



Met Office

Some thoughts on convective “triggering”,  
“closure” and “cloud model”...

...and a new stochastic scale-aware scheme.

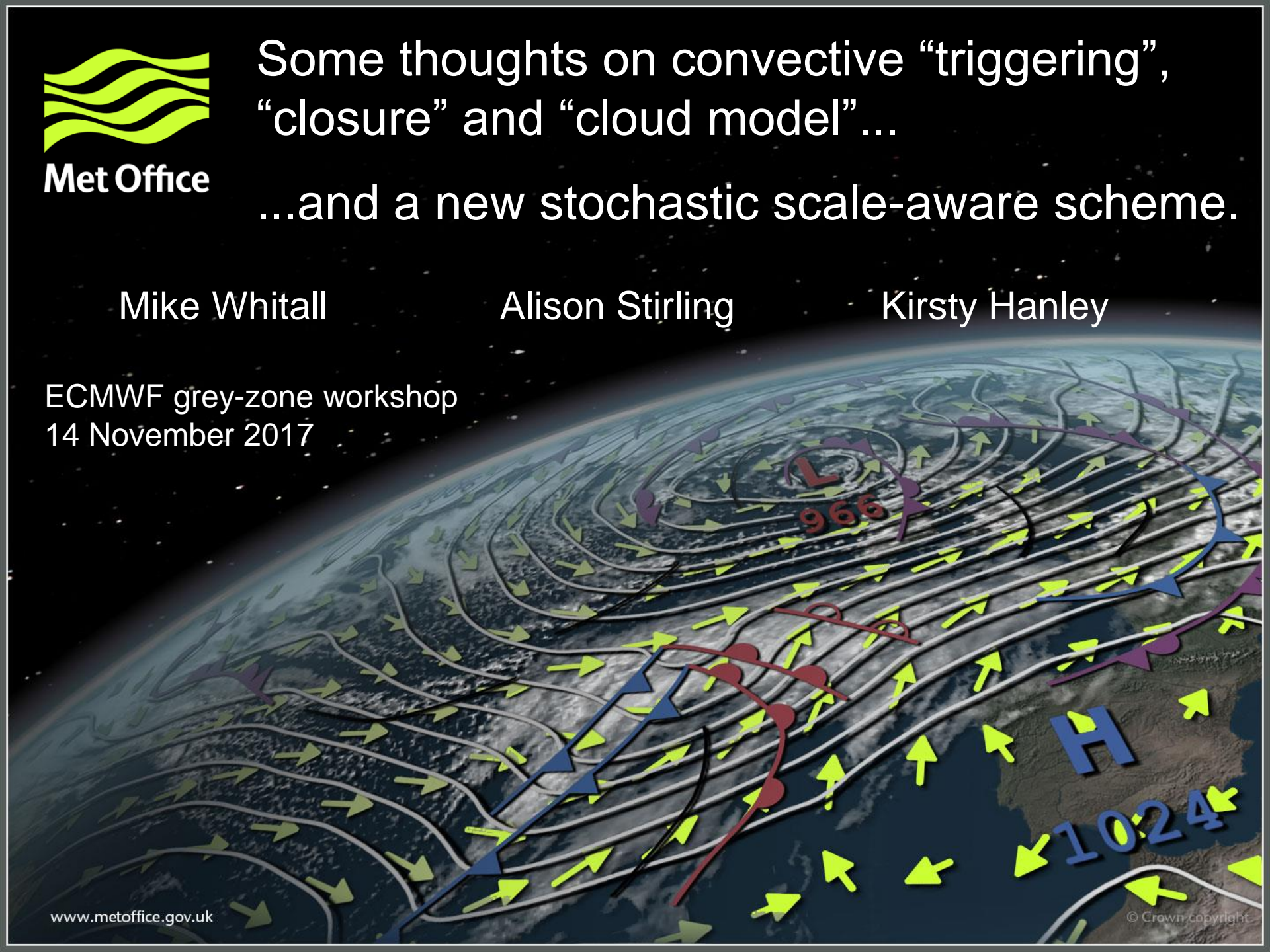
Mike Whittall

Alison Stirling

Kirsty Hanley

ECMWF grey-zone workshop

14 November 2017

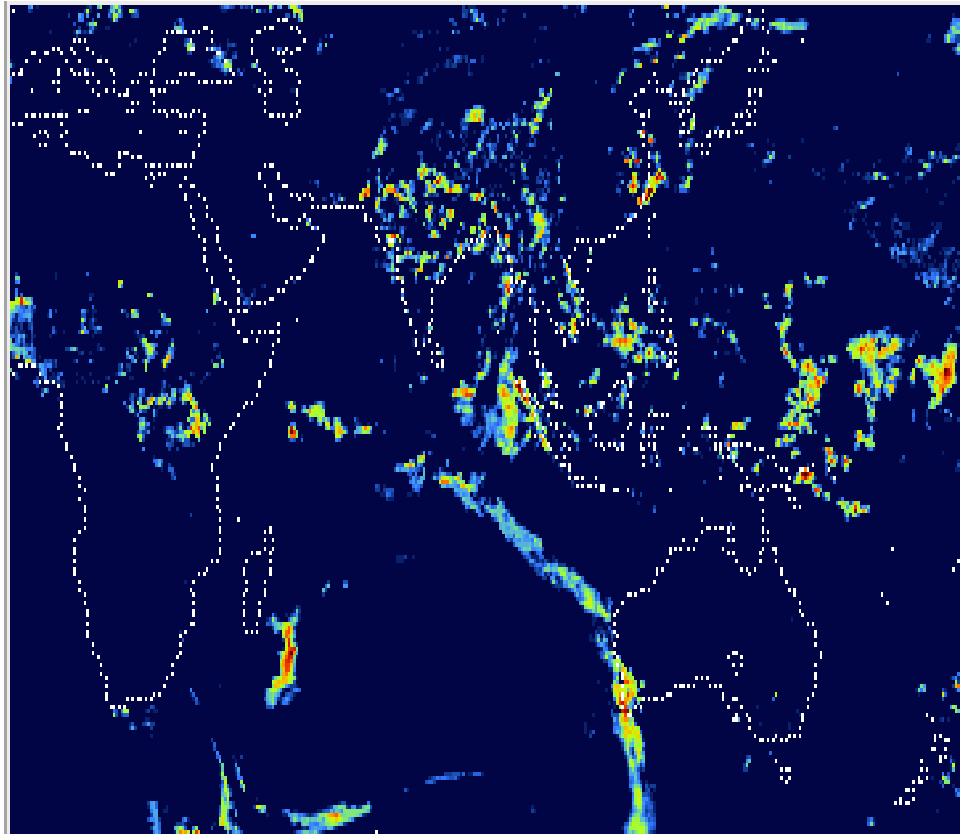


## Existing UM convection scheme:

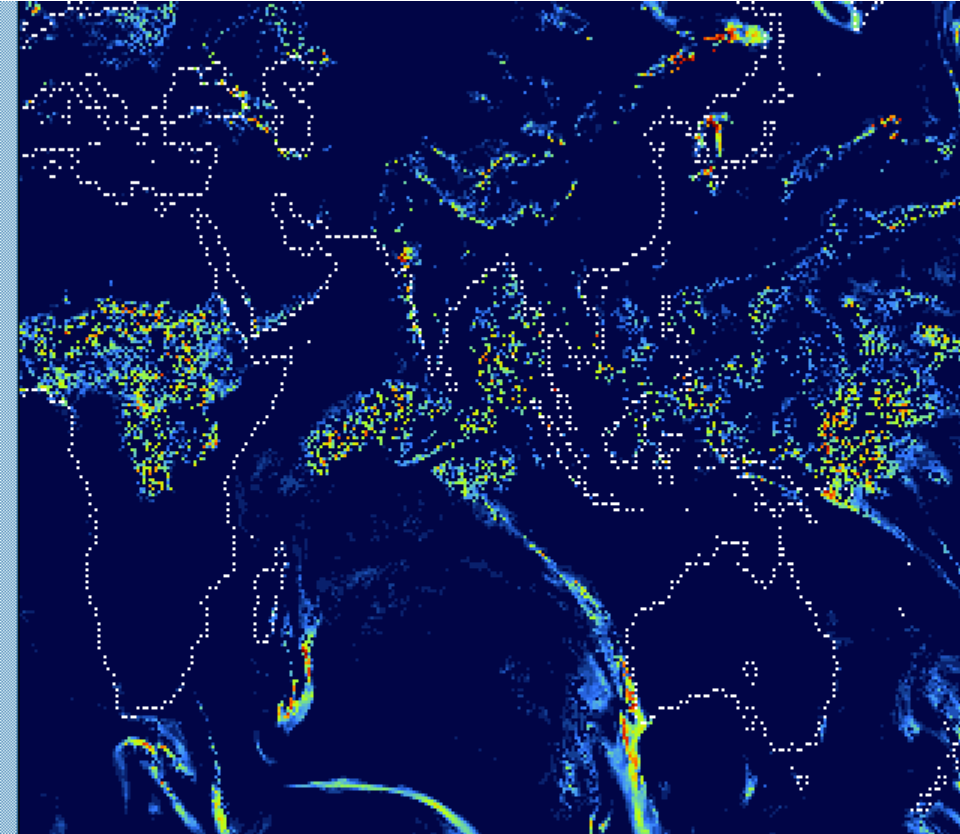
- Doesn't adapt with resolution (parameterises what should be resolvable).
- Deficient organisation on resolved scales (at all resolutions!)

Something has gone very wrong; if it is really an “equilibrium” scheme, why doesn't it yield a smooth, equilibrium behaviour?

TRMM



Met UM GA7 N320

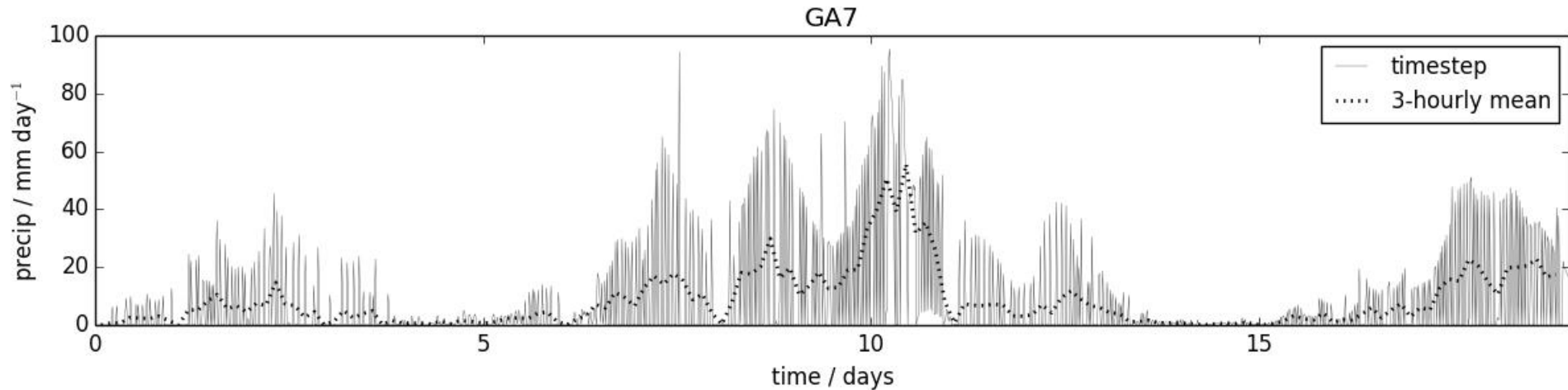


# Where to start?

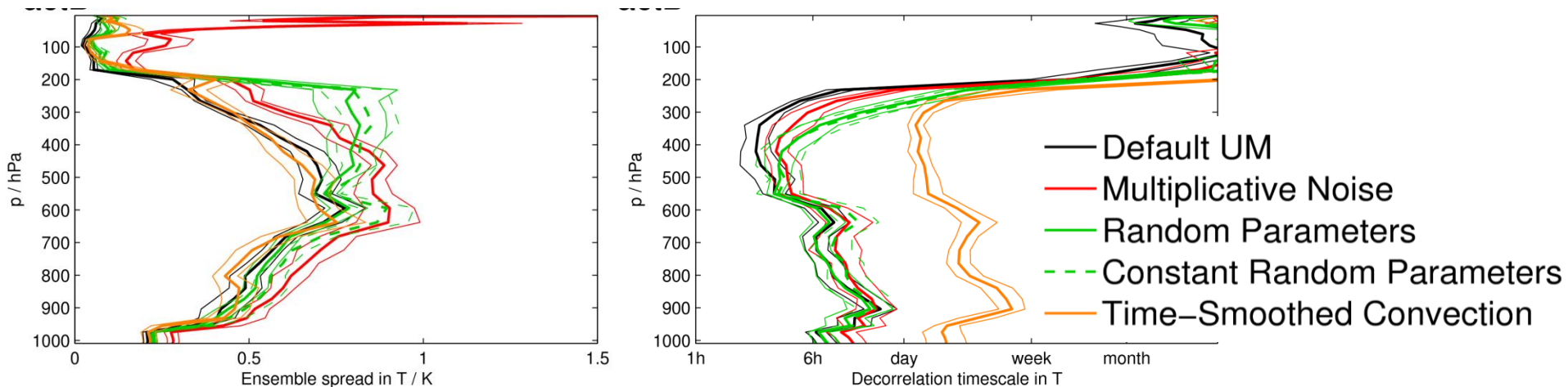
Many attempts to promote scale-awareness and/or improved organisation have focussed on modifying / perturbing the **convective closure** (c.f. SPT rescales the tendencies).

In the UM, this makes less difference than expected...

CAPE closure dysfunctional; trigger intermittency controls mean mass-flux and variability!

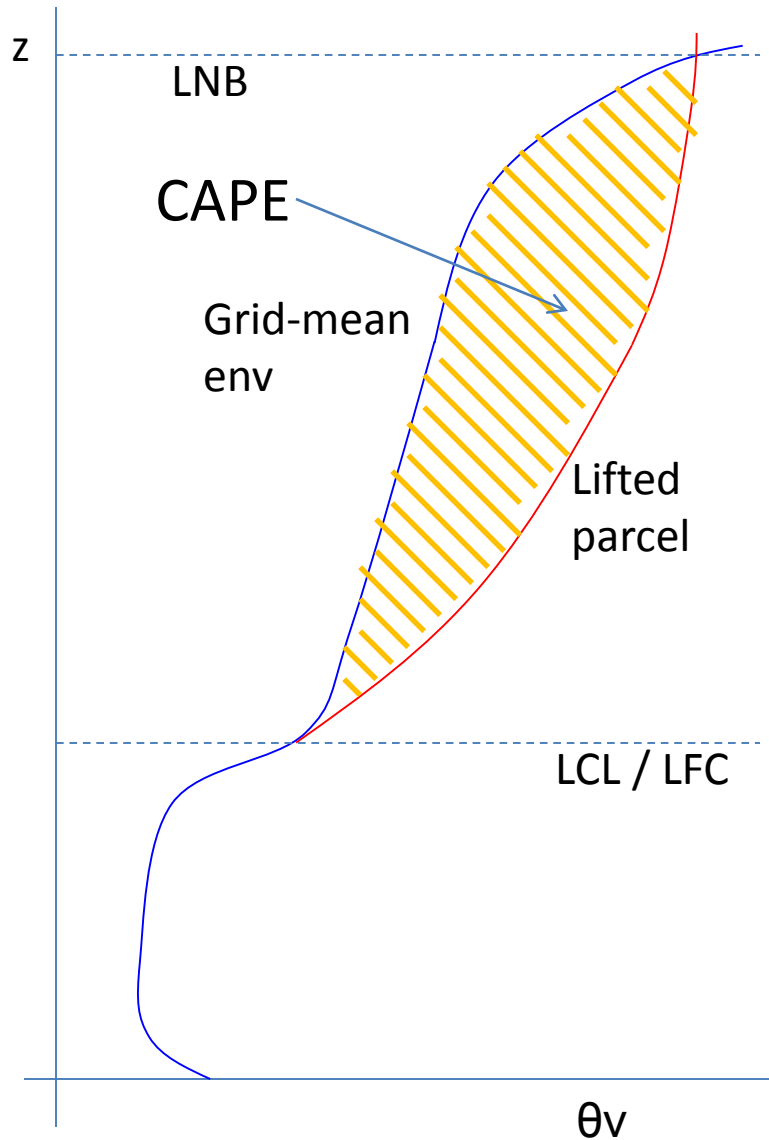


UM SCM ensemble (TOGA-COARE) – spread and decorrelation time-scale:

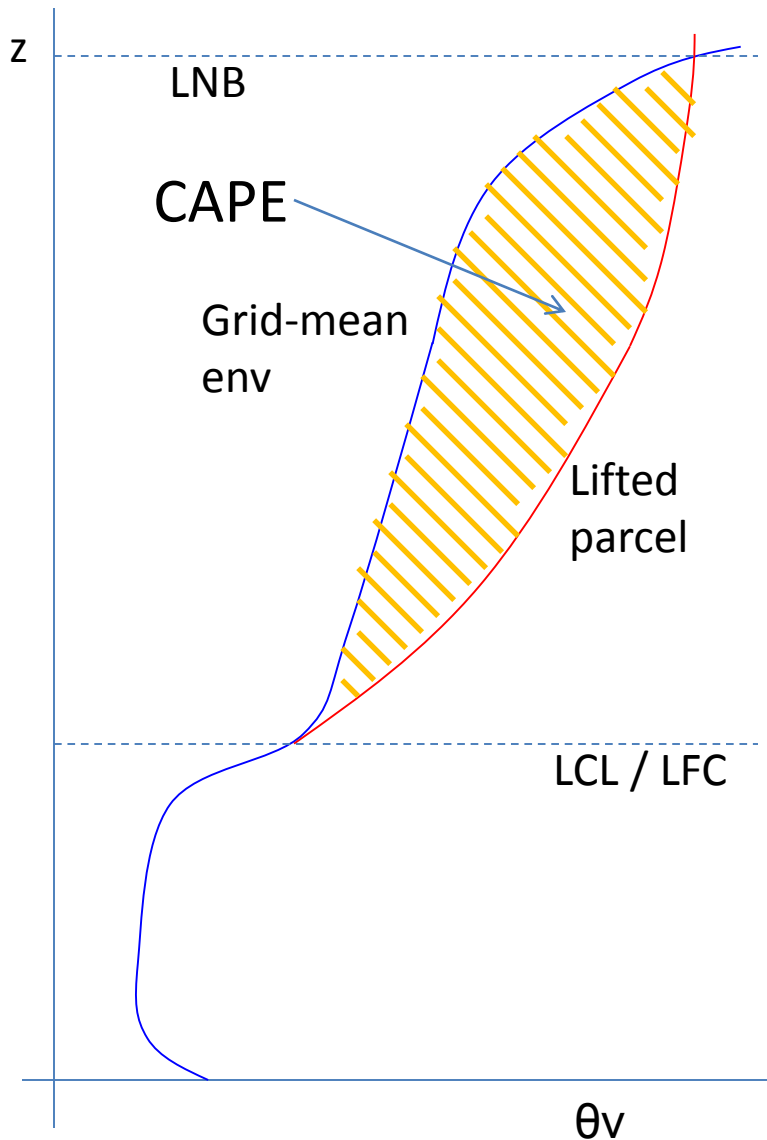


# Problem with CAPE closure

$$CAPE = \int_{z_{LFC}}^{z_{LNB}} \frac{g}{\theta_{v env}} (\theta_{v par} - \theta_{v env})$$



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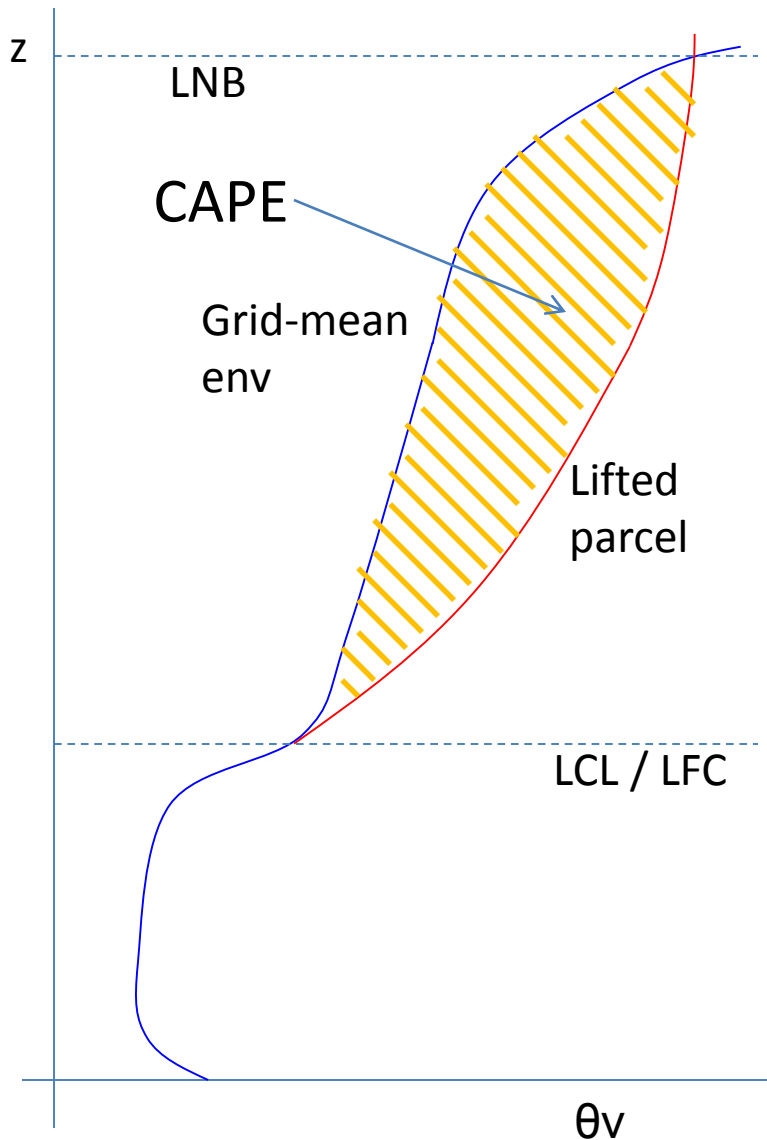


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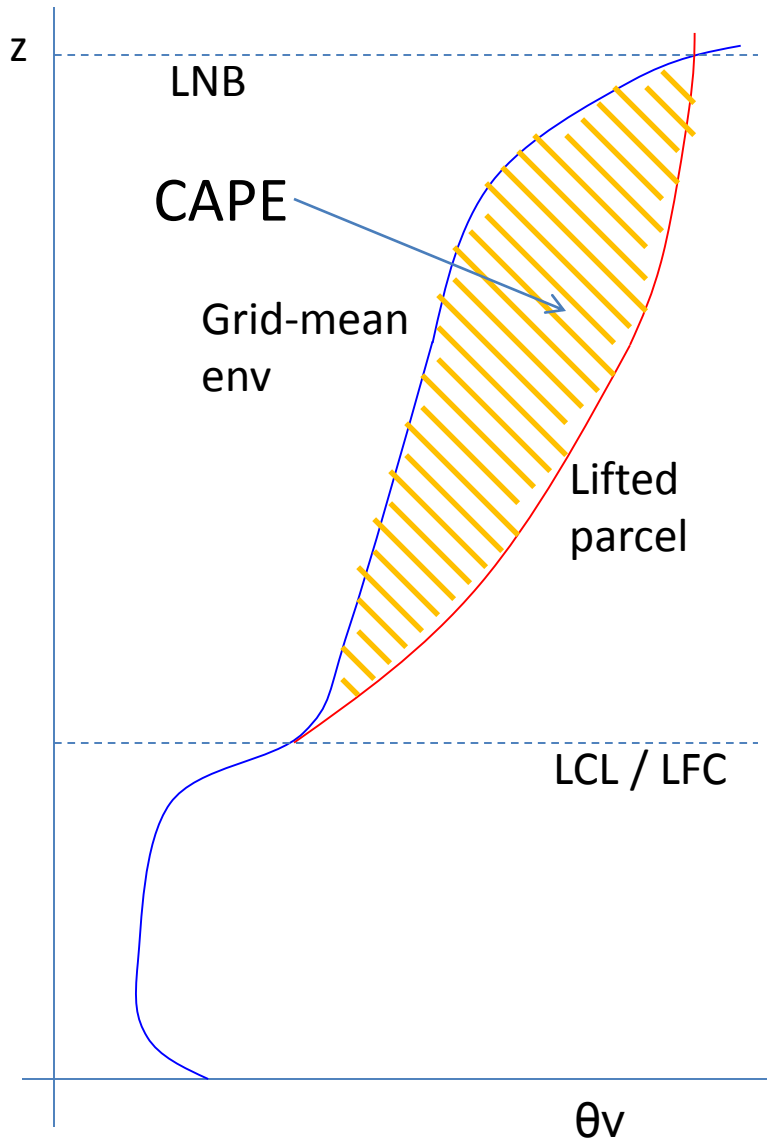
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$$M_{close} = M_{guess} \frac{CAPE}{-\tau_{CAPE} \left. \frac{\partial CAPE}{\partial t} \right|_{guess}}$$



