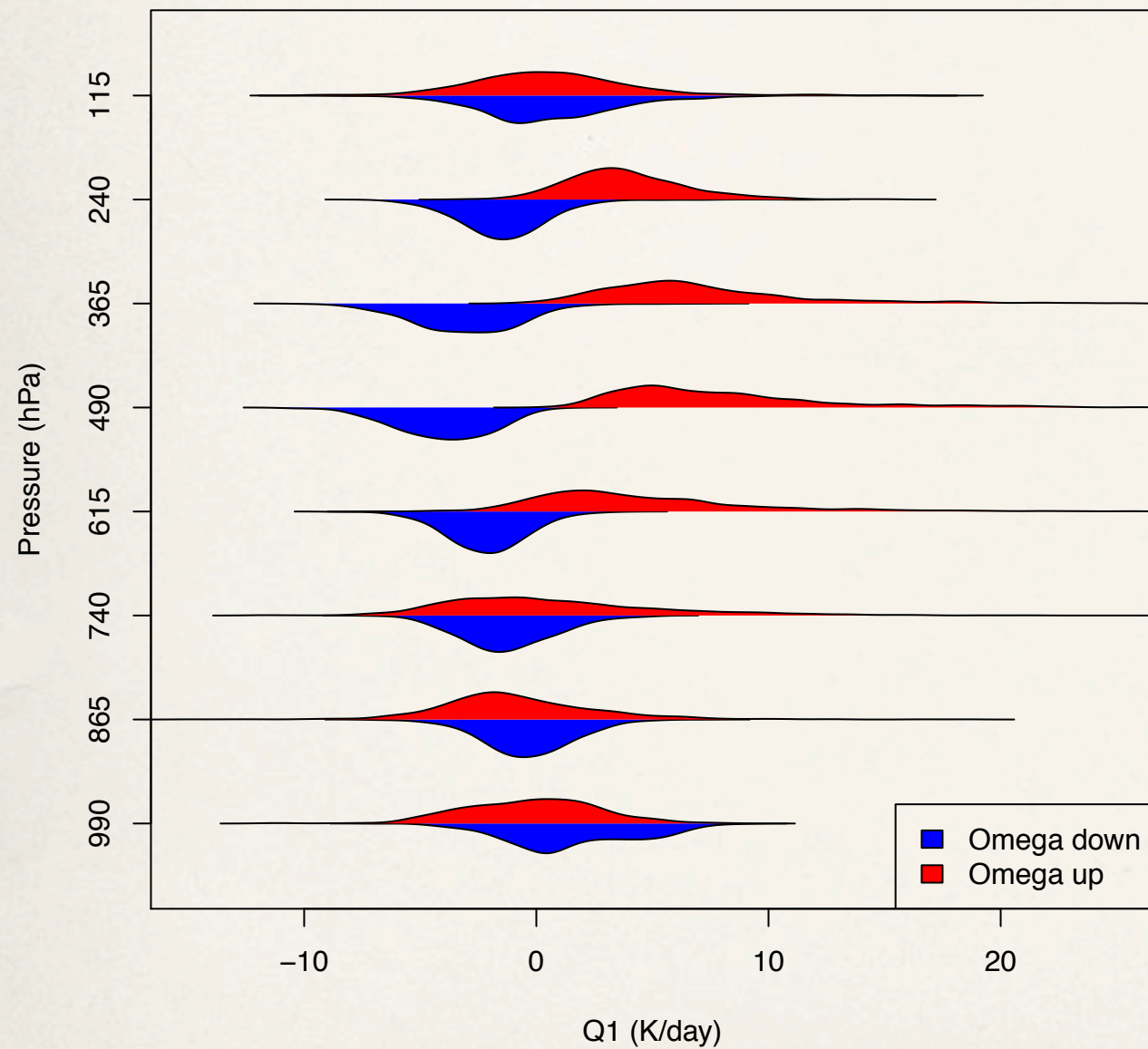


Q1 vs pressure for high/low CAPE

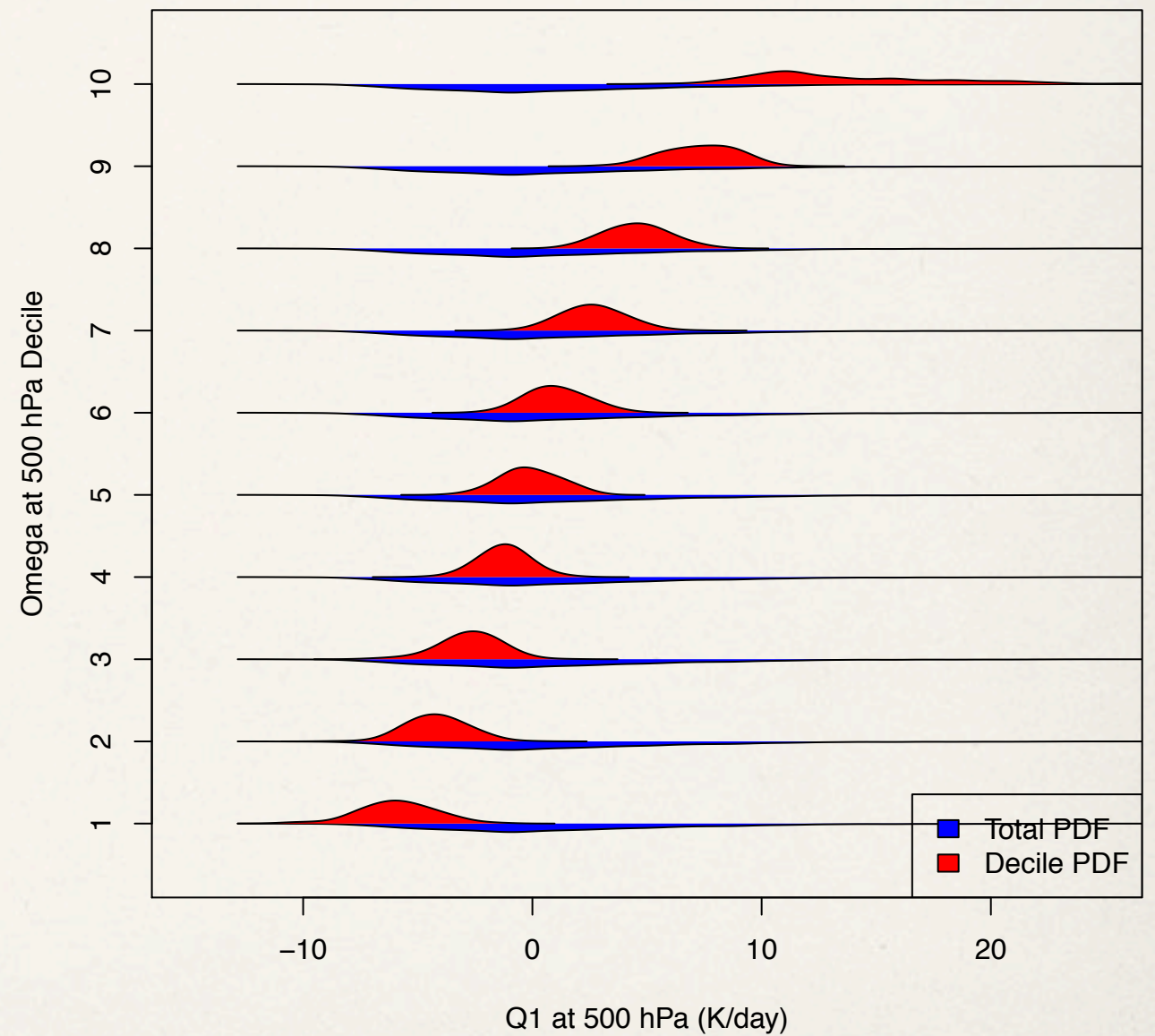


Q1 at 500 hPa by CAPE deciles

How stochastic is it? - A converging view

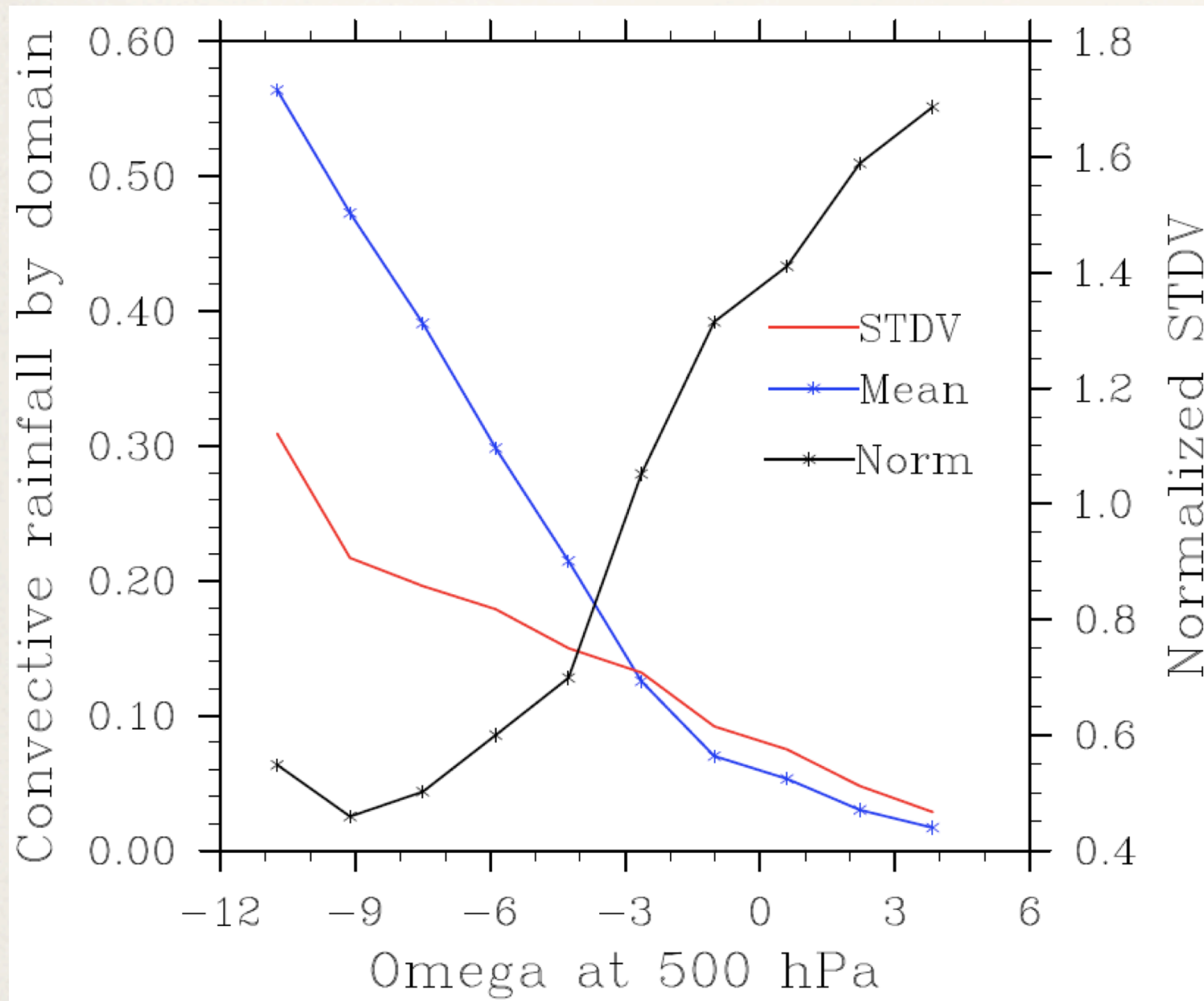


Q1 vs pressure for ω up and down



Q1 at 500 hPa by ω at 500 deciles

How stochastic is it? - A converging view



- * Both mean and standard deviation increase with large-scale “forcing”.
- * However, the signal to noise ratio decreases.
- * Hence, overall convective behaviour becomes more “predictable” as the “forcing” increases.
- * This is contrary to some implementations of “stochastic” convection.

Next Steps

- ❖ Extend to more sites
- ❖ Study domain size dependence
- ❖ Forced modelling
- ❖ Large domain modelling

Conclusions

- ❖ Data sets of with frequent concurrent observations of large and small scales in a convecting atmosphere can be constructed at least at some sites using a combination of NWP analyses and radar data.
- ❖ Early results indicate poor relationships between stability-based measures and the small scales but much stronger links between convergence based variables and convective heating. C&E!?
- ❖ As a consequence, the degree of stochastic behaviour is a strong function of the “model” chosen to link the scales - all the more reason to build uncertainty estimates straight into the parametrizations..
- ❖ Naturally, poor models can look very stochastic, better models less so.

Conclusions

- ❖ How do we know when we have a bad model and when the problem is truly stochastic?
- ❖ Efforts on all sides of parametrization are required and the well-balanced application of data, theory and models is required in finding the answers!
- ❖ This workshop should contribute to a programme to do this better!