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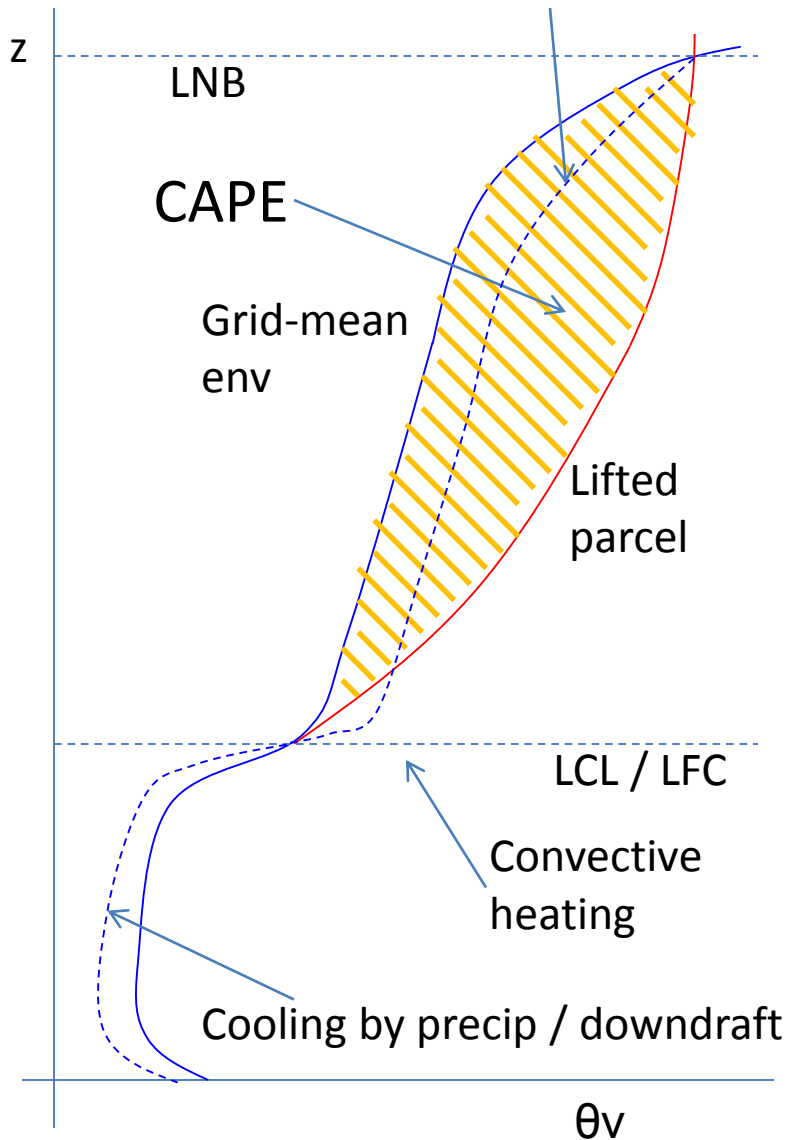
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End-of-timestep profile



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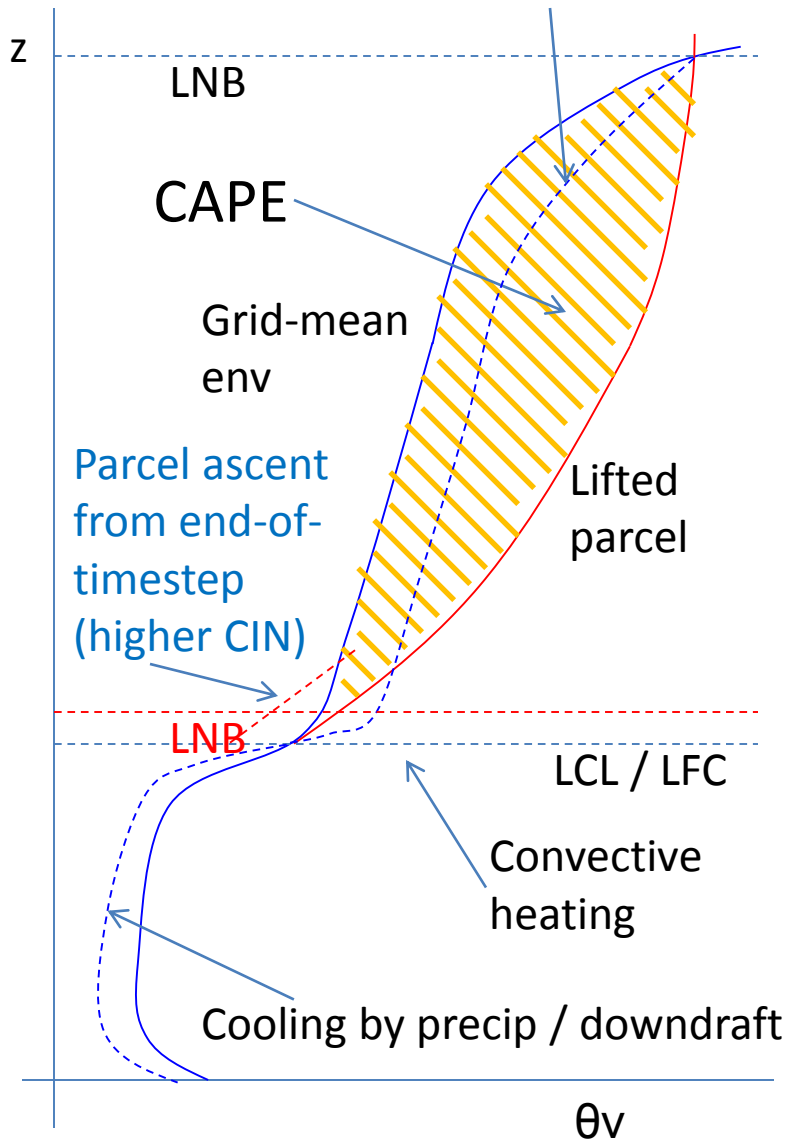
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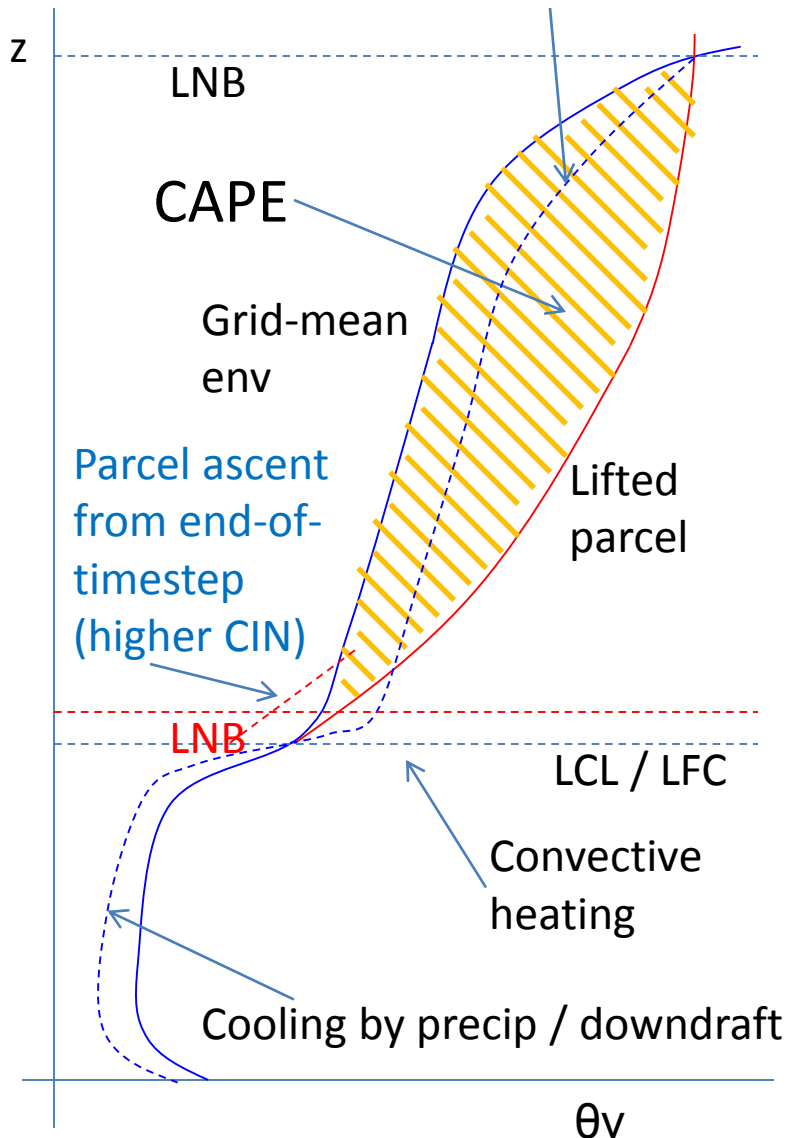
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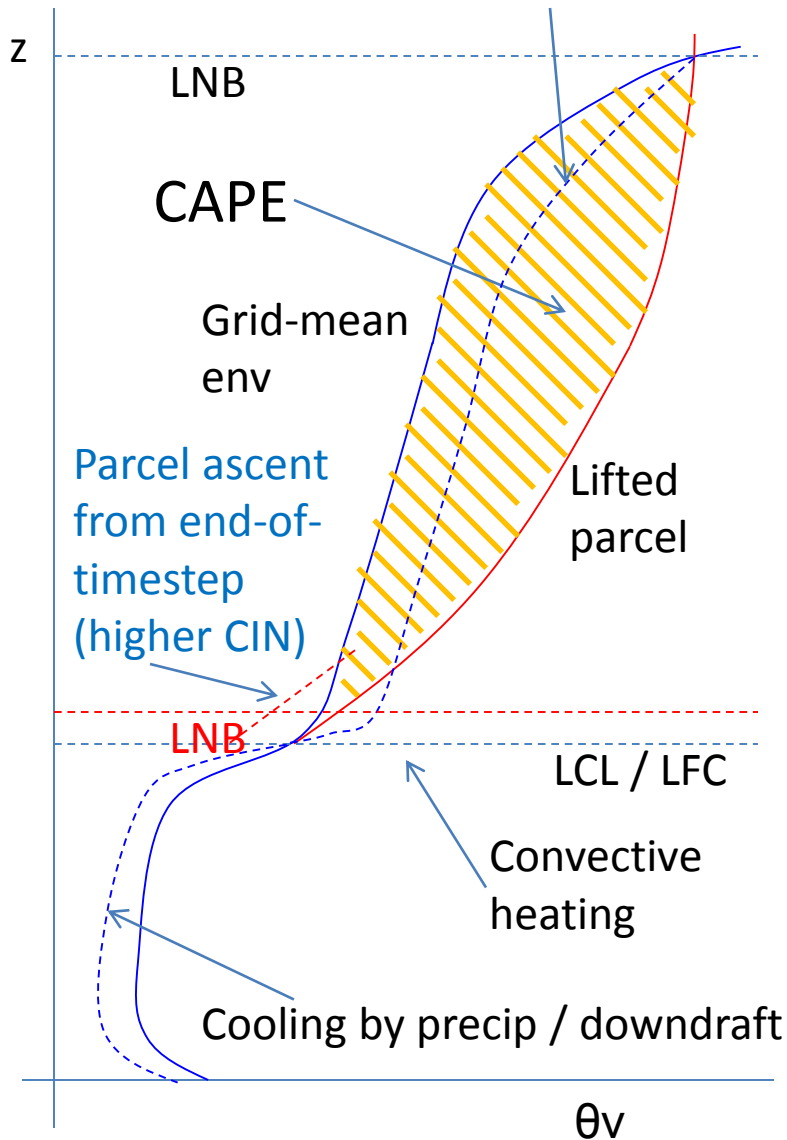
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But closure was meant to remove CAPE smoothly over time  $\tau$ ; what went wrong?

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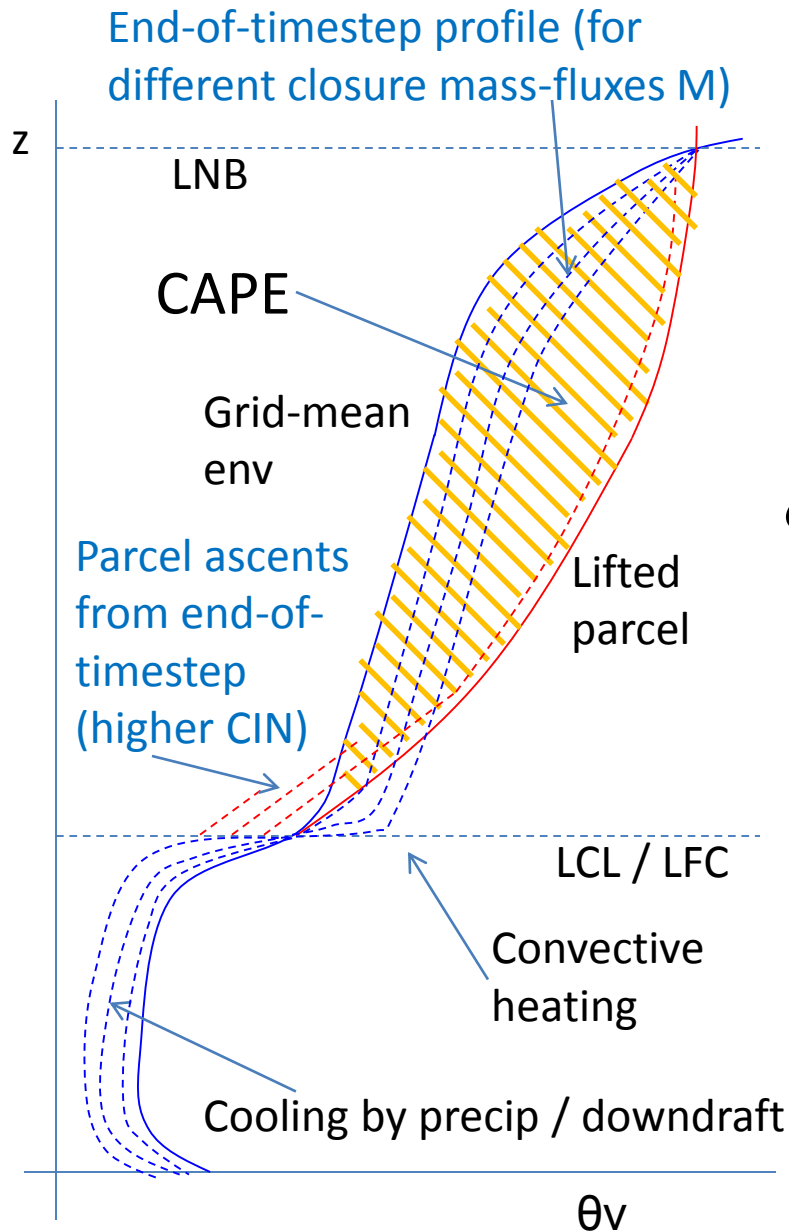
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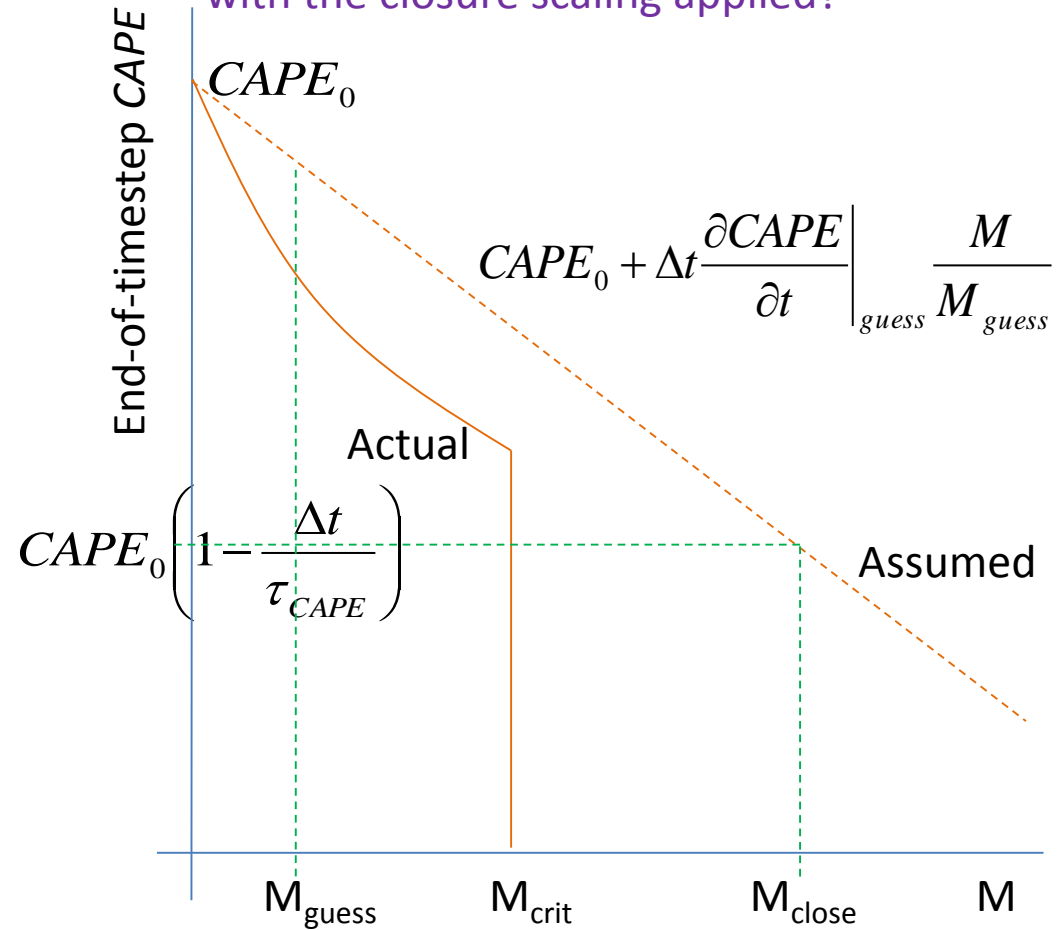
The dominant term modulating the parcel-integrated CAPE is change in  $z_{LNB}$  (neglected), when increased CIN causes the parcel to terminate below the LFC ( $\rightarrow$  CAPE suddenly drops to zero, convection not triggered).

Closure formula assumes  $\Delta CAPE$  over the timestep scales linearly with  $M$ , but it doesn't...

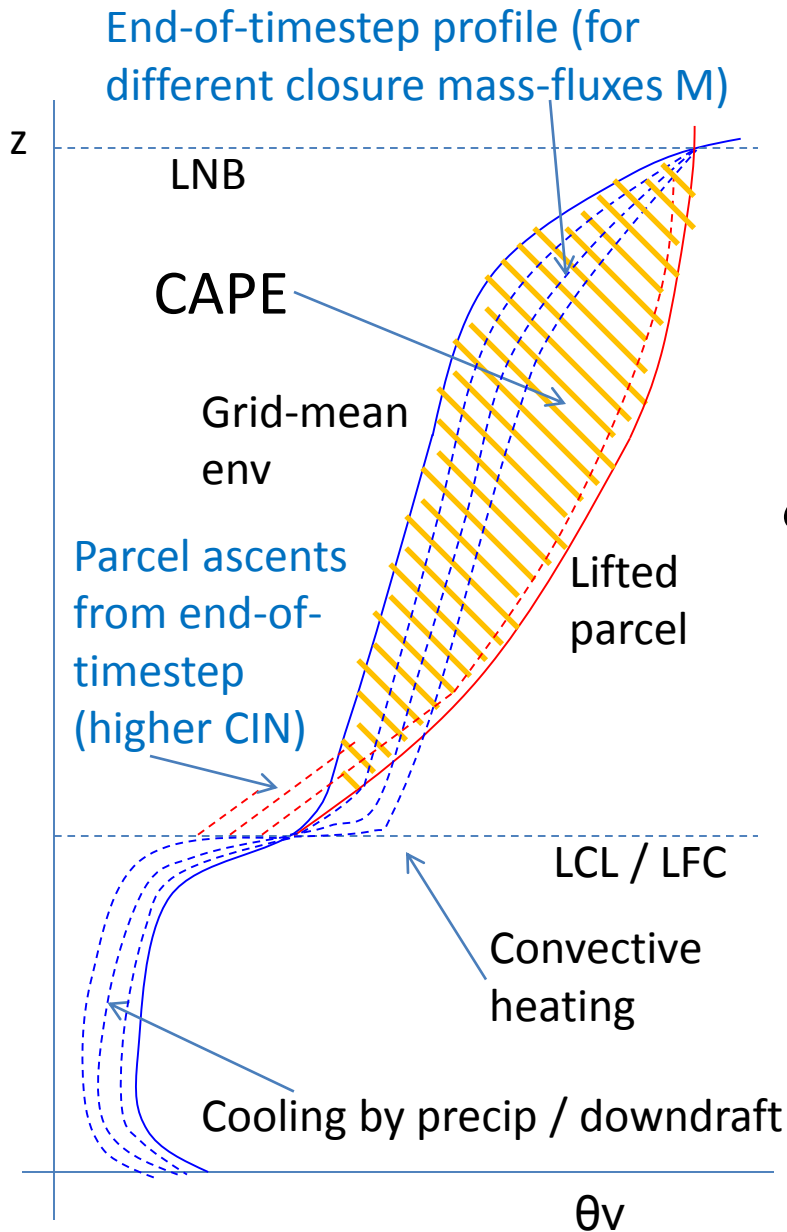
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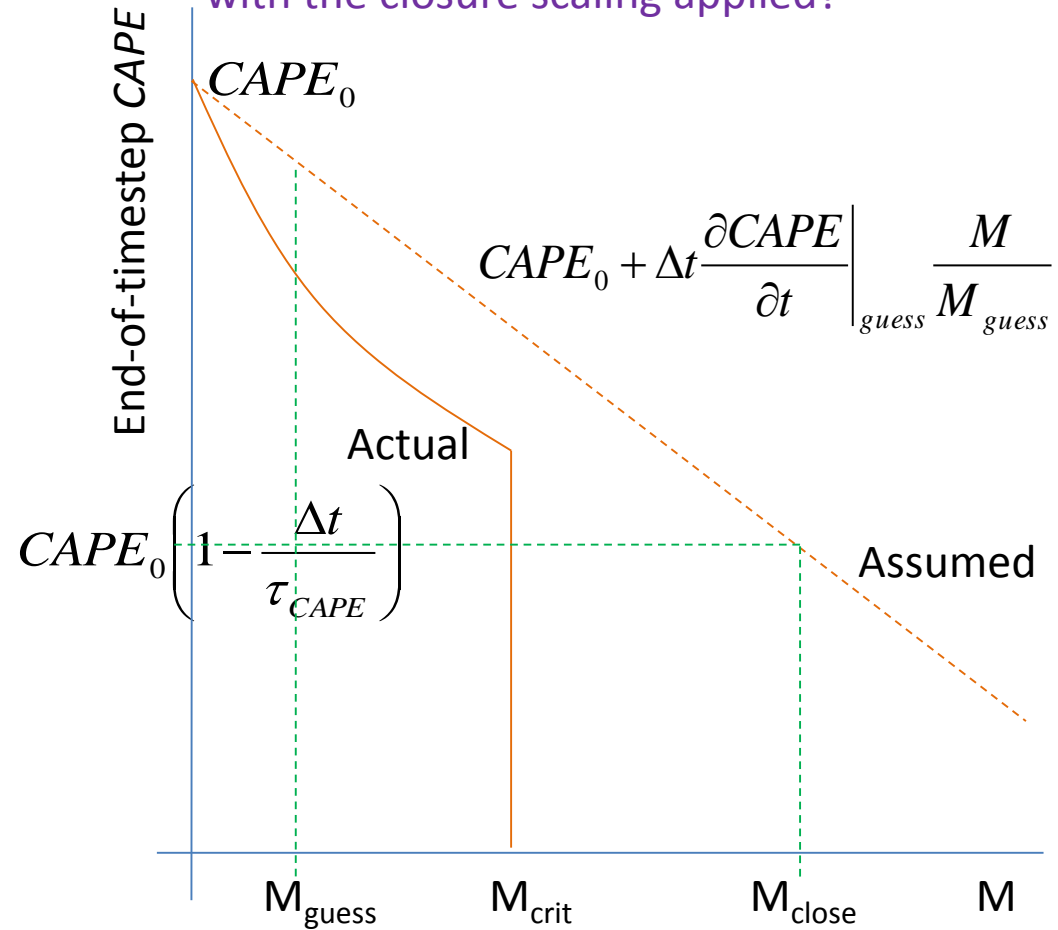
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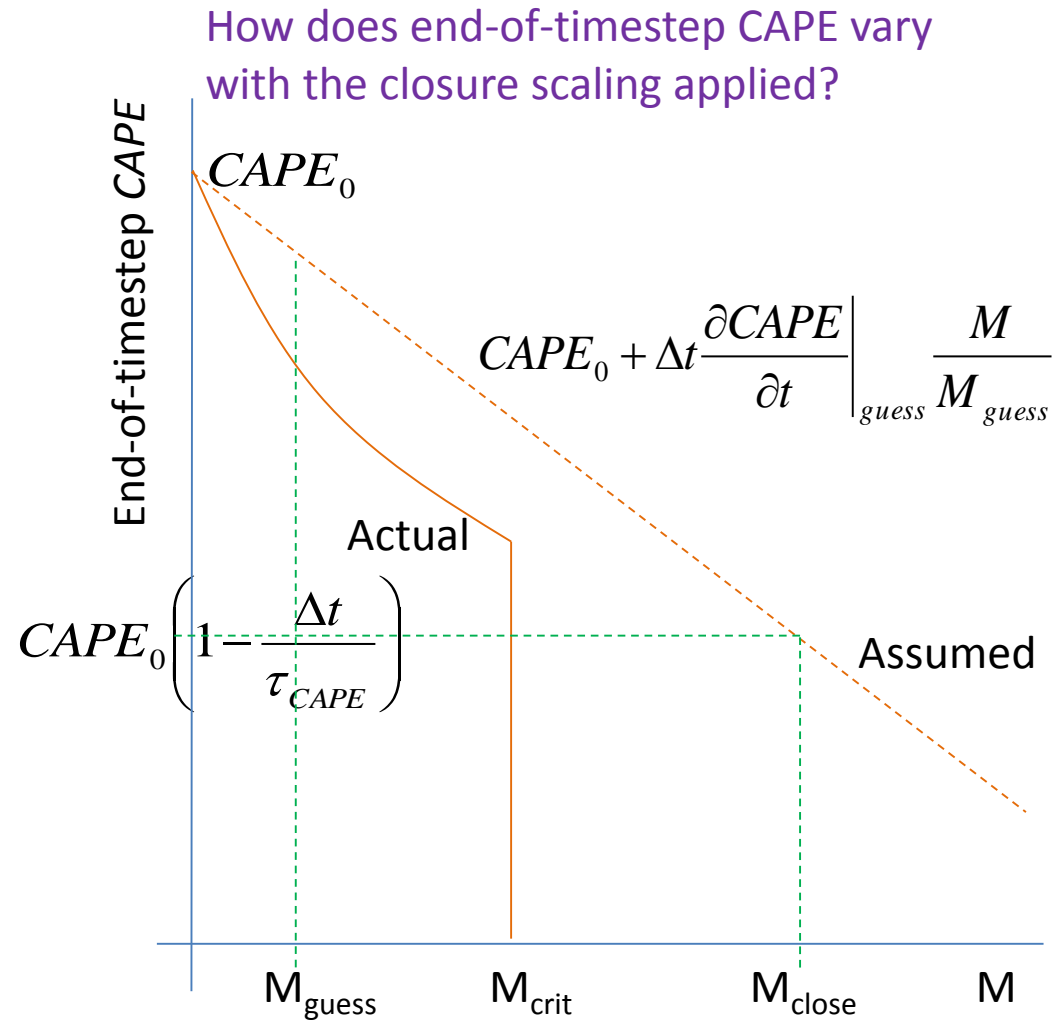
Final parcel-integrated CAPE highly non-linear function of mass-flux.

Often no solution yielding smooth reduction of CAPE over the timescale.

**This closure is fundamentally ill-posed!**

# Problem with CAPE closure

Can't we just use a much longer CAPE timescale, so that we don't get into the "on-off" regime?



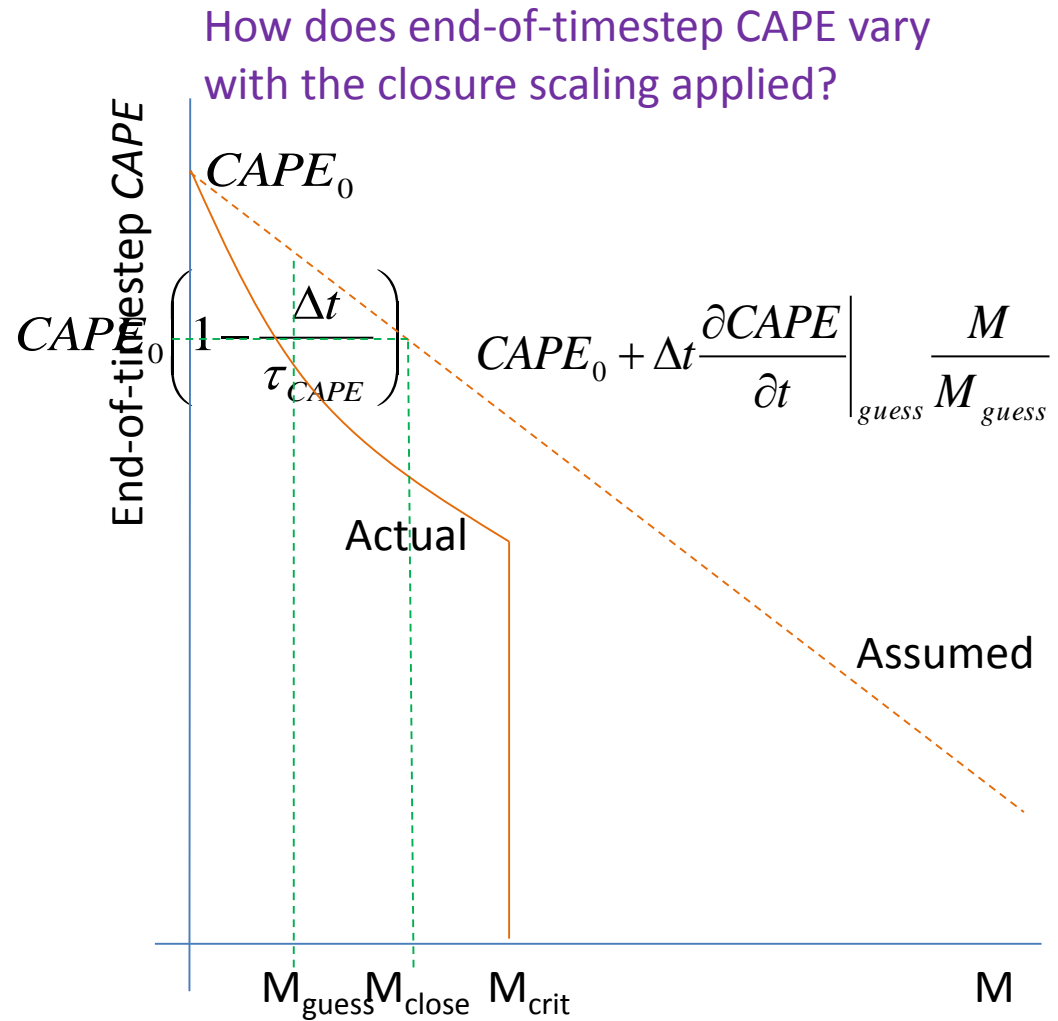
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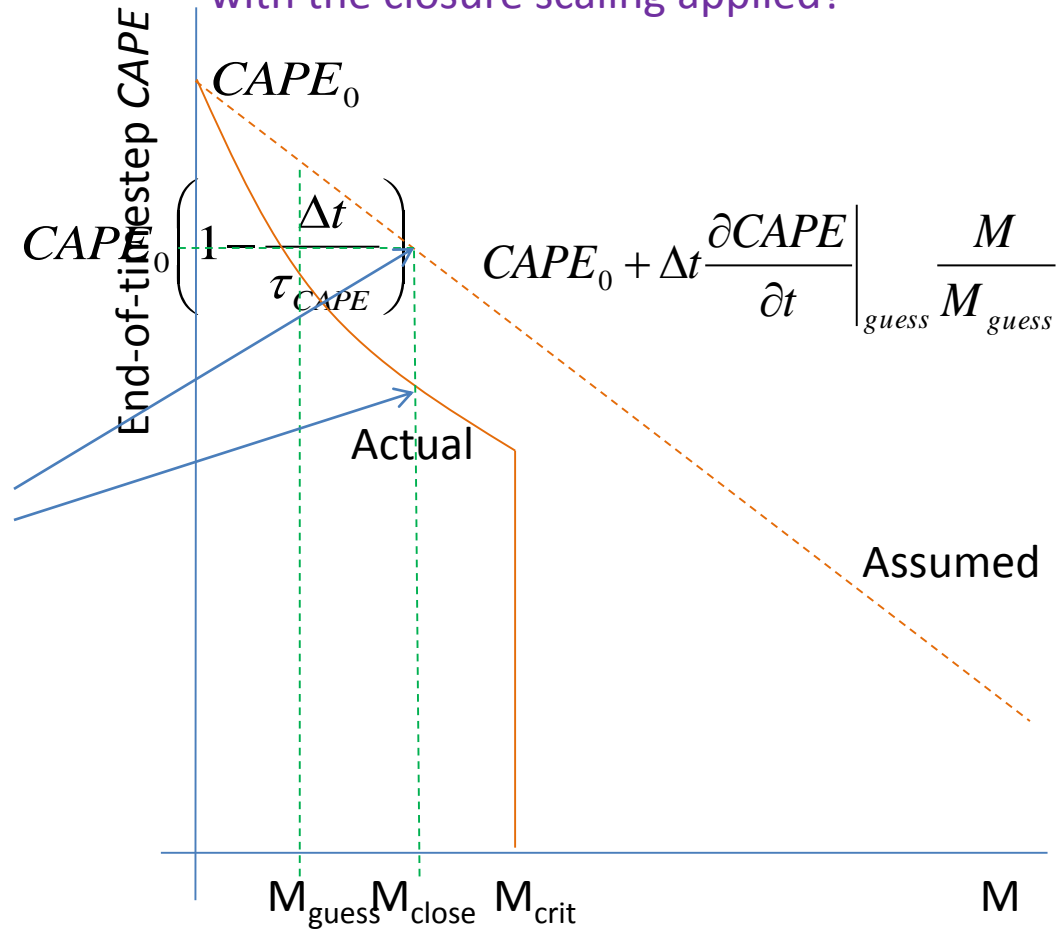


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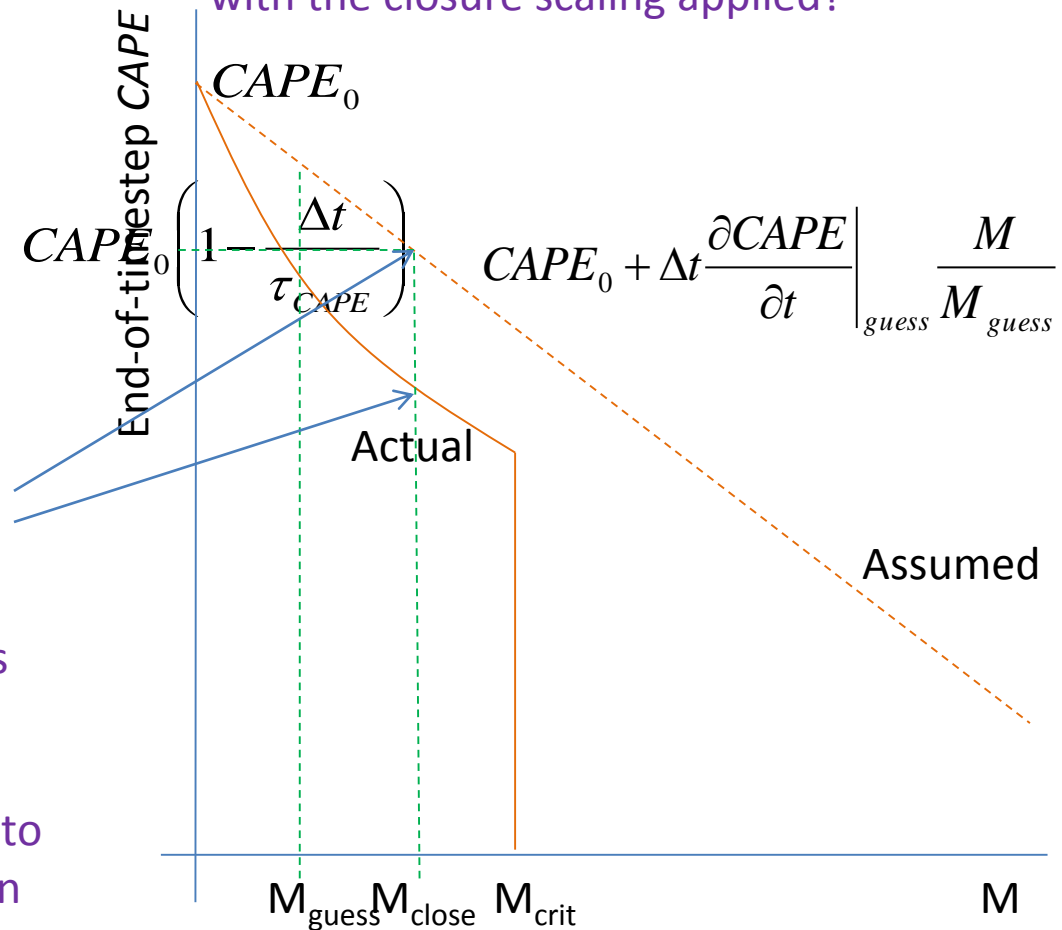
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Operationally, long CAPE timescales give poor performance. It is important that the convection scheme *can* give a strong response to a strong resolved-scale forcing, even when CAPE isn't that large

(otherwise, strongly forced systems such as Tropical cyclones spuriously dissipate!)

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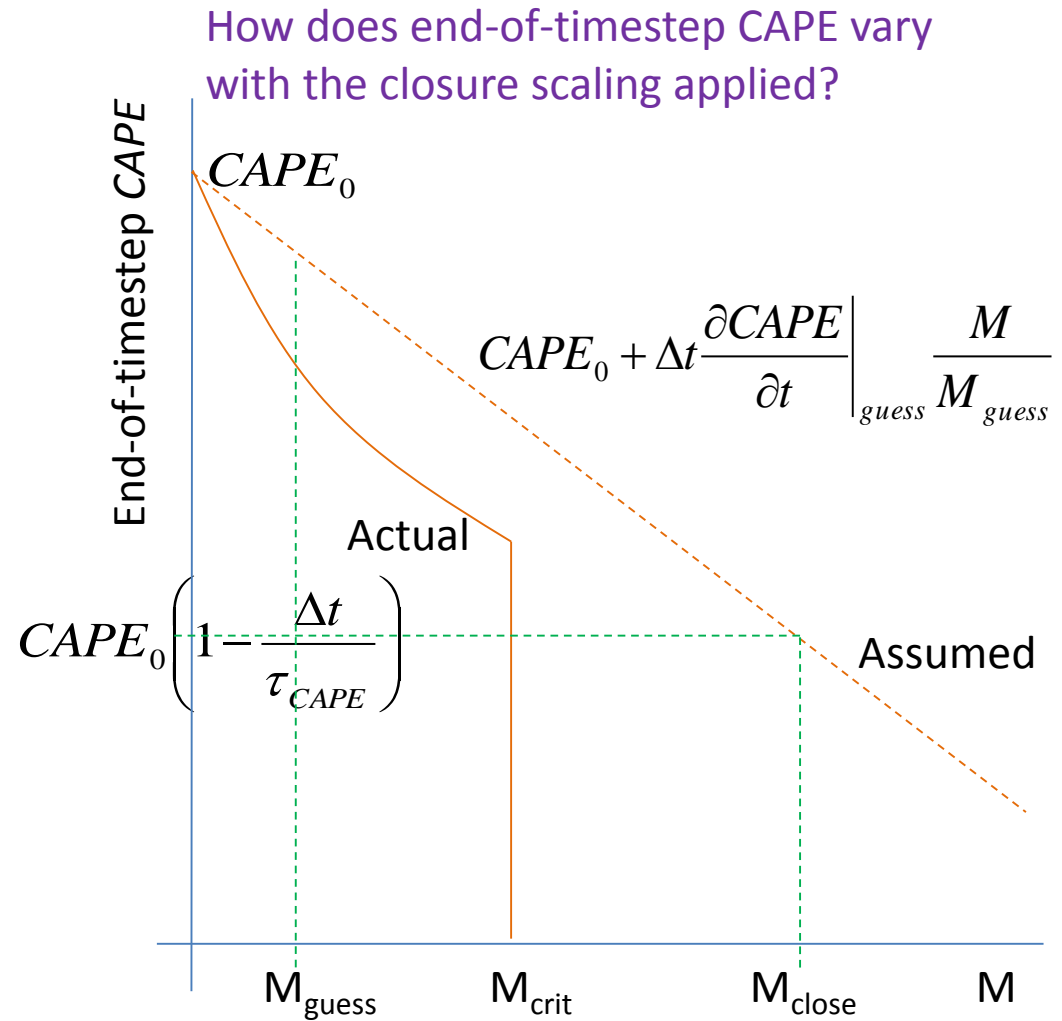
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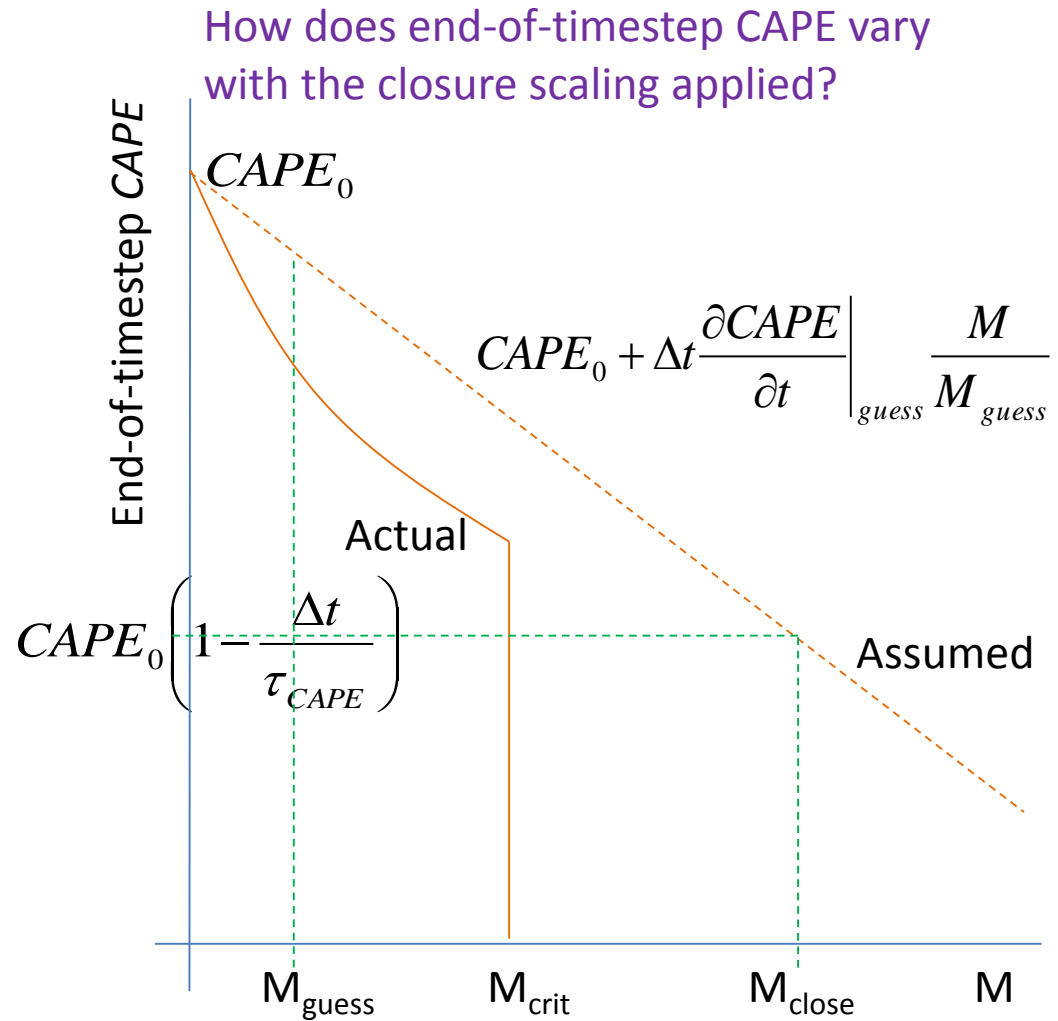
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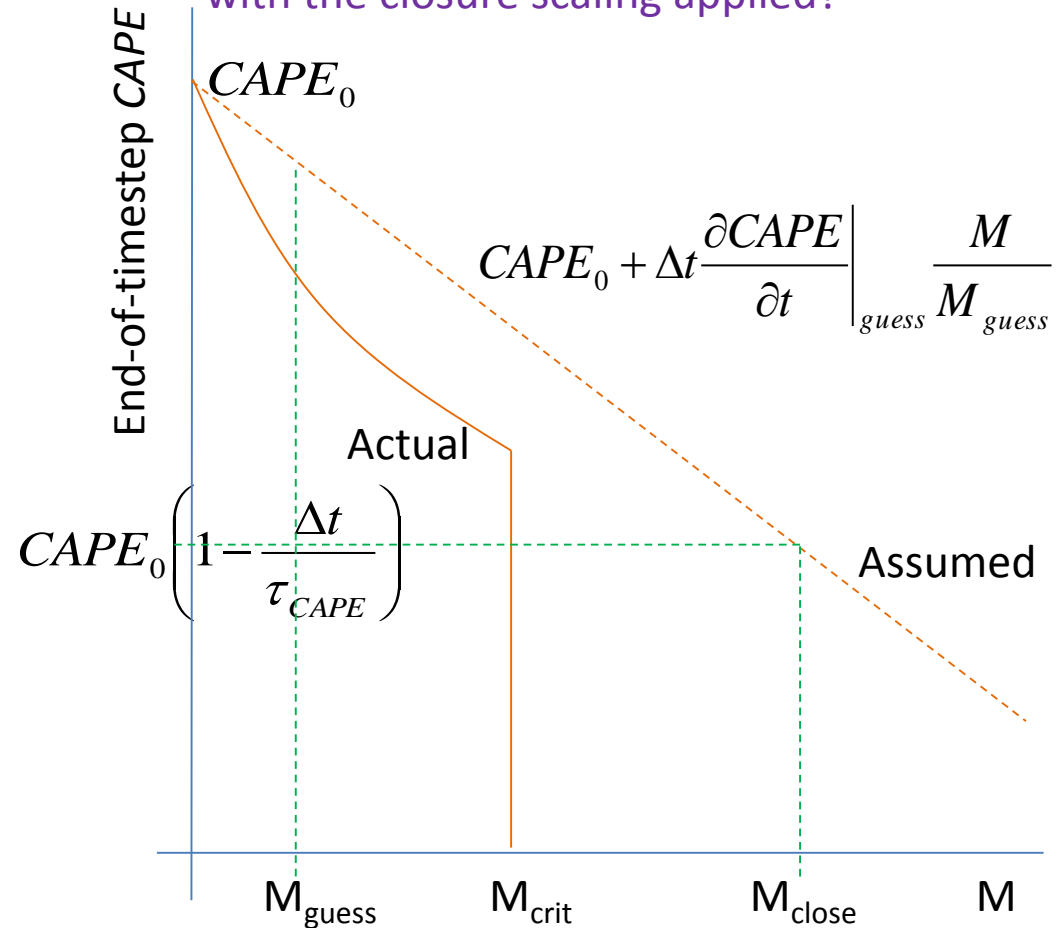
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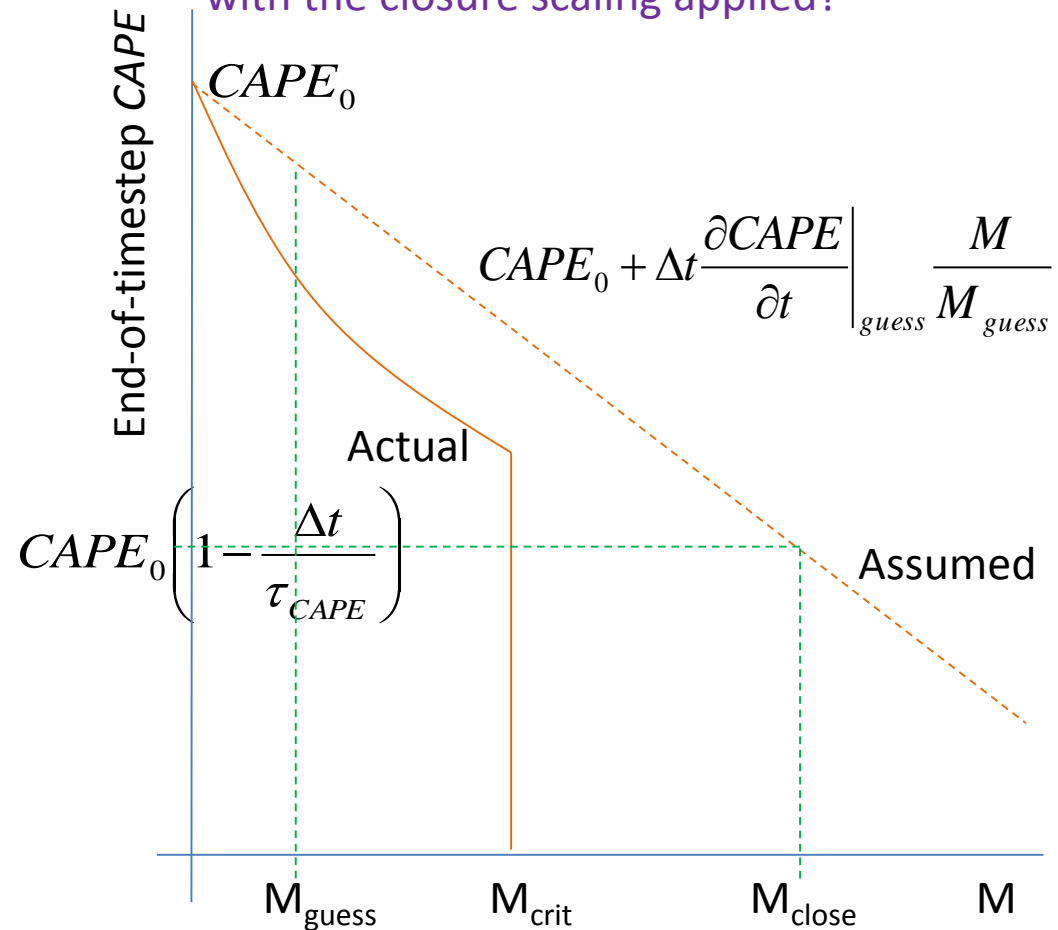
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("triggering" is basically just a termination height estimate for the updraft below cloud-base).

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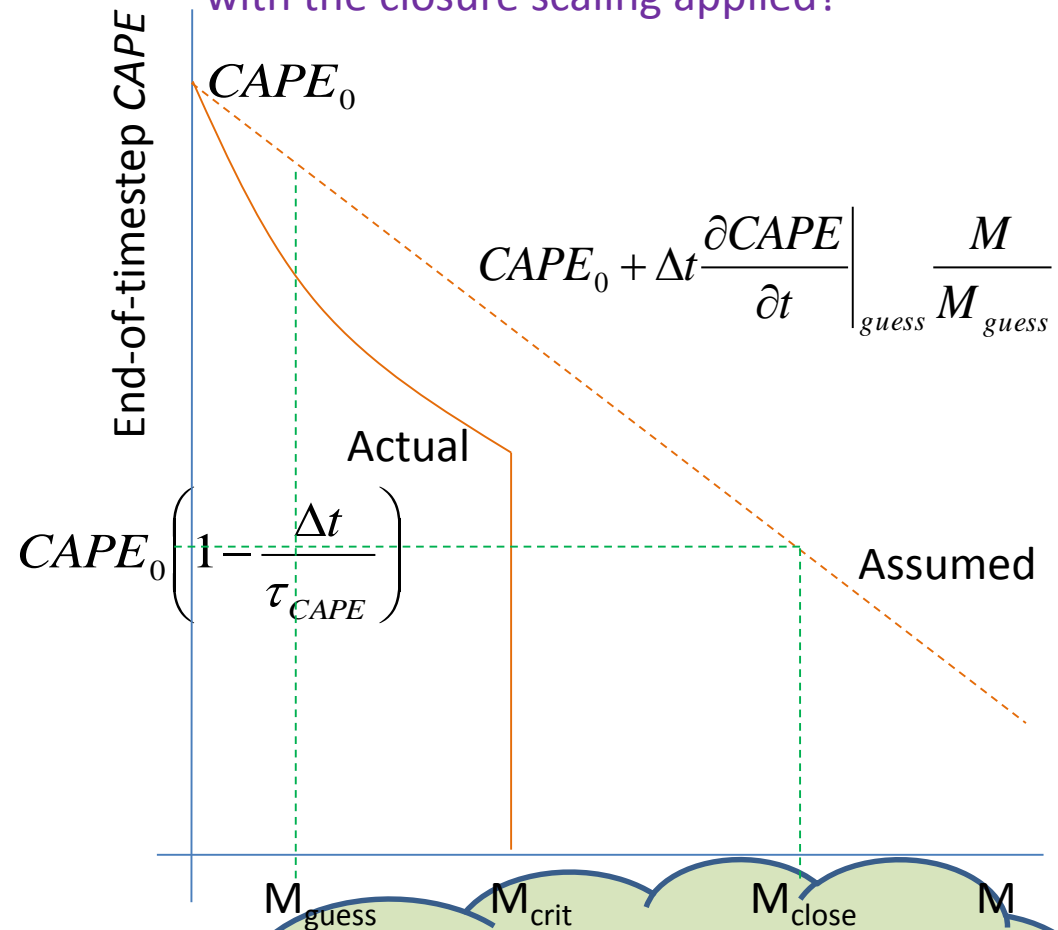
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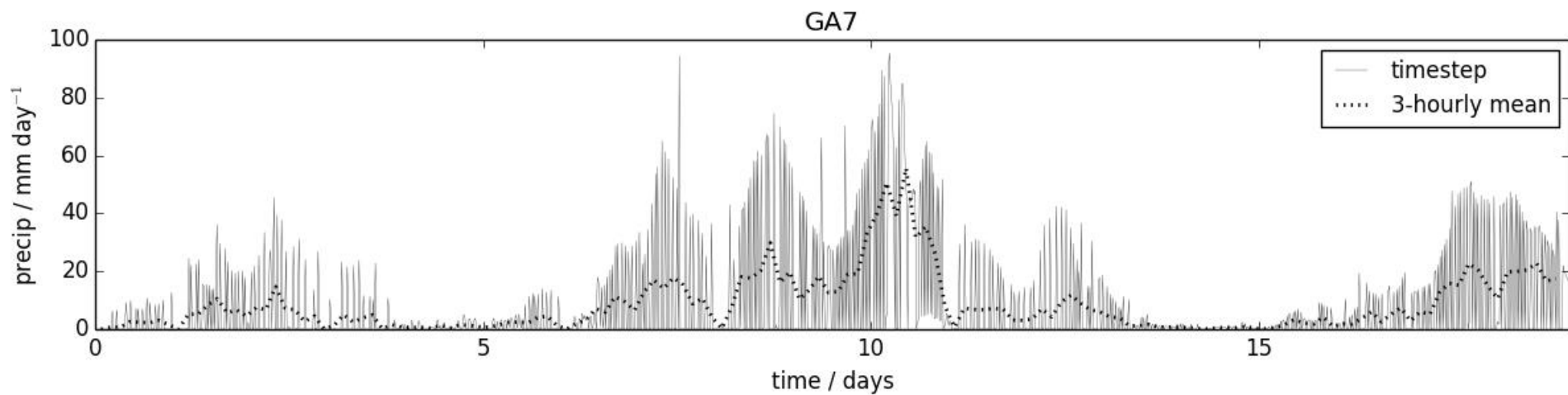


Now we're saying that, in order to make our *diagnostic equilibrium* CAPE closure work, we have to make the cloud model *prognostic*!  
Does that make any sense?



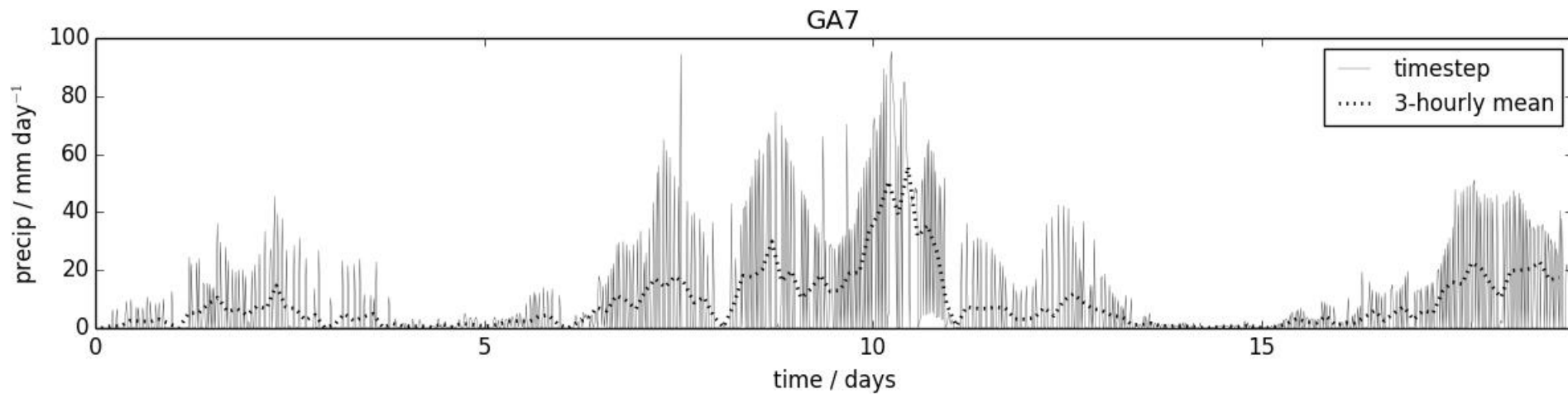
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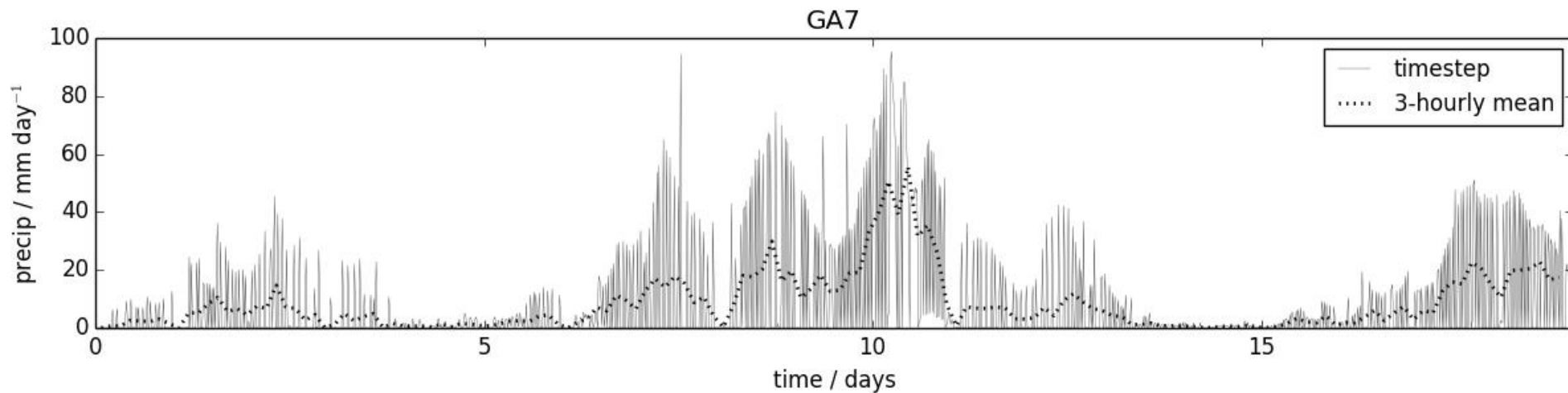
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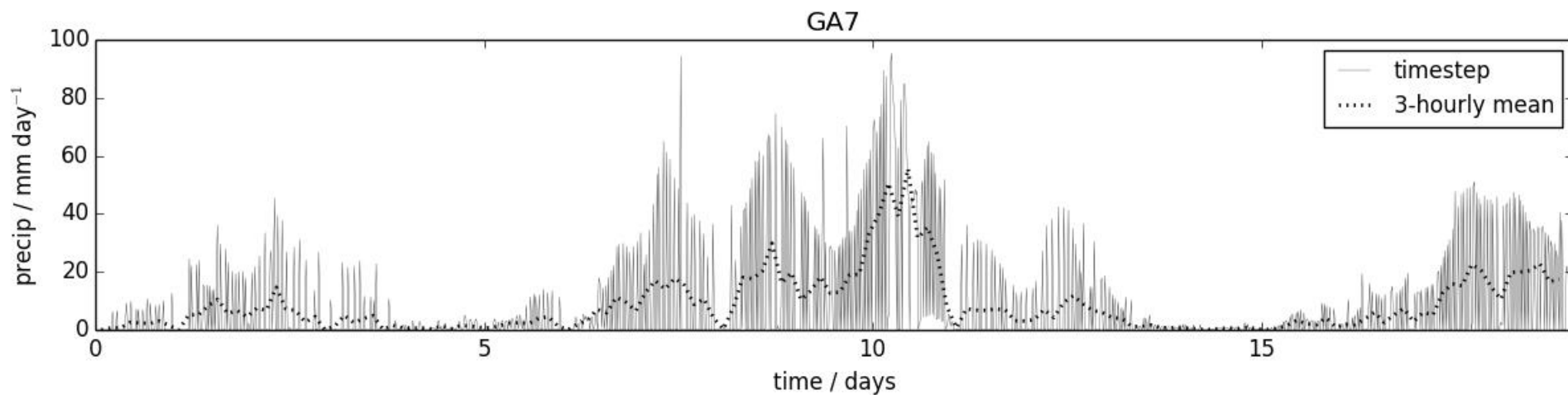
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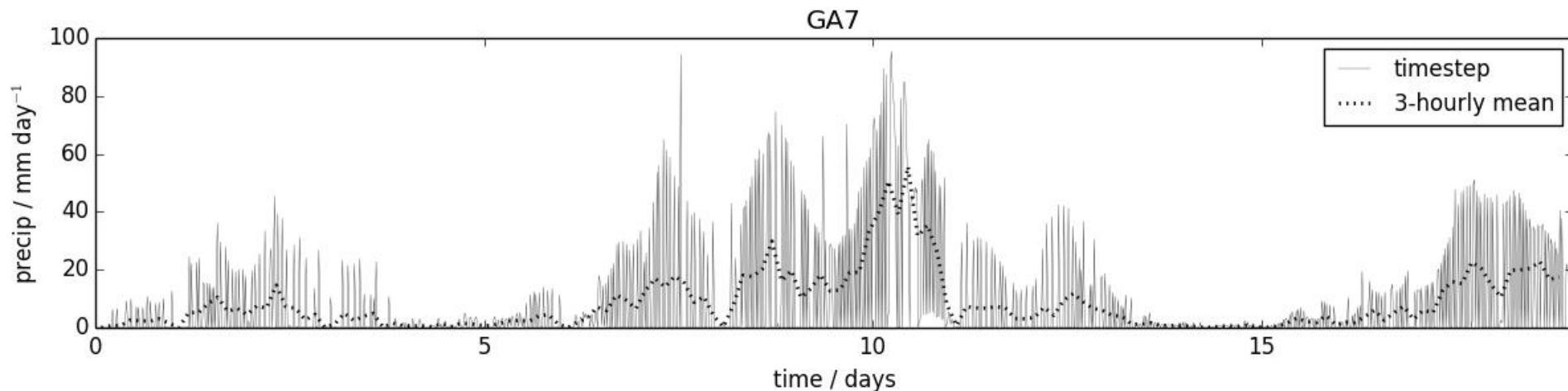
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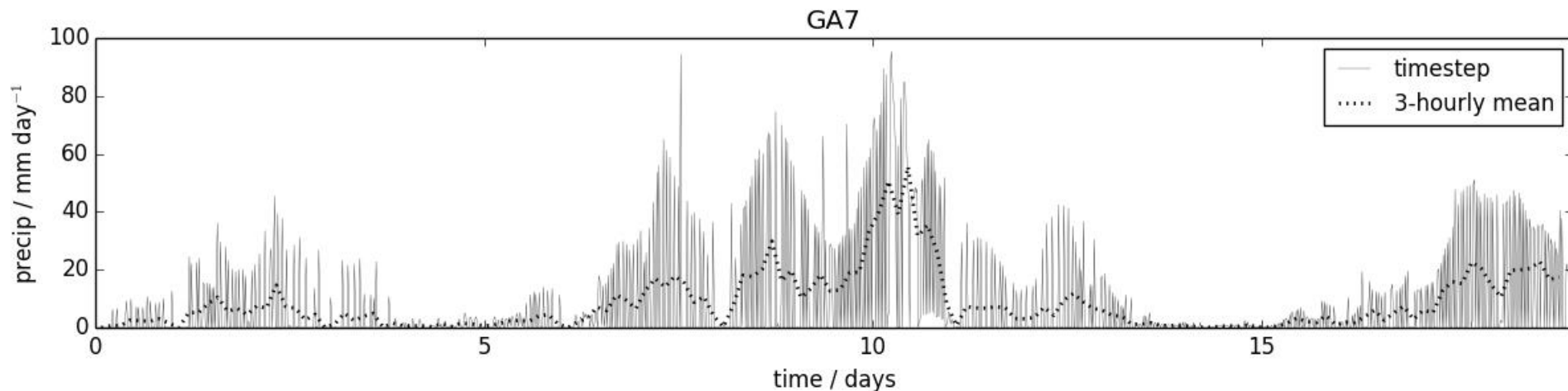
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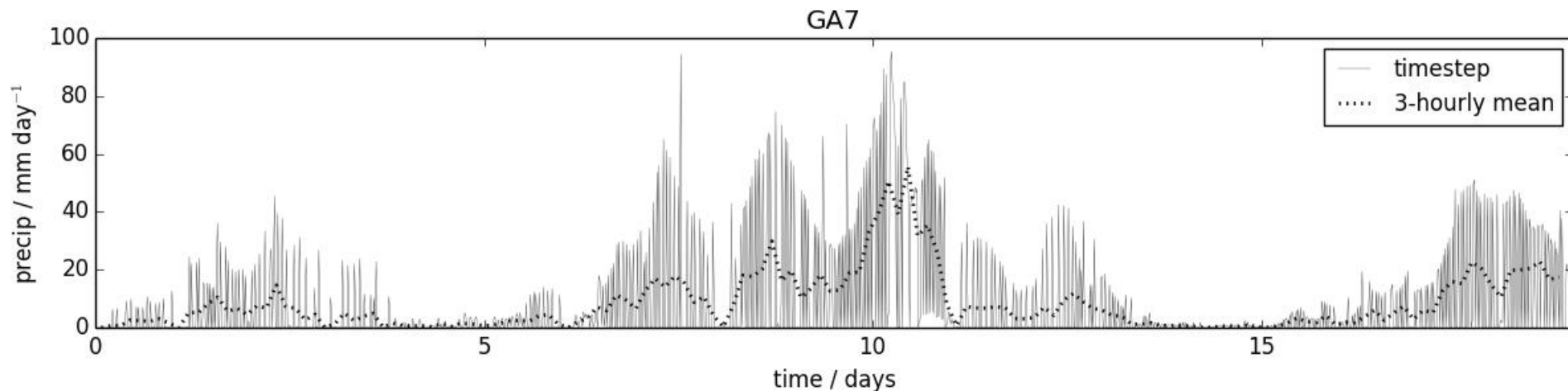
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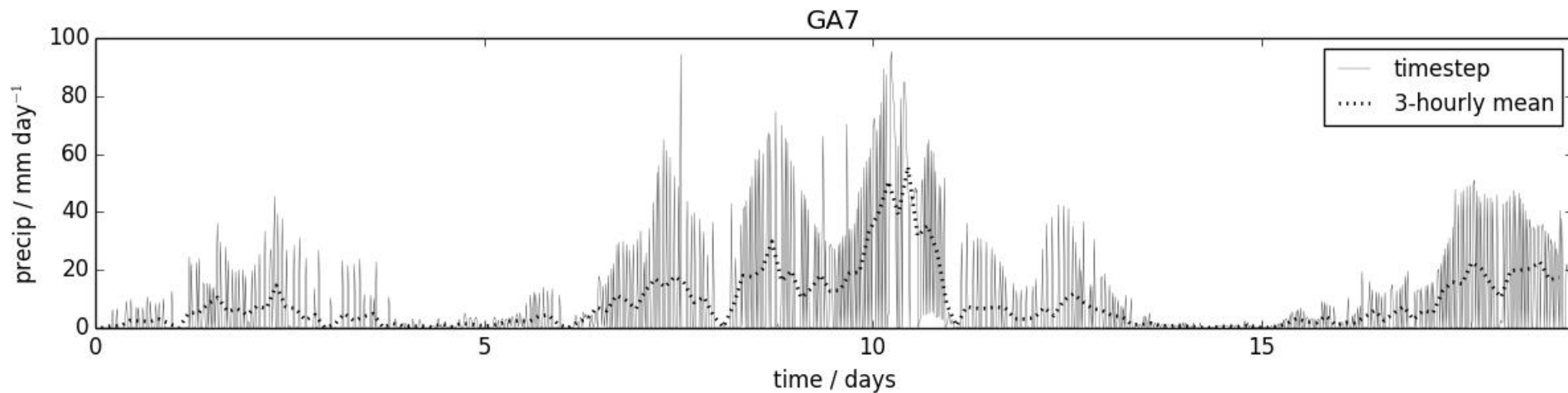
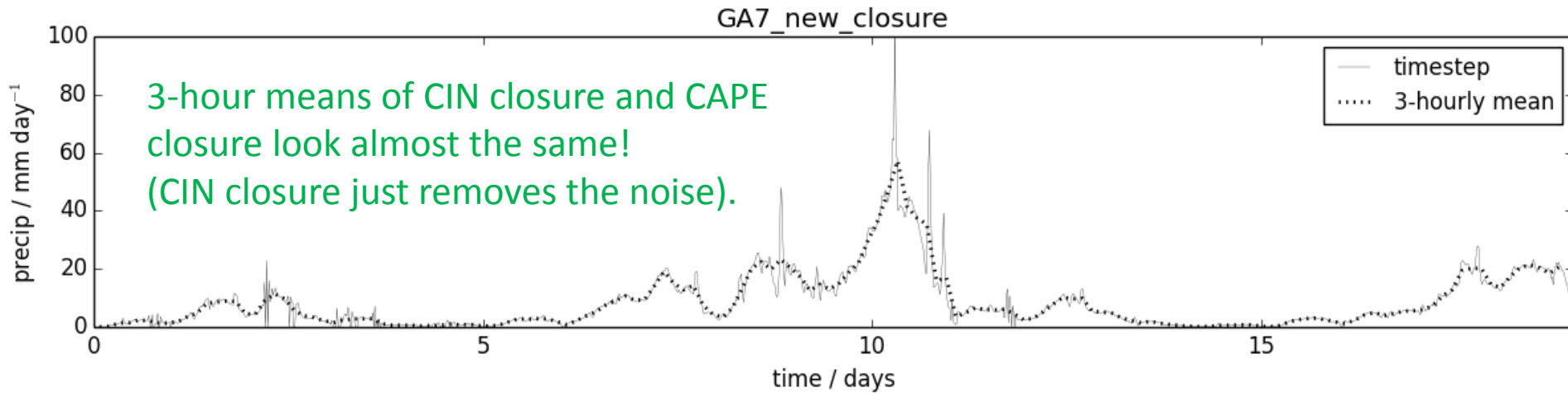
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(unless closure time-scale is long enough to impose a stronger restriction than the triggering, but this is detrimental to strongly-forced systems).
- Thinking of them as separate entities is what got us into this mess!





# Summary so far

Experiment with CIN closure; just set mass-flux to largest value we can “get away with” without shutting off the convection on the next timestep (requires iteration):



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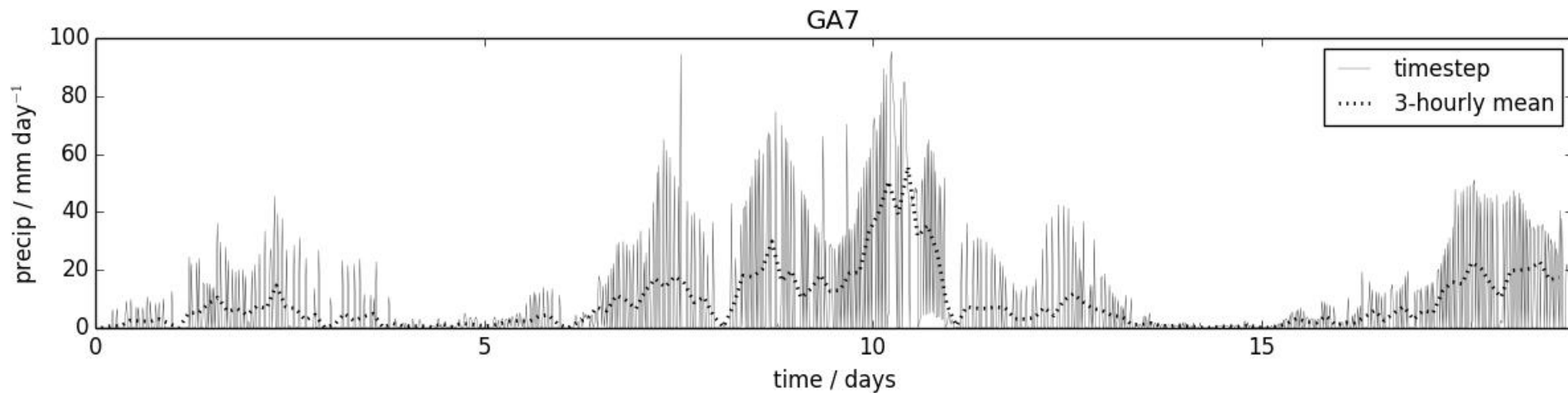
Some wise words:

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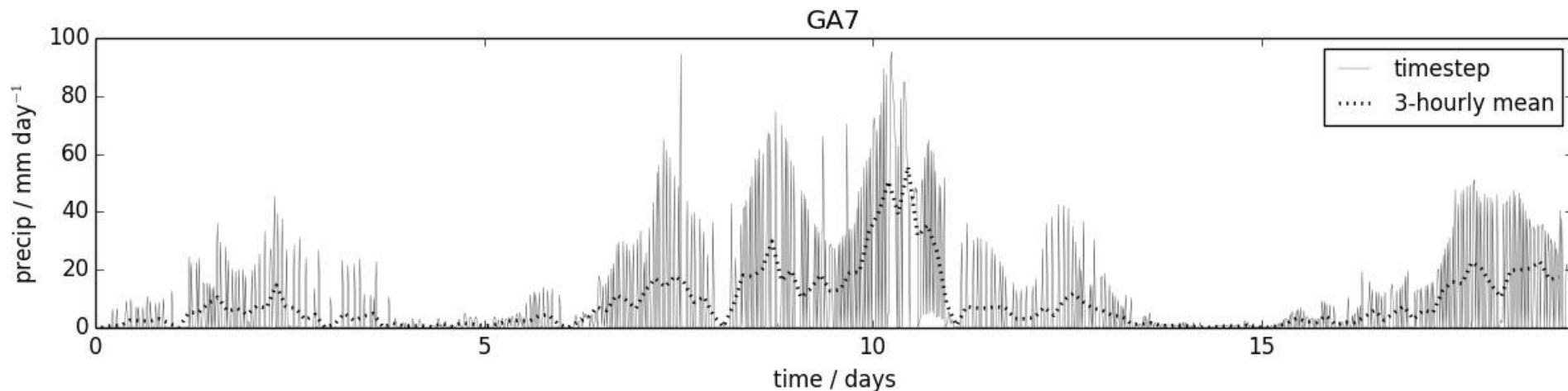
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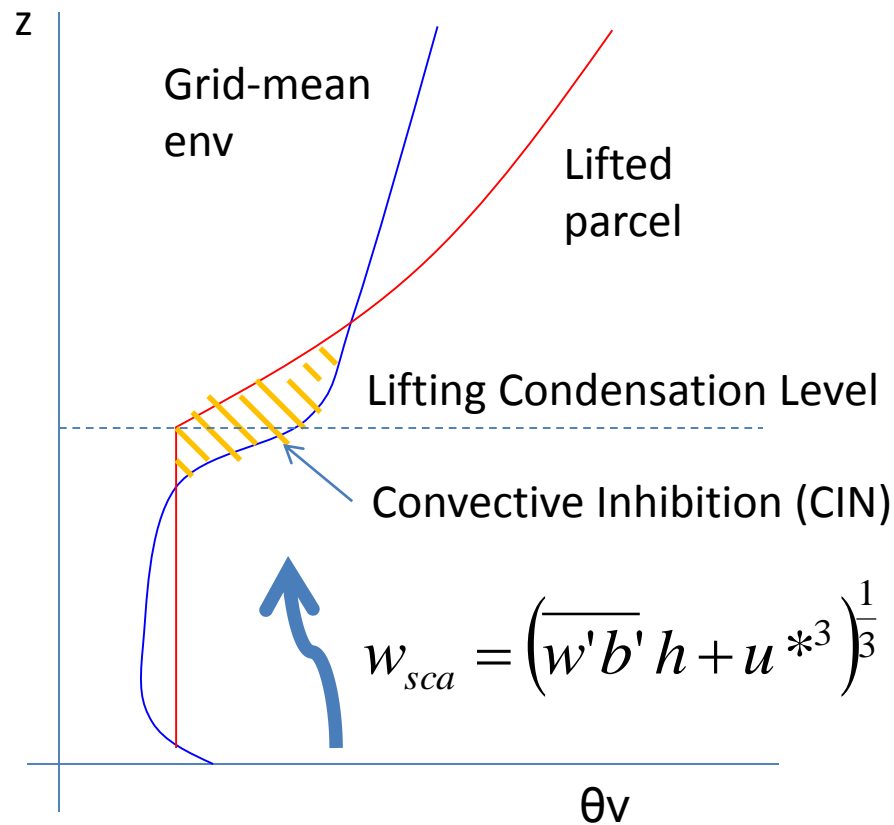
Need a rethink about how to effectively control the mass-flux, if we want to make it scale-aware and/or make variability more realistic.

Need to start from the triggering / cloud-model, not just the “closure”.



# Convective Diagnosis

To meaningfully force the mass-flux, need to force the threshold for convection triggering (average mass-flux is controlled by the CIN-based diagnosis)....



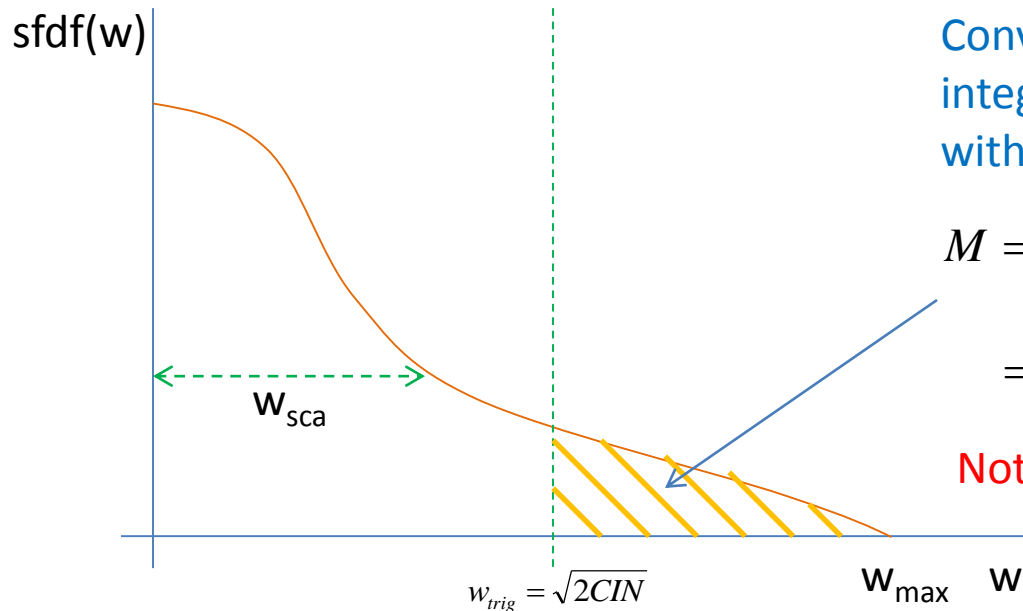
If  $KE < CIN$ , parcel top (where KE runs out) sets boundary-layer top height used to parameterise non-local turbulence.

If  $KE > CIN$ , parameterised non-local turbulence extends up to the LCL, with parameterised convection (shallow or deep) triggered from the LCL upwards.

Scale-awareness can be introduced by considering the sub-filter-scale distribution of  $w$ , and allowing the properties of that distribution to vary...

# PDF-based triggering & closure framework

Assume some distribution of  $w$  inside the sub-filter-scale updrafts below cloud-base (which may or may not trigger convection out of the boundary-layer):



Convection base mass-flux is  $\rho$  \* the integral over the part of the distribution with  $w$  large enough to overcome the CIN:

$$M = a_{ud} \rho \int_{w_{trig}}^{w_{max}} w \text{sdfd}(w) dw$$

$$= a_{ud} \rho f(w_{max}, w_{sca}, w_{trig}(CIN)) \quad (1)$$

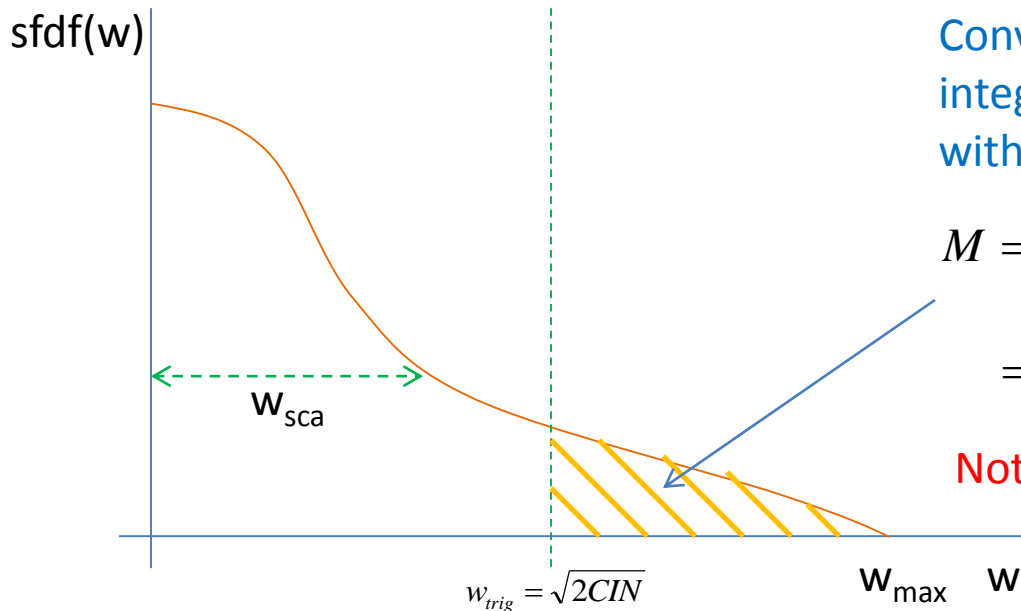
Note: if  $w_{max} \leq w_{trig}$  then  $M = f = 0$

Assume a functional form for the distribution, such that it can be described by 3 parameters:

- its maximum  $w_{max}$
- a shape parameter  $w_{sca}$
- the total BL updraft area  $a_{ud}$

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Convection base mass-flux is  $\rho$  \* the integral over the part of the distribution with  $w$  large enough to overcome the CIN:

$$M = a_{ud} \rho \int_{w_{trig}}^{w_{max}} w sfd f(w) dw$$

$$= a_{ud} \rho f(w_{max}, w_{sca}, w_{trig}(CIN)) \quad (1)$$

Note: if  $w_{max} \leq w_{trig}$  then  $M = f = 0$

Assume a functional form for the distribution, such that it can be described by 3 parameters:

- its maximum  $w_{max}$
- a shape parameter  $w_{sca}$
- the total BL updraft area  $a_{ud}$

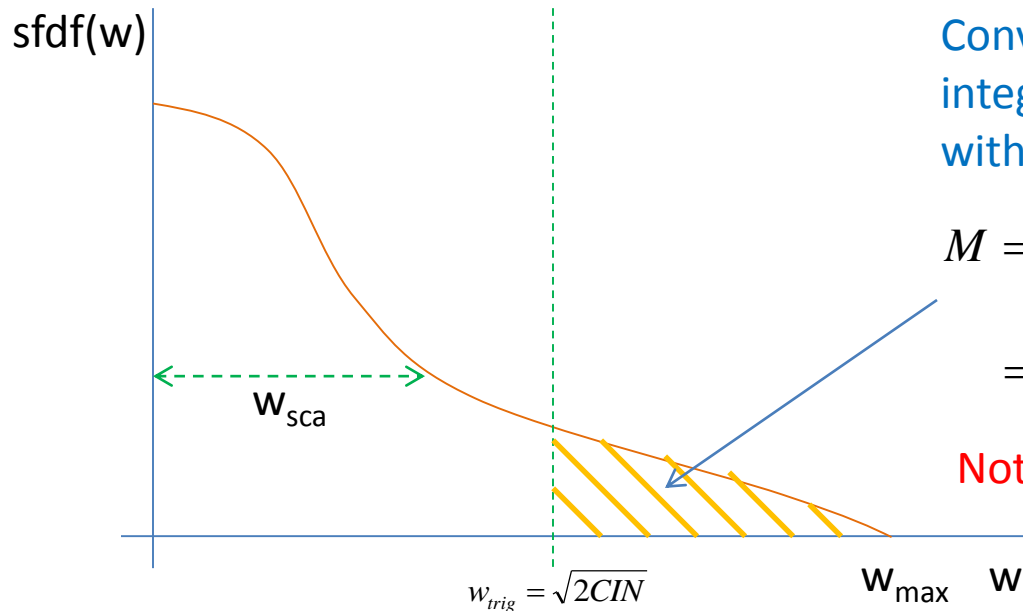
c.f. Validation of this type of closure by

Fletcher & Bretherton (2010):

Evaluating Boundary Layer–Based Mass Flux Closures Using Cloud-Resolving Model Simulations of Deep Convection. *JAS*. **67**, 2212.

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For a numerically robust solution, this closure needs to be solved implicitly w.r.t. CIN (convection and other forcings adjust the CIN on timescales  $\ll \Delta t$ ).

A scale-aware, stochastic approach to the triggering and closure can be found by considering the sampling distributions of the sub-filter distribution properties

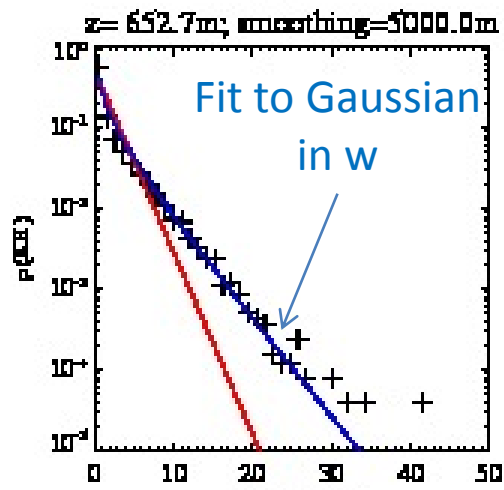
$w_{sca}, w_{max}, a_{ud} \dots$



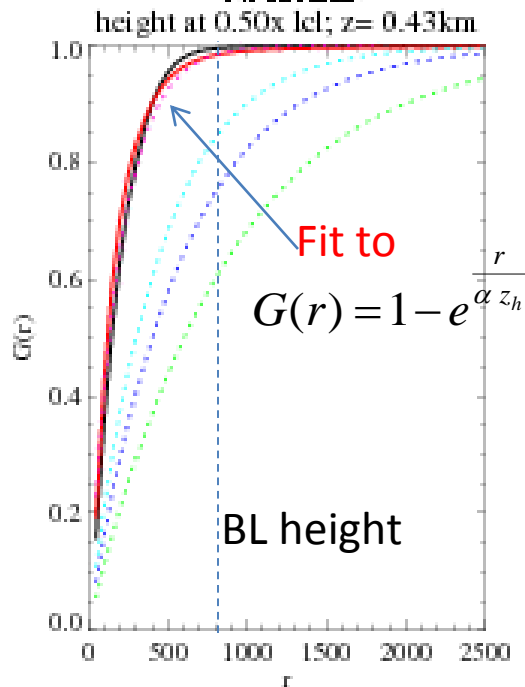
# Use LES to construct statistical model for sub-filter-scale $w$ distribution

Alison Stirling: LES of onset of deep convection, at 25m resolution.

PDF of BL  
updraft KE:



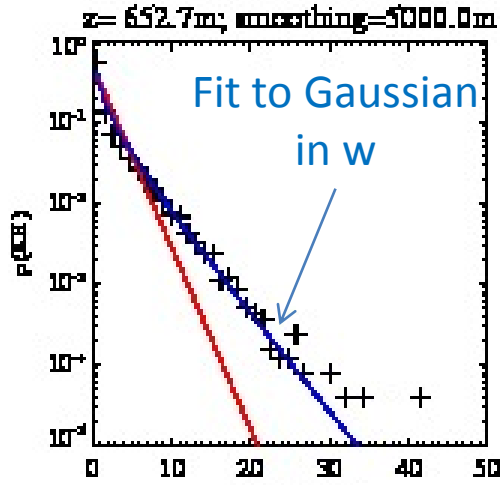
Apply Gaussian  
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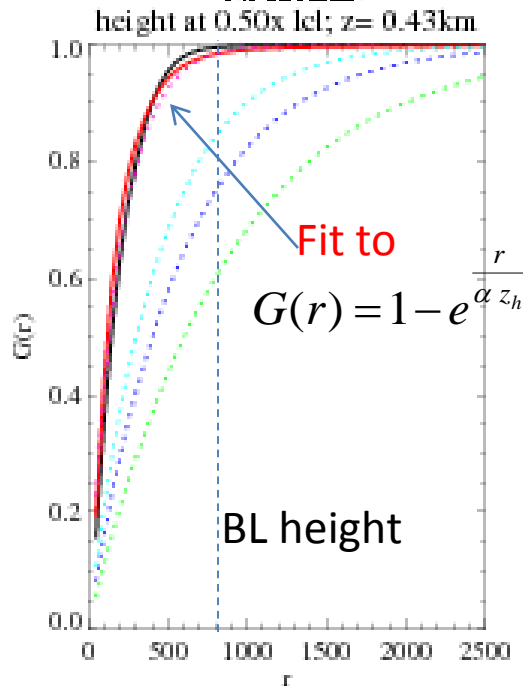
PDF of BL updraft KE:



Assume that at large-scale equilibrium:

$$w_{sca} = \left( \overline{w'b'} z_h + u_*^3 \right)^{\frac{1}{3}} \quad L = \alpha z_h \quad \tau = \frac{L}{w_{sca}}$$

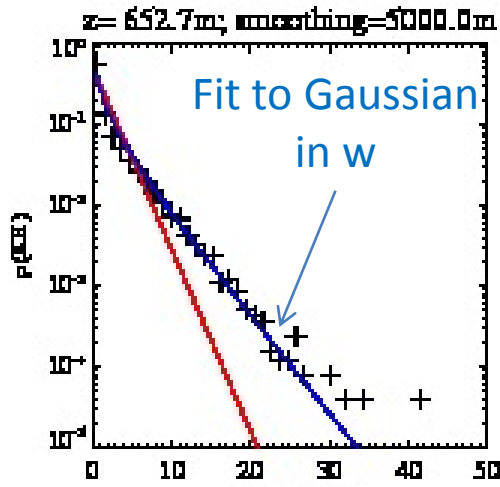
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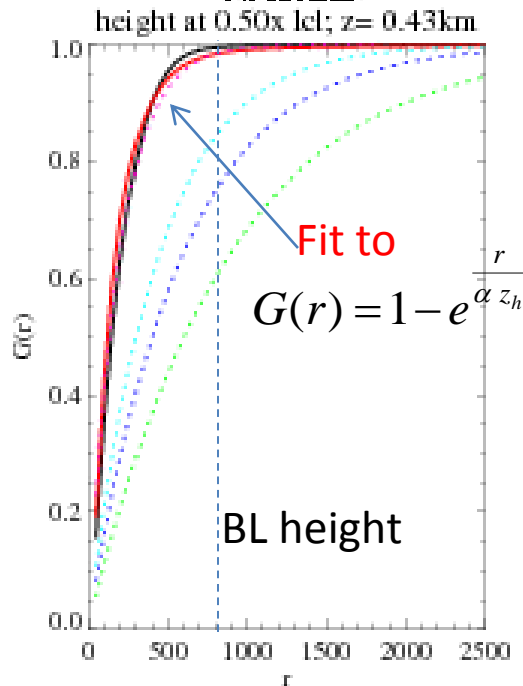
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Rescale these based fraction of TKE expected to be sub-filter-scale at the model's grid-length:

$$r \approx 4\Delta x$$

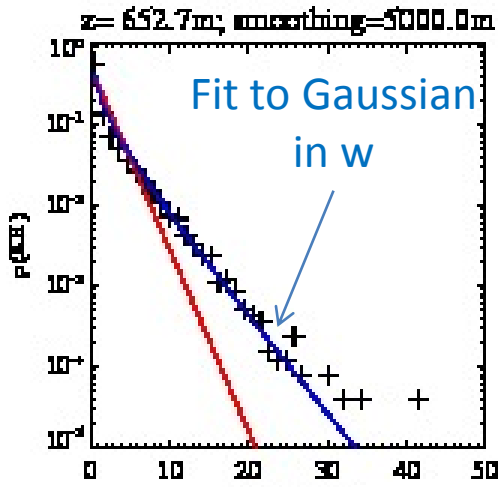
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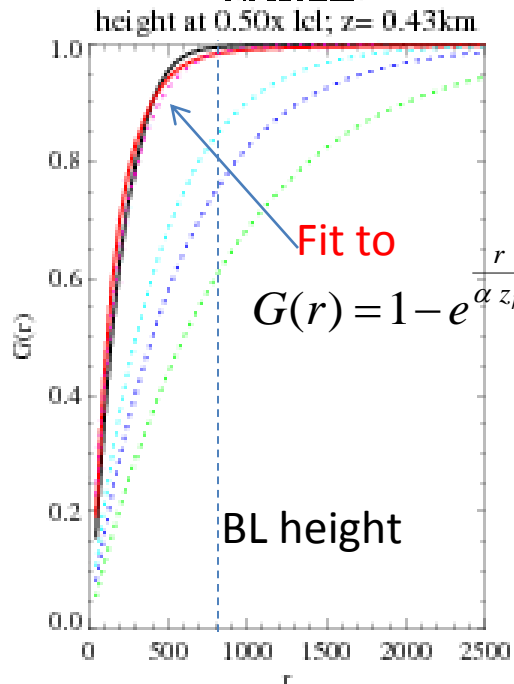
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$$n_{eqm} \approx \frac{1}{2} \frac{r^2}{L^2}$$

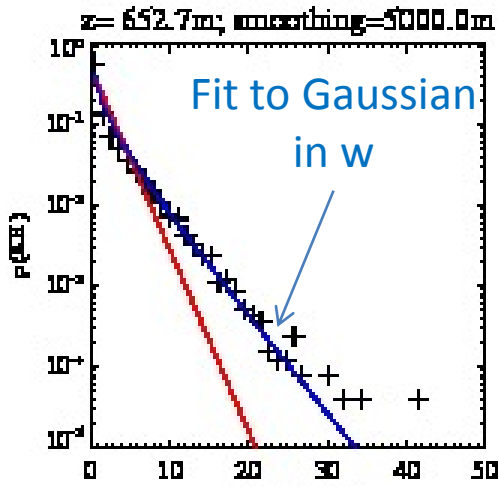
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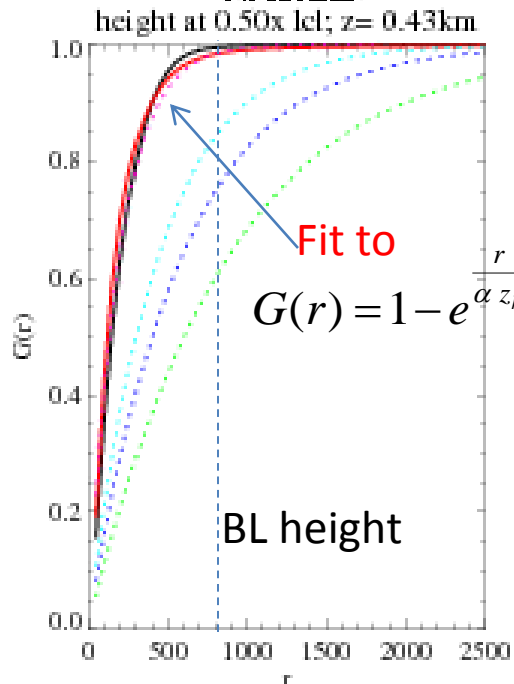
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BL updraft area scaled by Poisson distributed updraft number with this mean:

$$a_{ud} \approx \frac{1}{2} \frac{n_{Po}}{n_{eqm}}$$

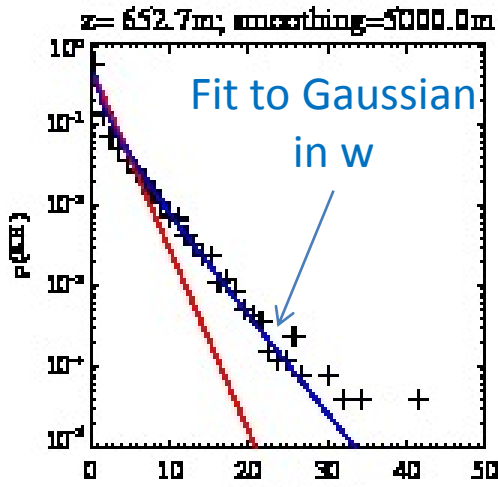
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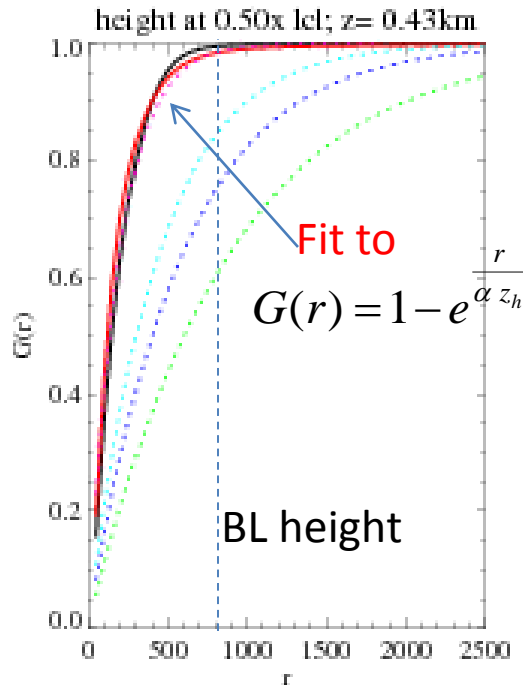
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BL updraft area scaled by Poisson distributed updraft number with this mean:

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Estimate sampling distributions for  $w_{sca}$ ,  $w_{max}$  using updraft number, and stochastically sample these...

# Scale-aware, stochastically-varying sub-filter-scale distribution

$$M = a_{ud}\rho \int_{w_{trig}}^{w_{max}} w s f d f (w) dw$$

Fine grid-resolution

Few BL updrafts per grid-cell

Many grid-cells don't trigger

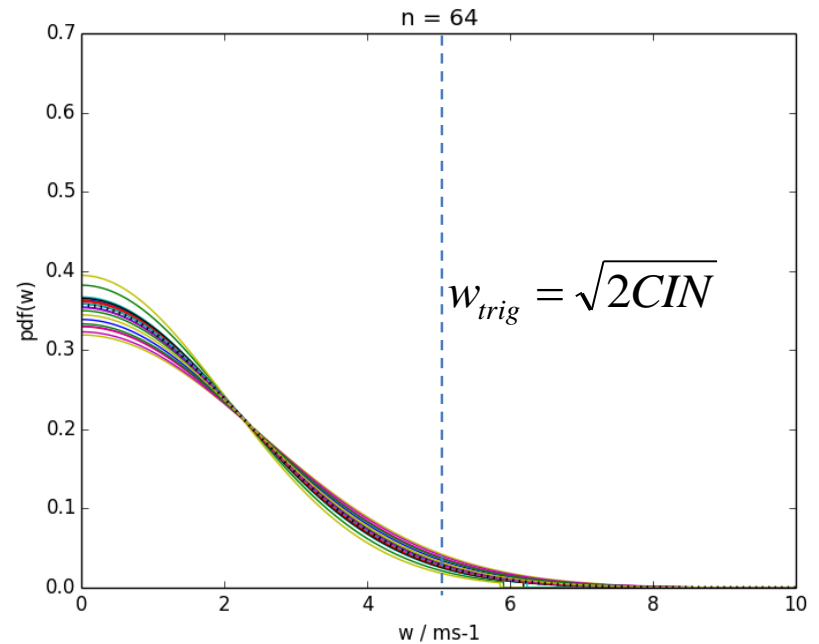
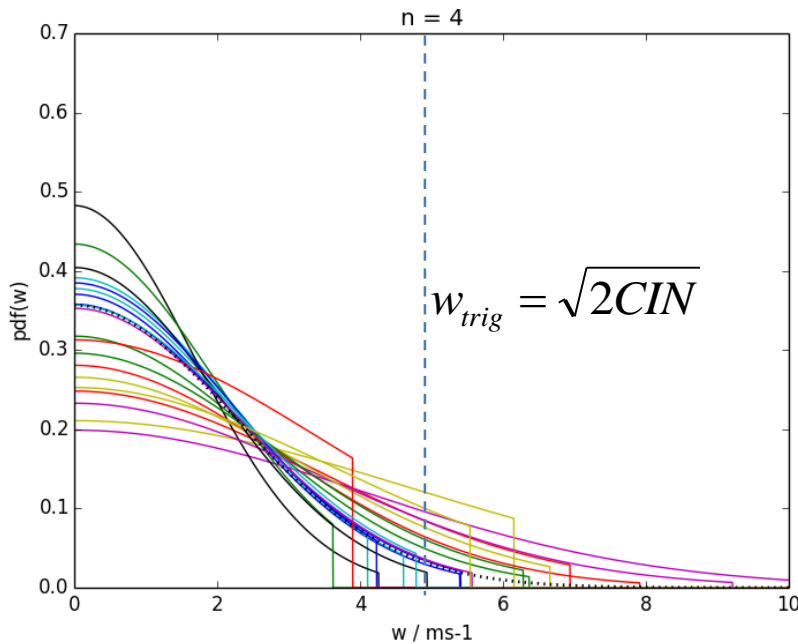
Large mass-flux in a few grid-cells

Coarse grid-resolution

Many BL updrafts per grid-cell

All grid-cells trigger

Small mass-flux in each grid-cell



In practice, most of the scale-awareness comes from the sampling distribution for  $w_{max}$ ;

A larger number of BL updrafts per filter-scale area increases the probability of having one or two exceptionally intense updrafts, which trigger convection.

Note: in the scheme, the random sampling is autocorrelated in time and space...

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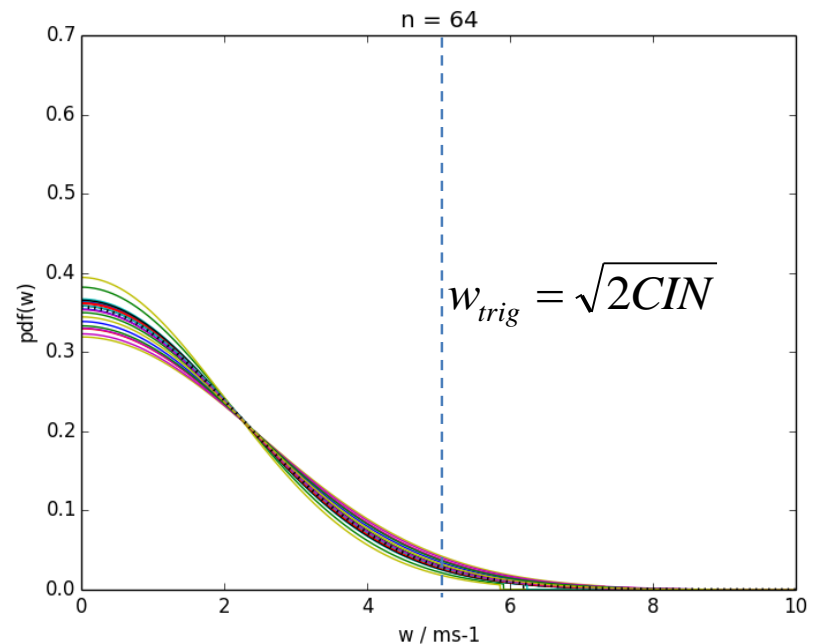
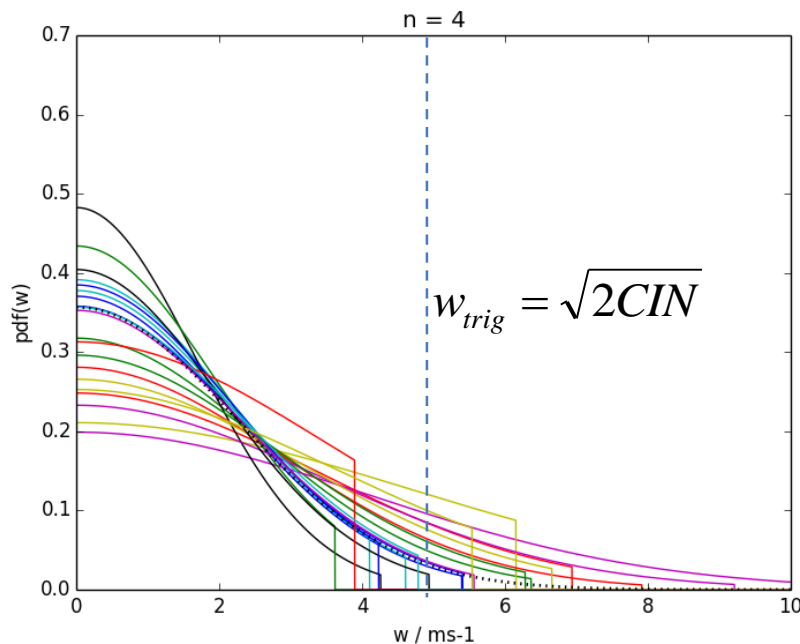
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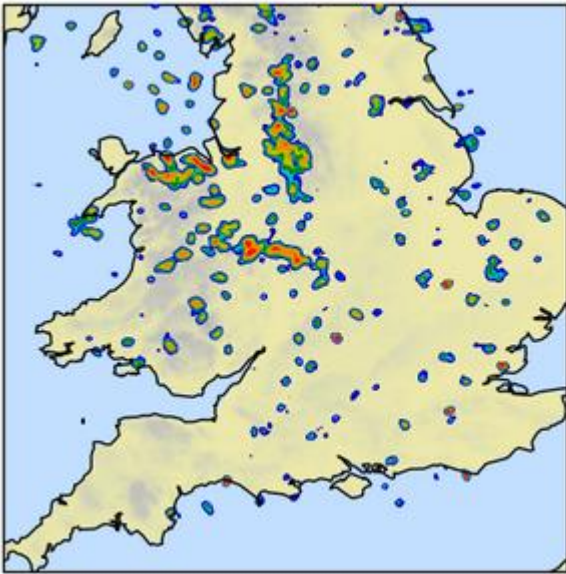
Entrainment rate: depends on  $1/L$

$L$  is sub-filter-scale updraft horizontal size; adapts with resolution (smaller  $\Delta x$  means any updrafts which are sub-filter-scale must be smaller, so have higher entrainment rates).

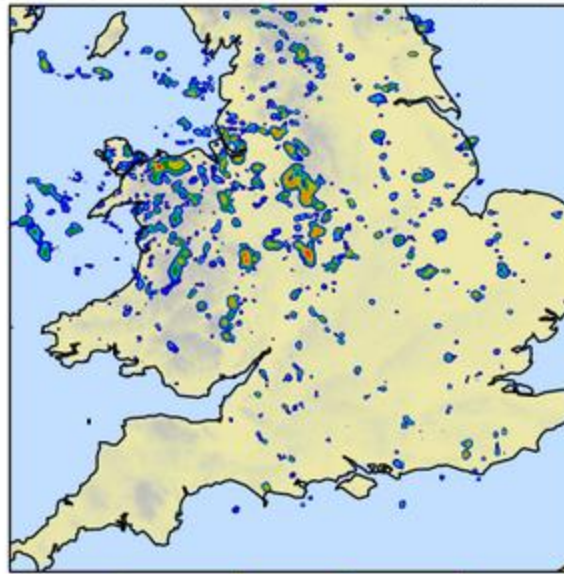
Also use ad-hoc “convective memory” to modulate entrainment and  $w$ -distribution properties as a function of recent convective precipitation.



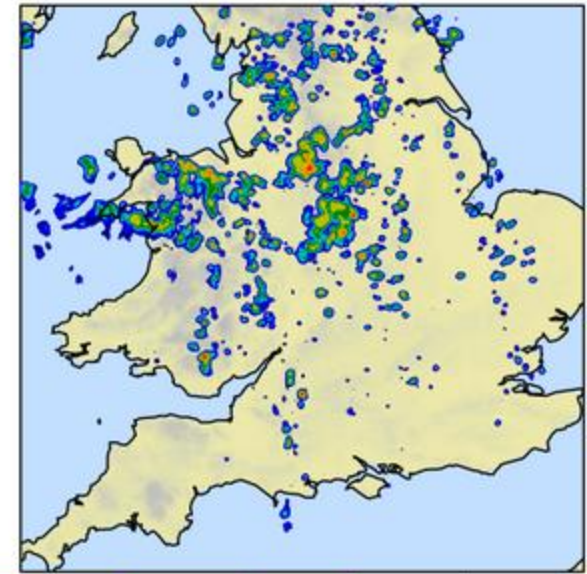
UKV2 PS38 (LS)



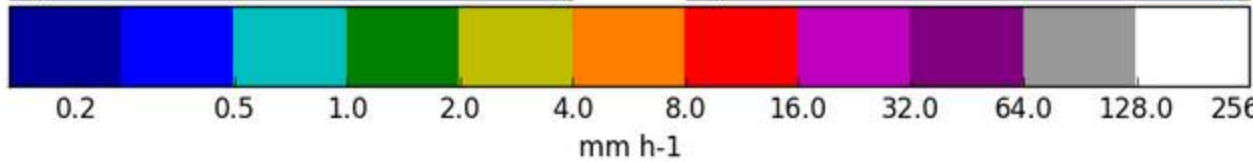
UKV2 PS38 + convection scheme (LS + conv)



Radar



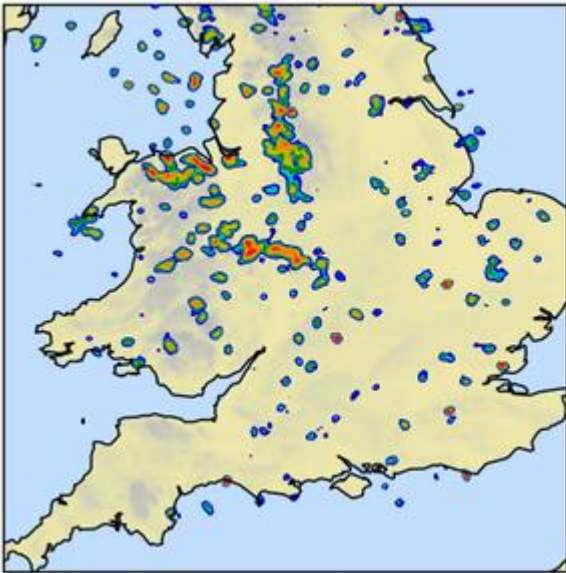
UKV tests and analysis by  
Kirsty Hanley



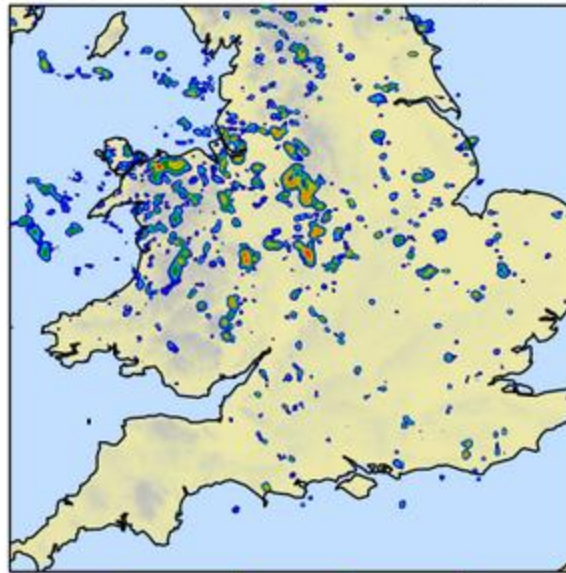
### UKV 1.5 km forecast

Improved representation of  
sporadic small showers /  
lighter rain-rates from  
parameterised convection.

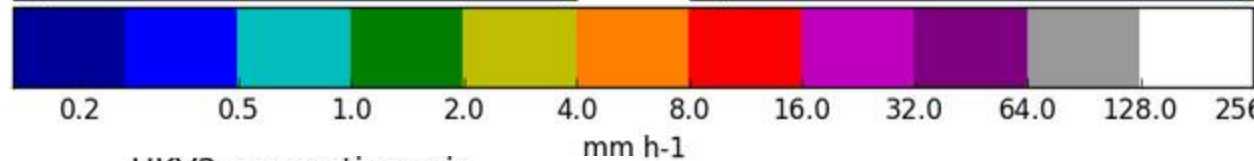
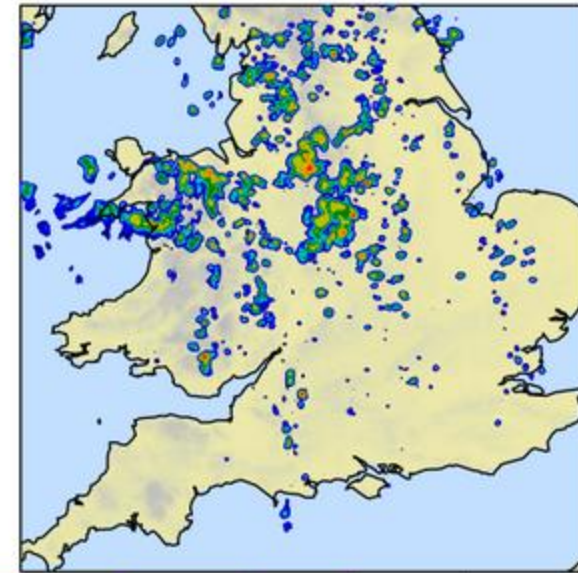
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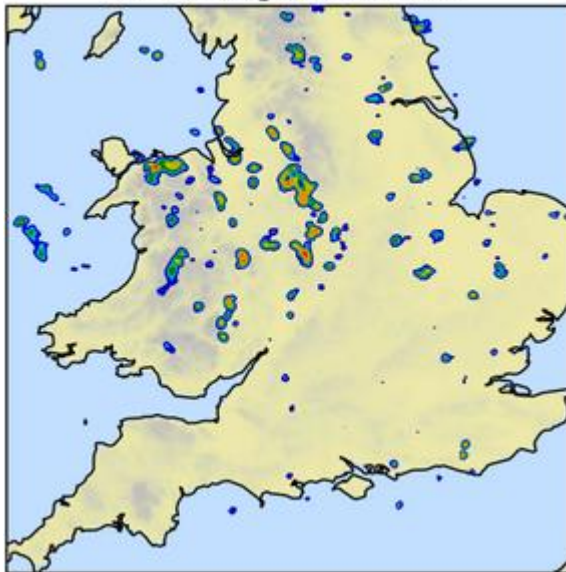
UKV2 PS38 + convection scheme (LS + conv)



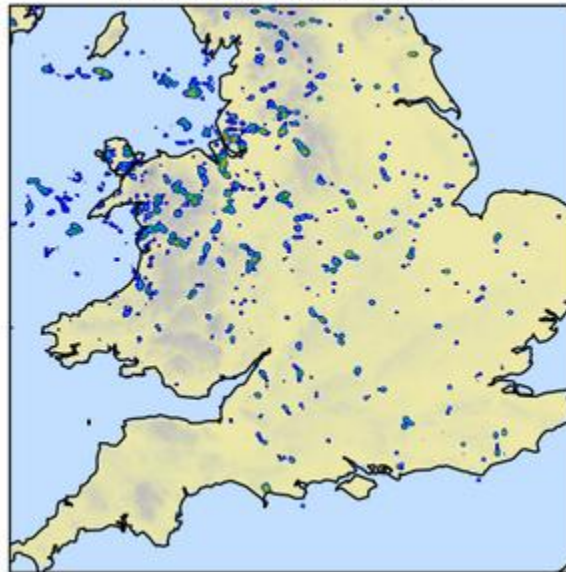
Radar



UKV2 large-scale rain



UKV2 convective rain



## UKV 1.5 km forecast

Improved representation of sporadic small showers / lighter rain-rates from parameterised convection.

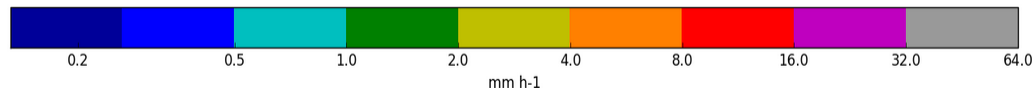
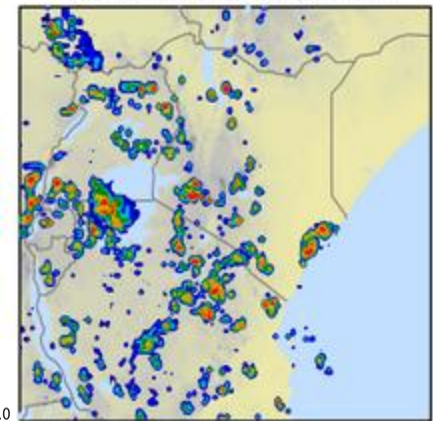
Larger, heavier showers still resolved.



## E Africa convection-permitting model.

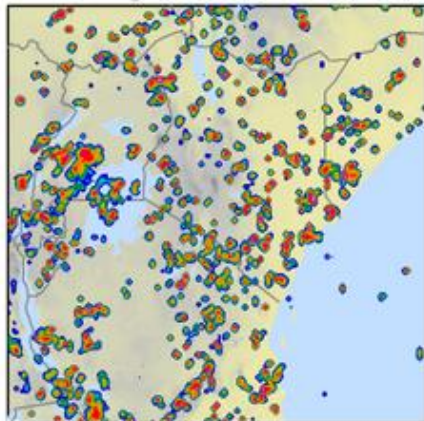
Model has too many small showers, and stochastic convection makes this worse...

Observations (GPM)

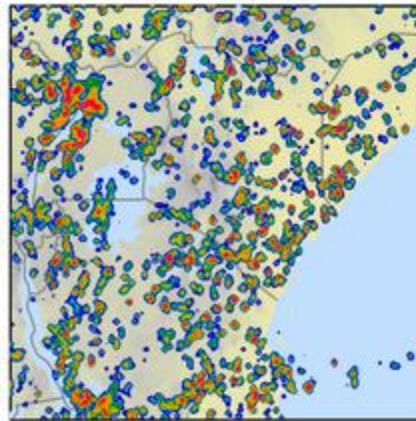


E Africa model tests and analysis by Kirsty Hanley

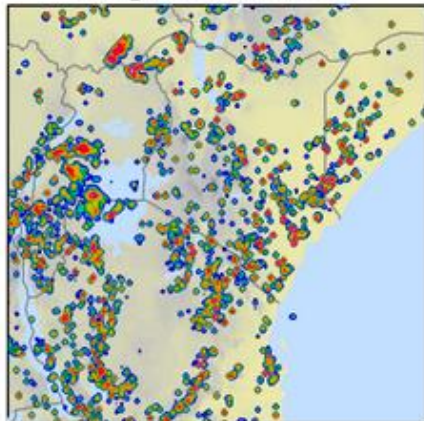
SingV 3.1 (4.4km)



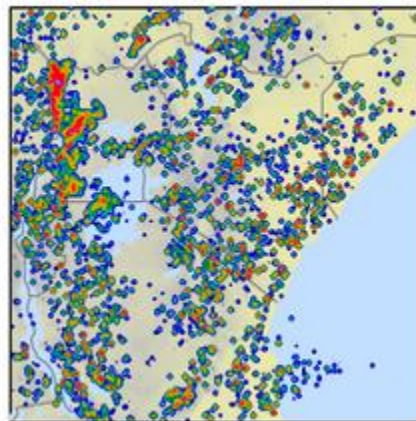
4.4km LS + conv



SingV 3.1 (1.5km)



1.5km LS + conv

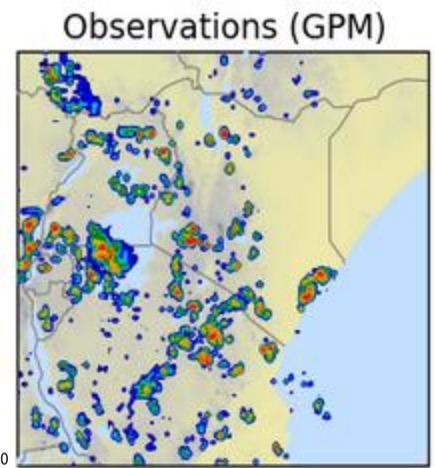
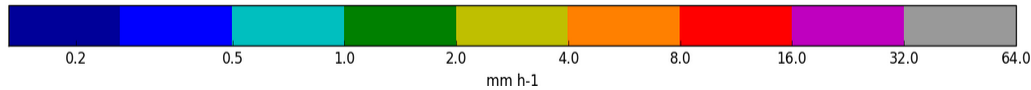




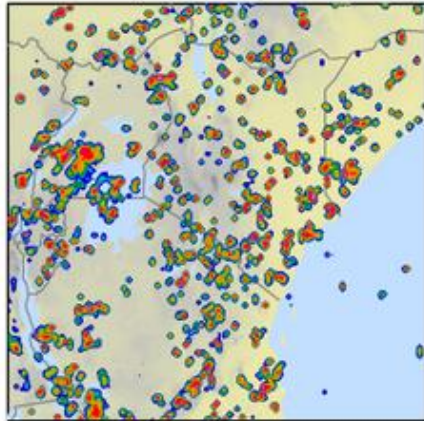
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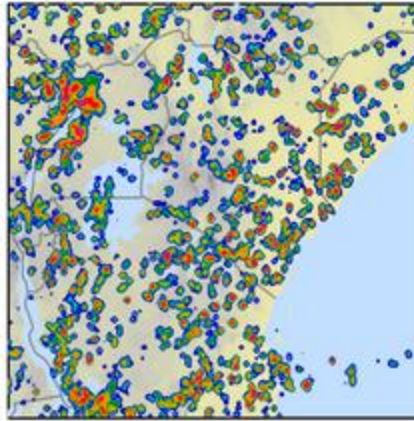
At higher resolution, parameterised rain gets lighter, resolved rain gets heavier, as expected.



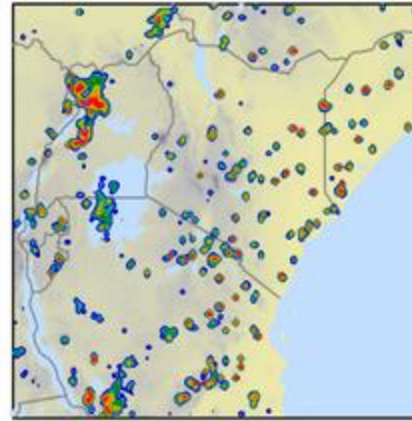
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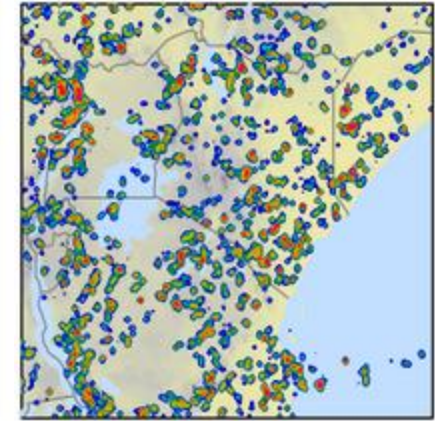
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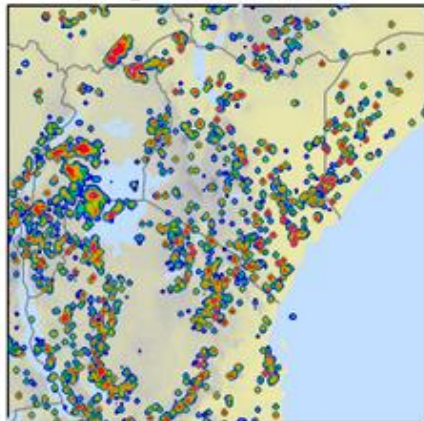
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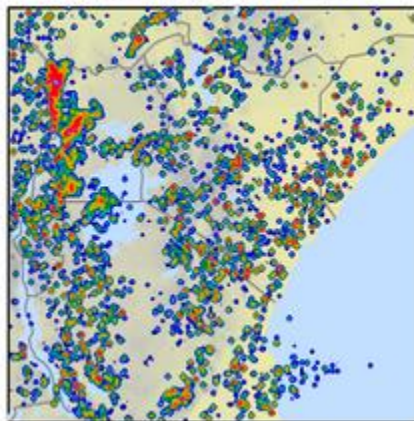
4.4km conv



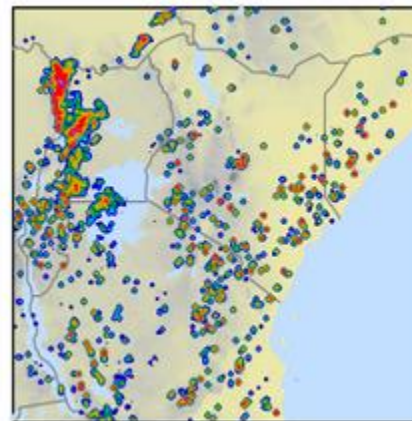
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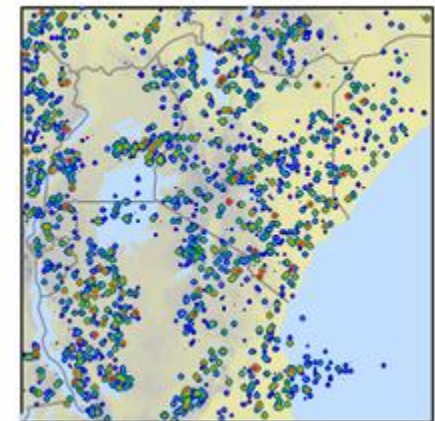
1.5km LS + conv



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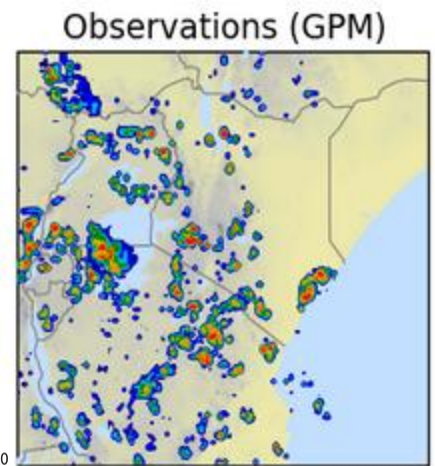
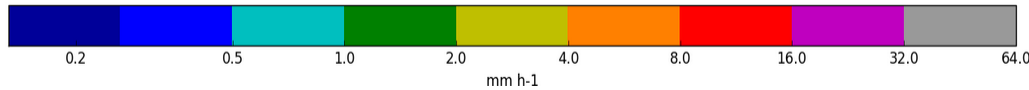




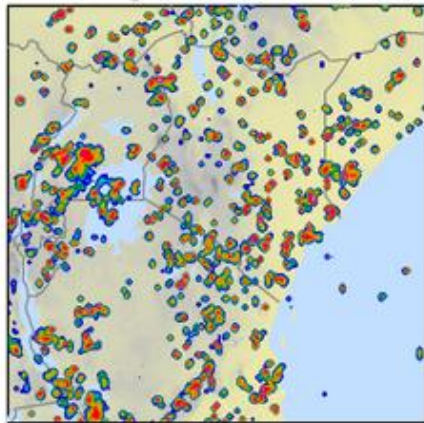
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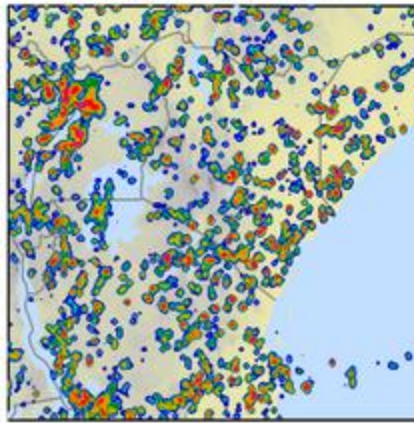
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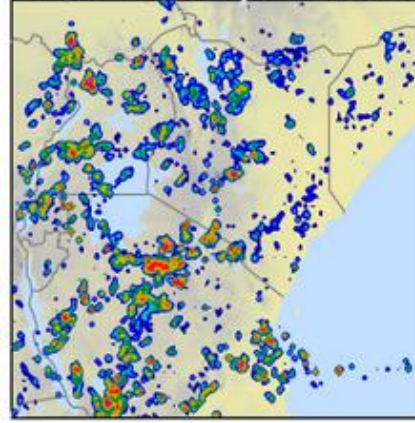
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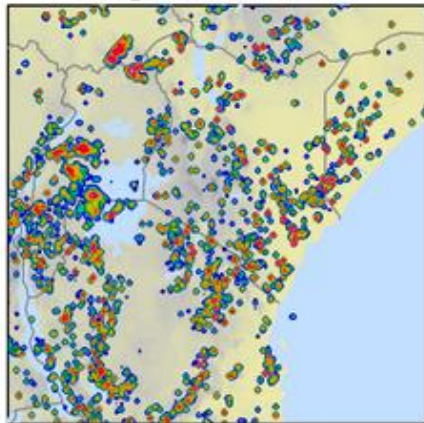
4.4km LS + conv



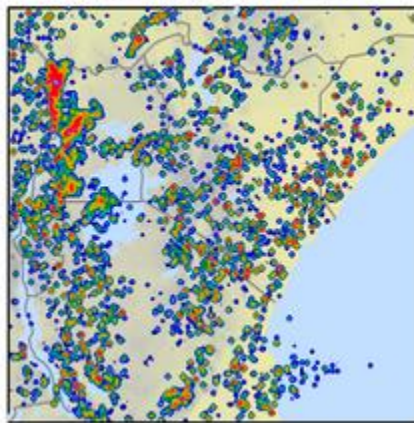
no perturbations (4.4km)



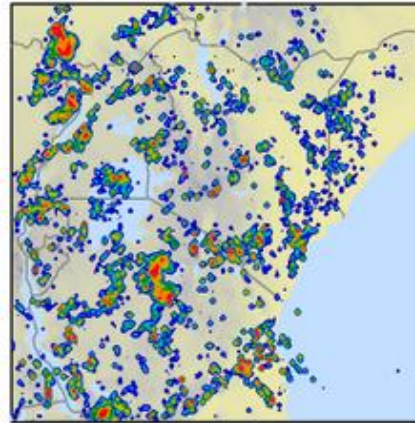
SingV 3.1 (1.5km)



1.5km LS + conv

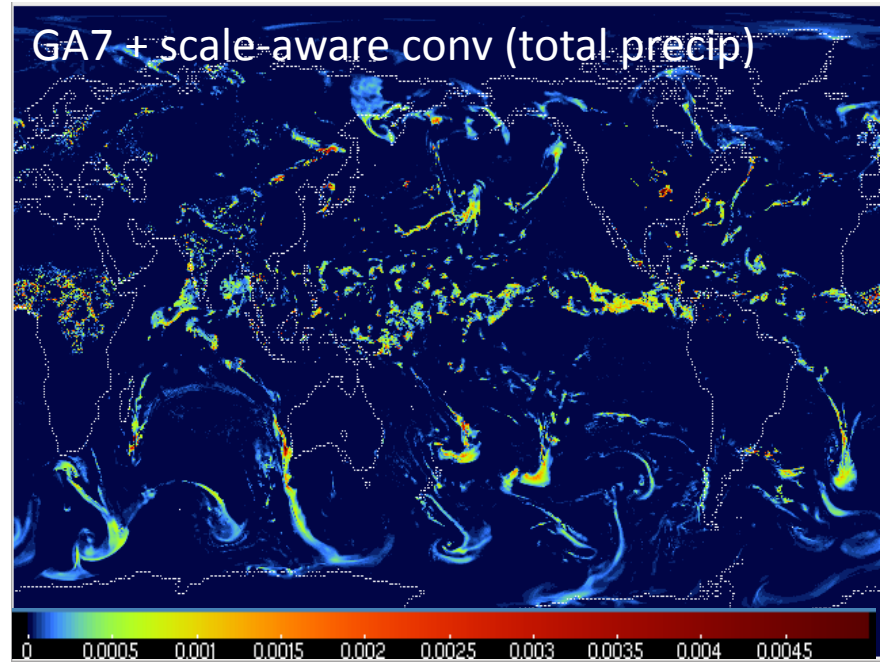
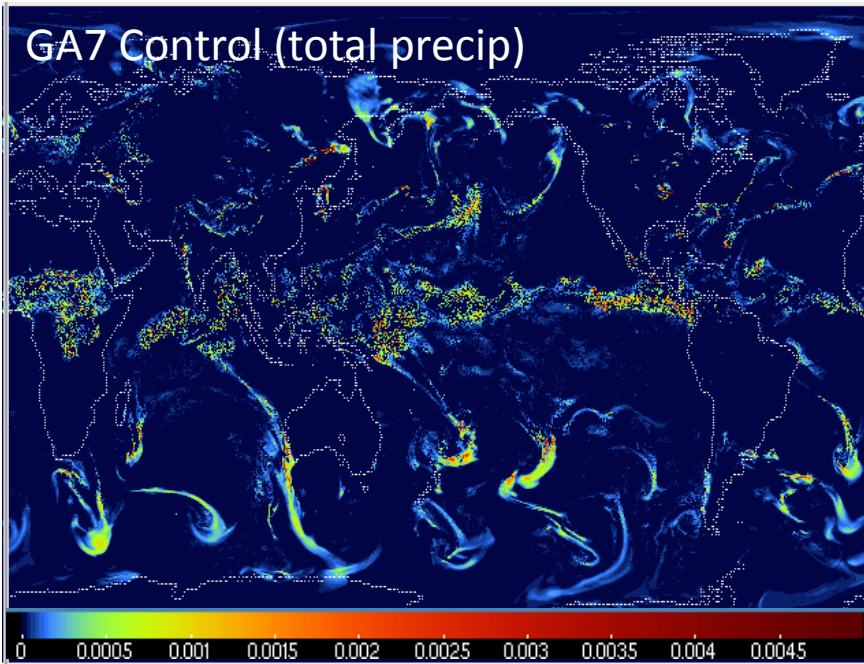


no perturbations (1.5km)



Control run already has stochastic BL perturbations.

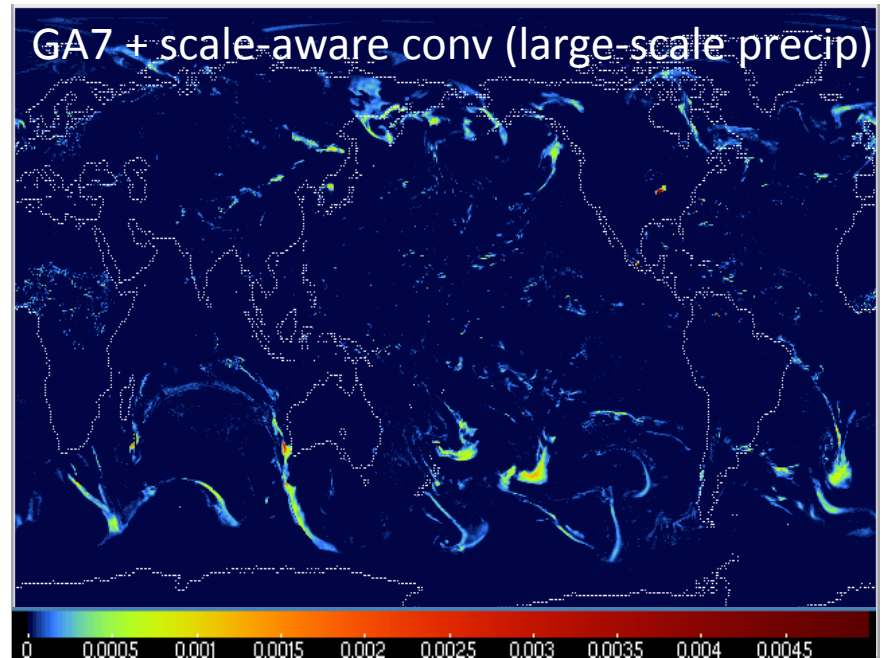
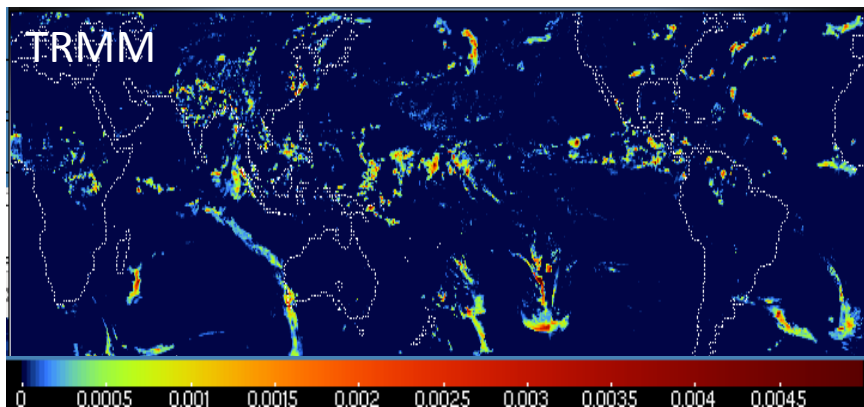
Adding stochastic convection but turning off BL perturbations, organisation is improved.



**N320 global NWP run (5-day lead-time).**

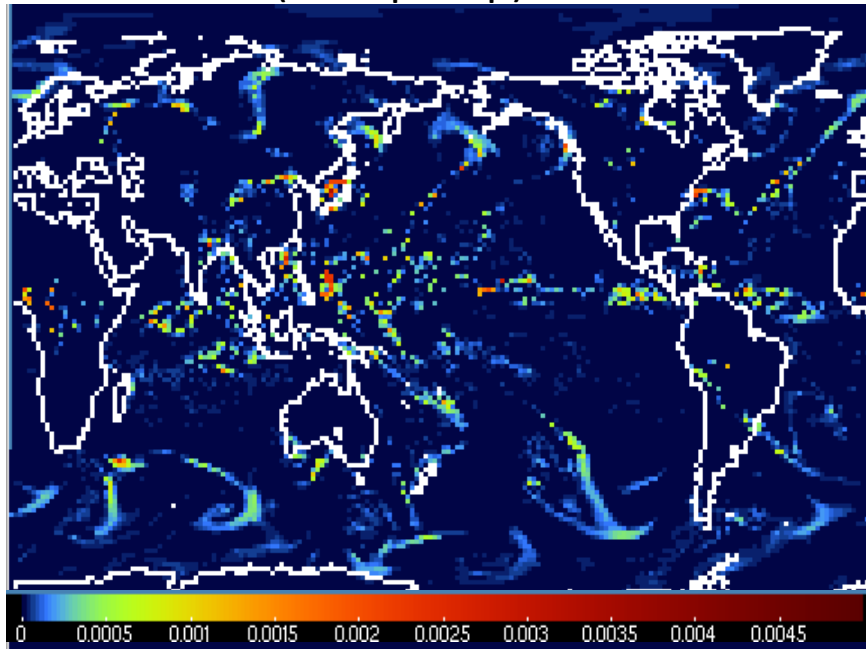
Convection scheme does nearly all the Tropical rainfall, as expected.

“Convective memory” used in new scheme makes rainfall more organised and persistent.

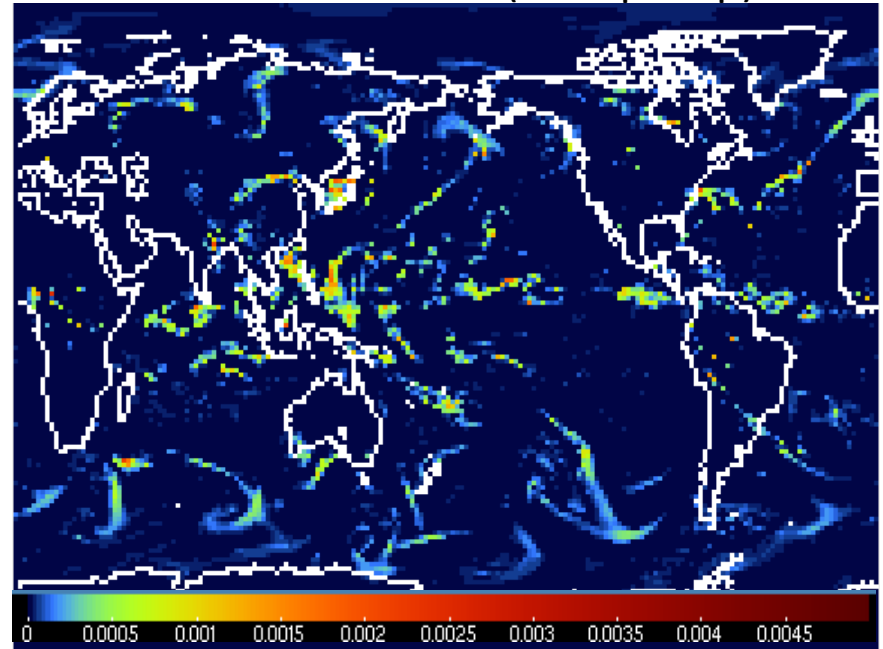




GA7 Control (total precip)



GA7 + scale-aware conv (total precip)



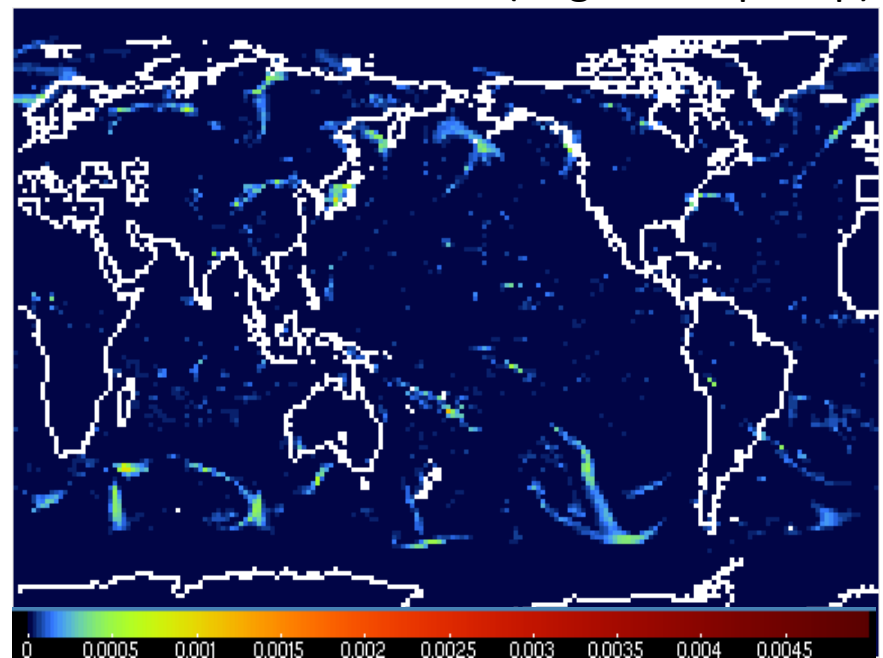
### N96 climate-AMIP-style run.

Again, KE PDF vs CIN triggering / closure removes intermittency, while “convective memory” increases organisation.

Effect of scale-aware scheme at N96 similar to effect at N320, but difference looks less pronounced.

Because model resolution is closer to equilibrium scale?

GA7 + scale-aware conv (large-scale precip)



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    - \* Dissipation / dilution of source parcels below cloud-base (c.f. Rio *et al.* 2013 found this was important).
    - \* Radiative effects of the diagnosed cumulus updrafts (GCM includes some, but cloud fractions for non-precipitating cumulus in a dry environment are much too small).
- Correcting this should slow down surface-heating, improving the diurnal cycle.

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Correcting this should slow down surface-heating, improving the diurnal cycle.
- Other familiar “parameterised convection” biases from the global model appear in the LAMs (e.g. spurious rain along coastal sea points).

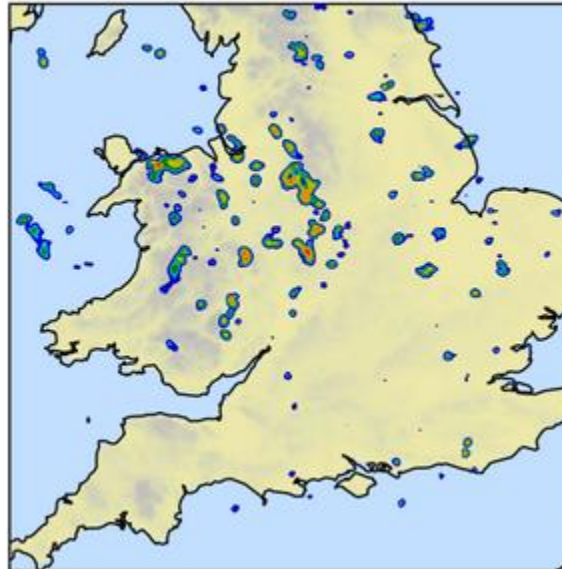
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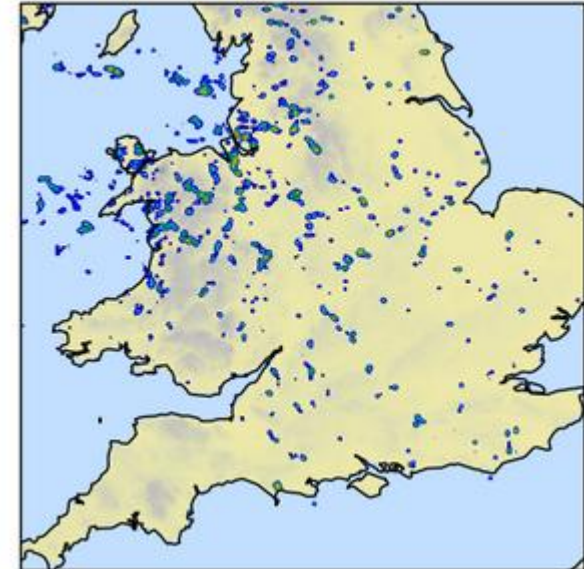
- Convective initiation too widespread / too early over Tropical land. Missing processes:
  - \* Dissipation / dilution of source parcels below cloud-base (c.f. Rio *et al.* 2013 found this was important).
  - \* Radiative effects of the diagnosed cumulus updrafts (GCM includes some, but cloud fractions for non-precipitating cumulus in a dry environment are much too small).Correcting this should slow down surface-heating, improving the diurnal cycle.
- Other familiar “parameterised convection” biases from the global model appear in the LAMs (e.g. spurious rain along coastal sea points).

- Spurious spatial separation between parameterised and resolved showers (parameterisation should add unresolved cores within resolved cloud-systems, but fails to do this).  
c.f. Problems with the UM “convective diagnosis” logic...

UKV2 large-scale rain



UKV2 convective rain



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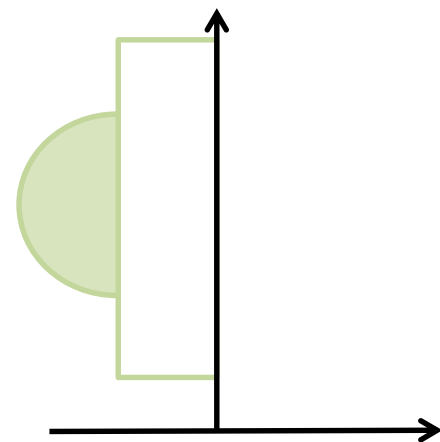
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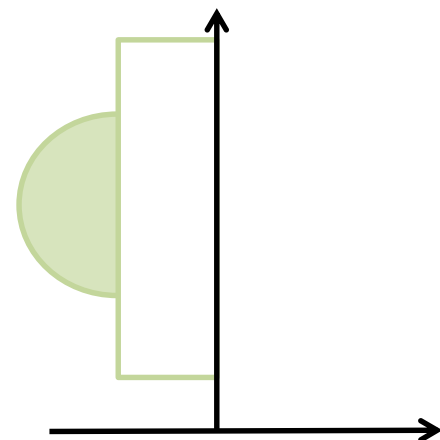
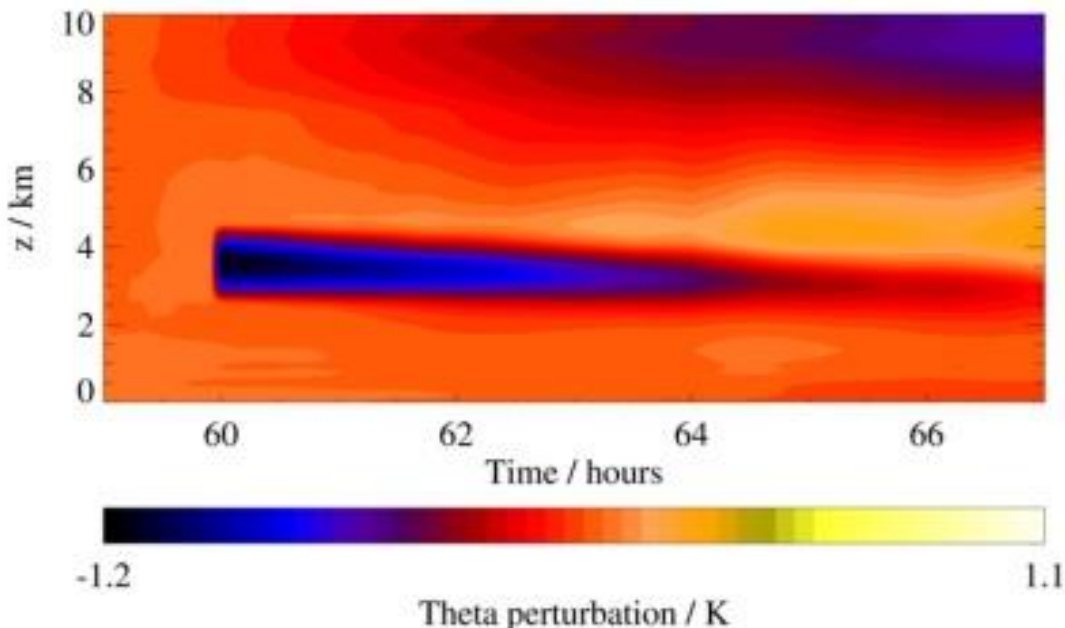
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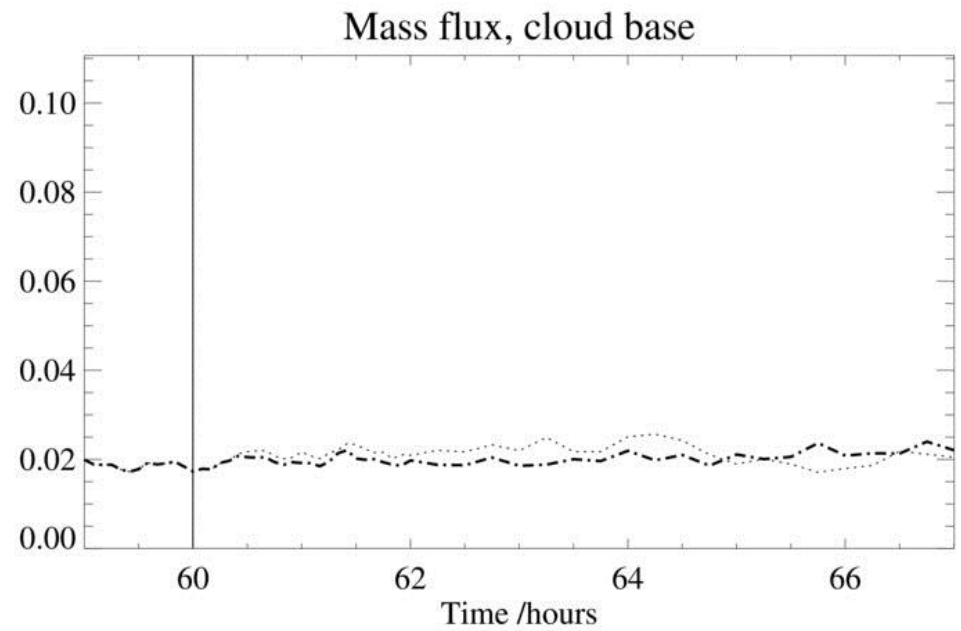
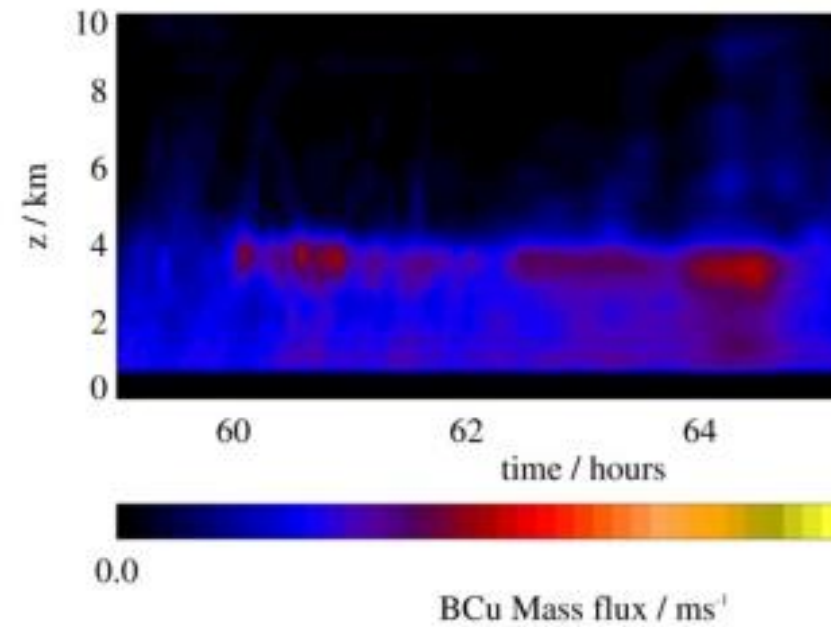
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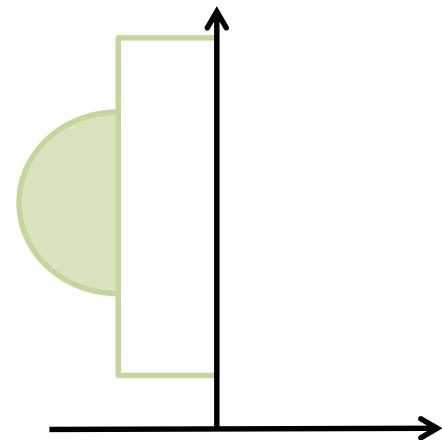
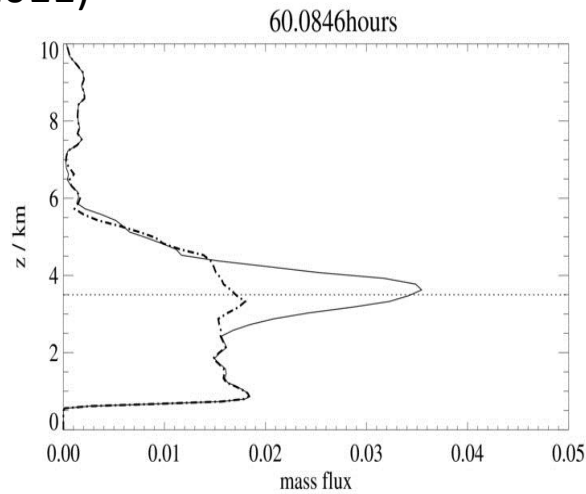
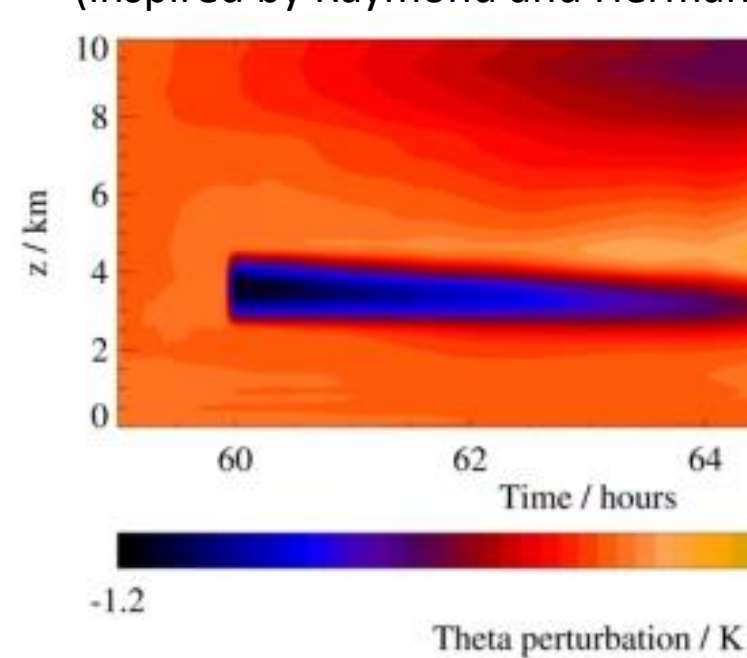
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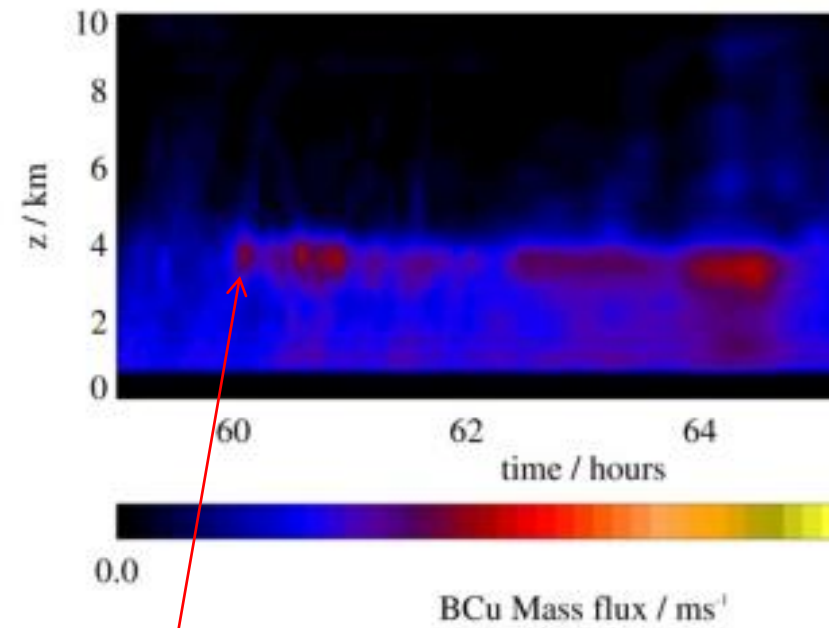
Alison Stirling; LES RCE with “jump-forcing” to free-troposphere CAPE (inspired by Raymond and Herman 2011)



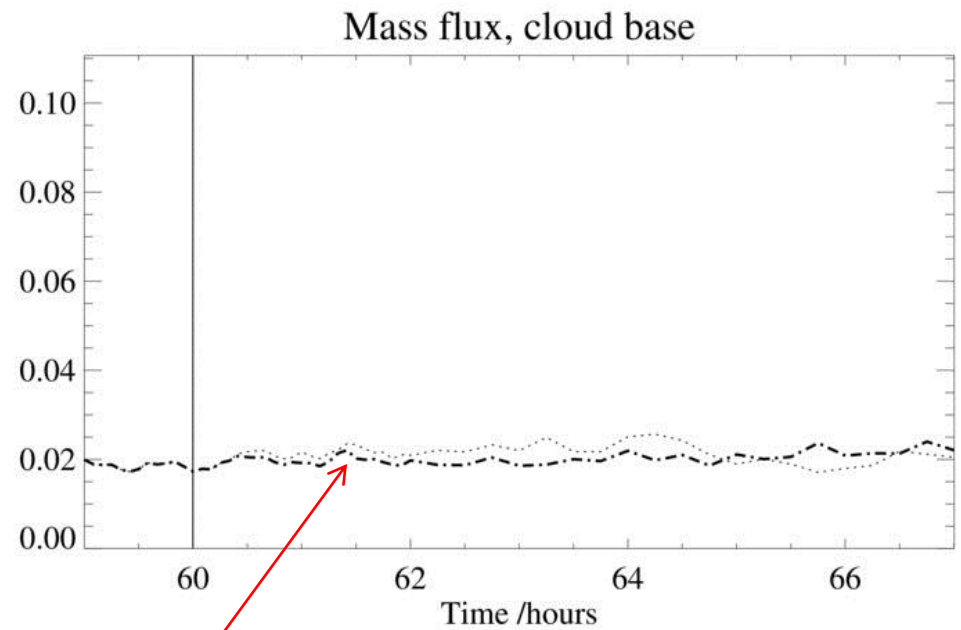


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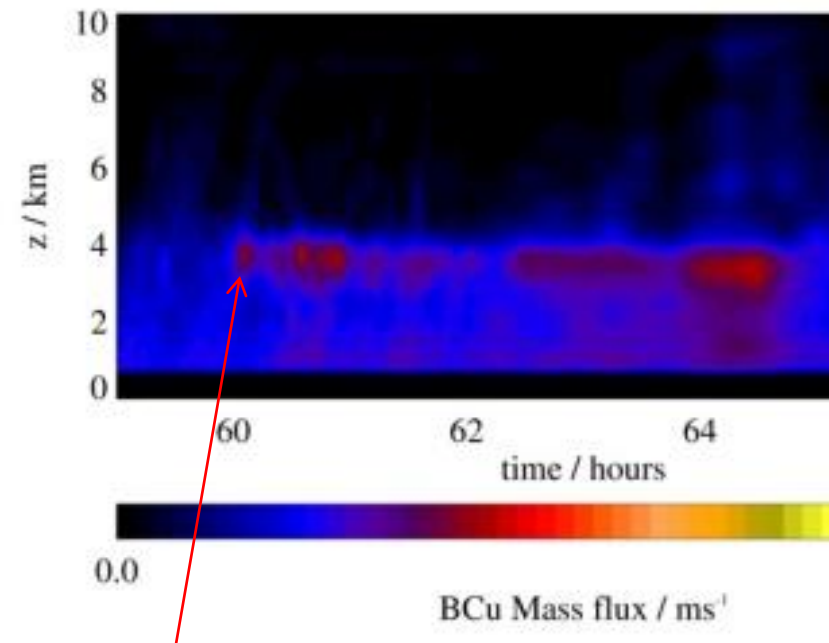




Immediate large increase in mass-flux in the layer destabilised by the forcing (from increase in updraft area fraction, not just  $w$ ).



Only modest increase in mass-flux at cloud-base, and only  $\sim$ hours after the forcing is applied.  
 (seems to be related to cold-pools driven by increased rainfall produced aloft).



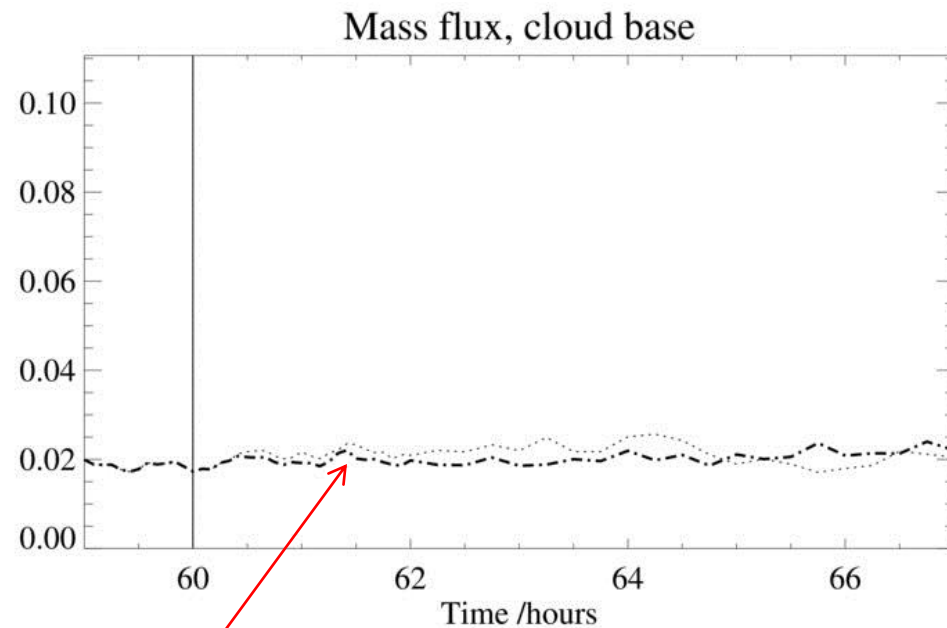
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Implications:

Increased buoyancy of convective updrafts in the free-troposphere increases the mass-flux primarily through lateral entrainment, *not* the cloud-base mass-flux.

**Vertically-integrated (CAPE) closure philosophy is not justified.**

Sensitivity of mass-flux to CAPE is via a process normally in a convection scheme's cloud-model. Again; "closure" and "cloud-model" are not really separable.



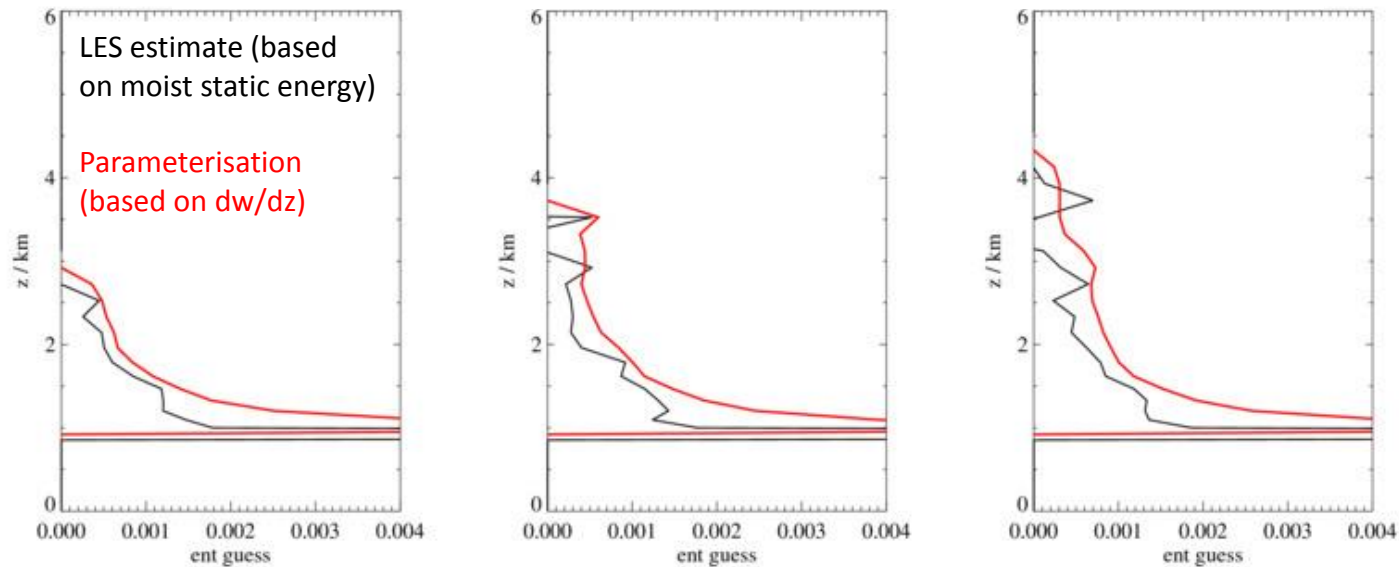
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# Adapting Entrainment

Control of the mass-flux via cloud-base by CIN / triggering / intermittency alone means it lacks sensitivity to tropospheric forcing.

We can address this by making entrainment depend on vertical acceleration of the updraft by buoyancy.

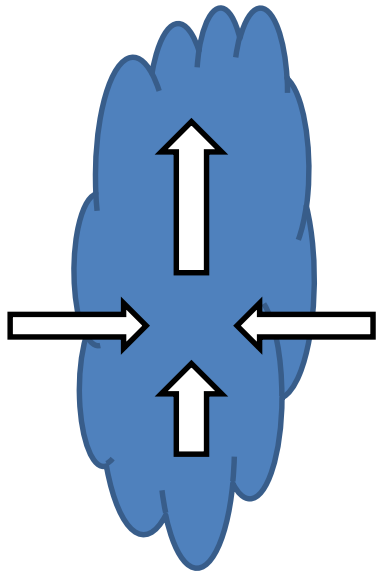
## Analysis of entrainment in LES: Alison Stirling



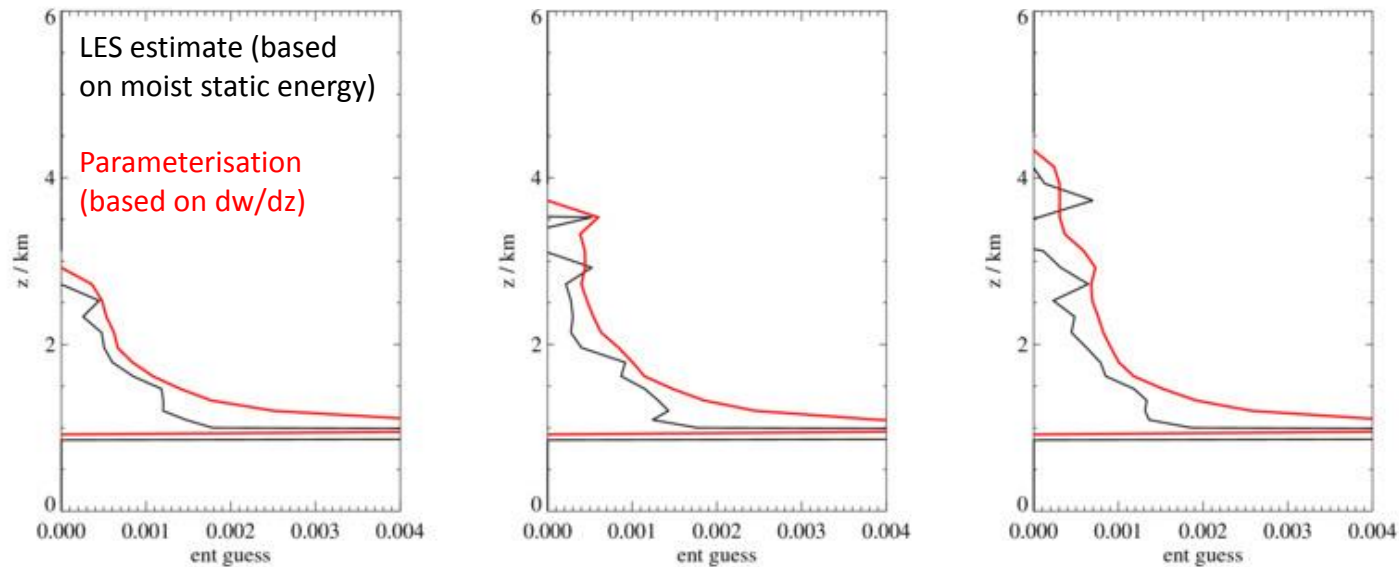
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Hypothesis: where convective updrafts accelerate, they try to preserve fractional area instead of contracting with height. From continuity, this means they must entrain laterally:

$$M = \rho \sigma w \quad \frac{\partial \sigma}{\partial z} = 0 \quad \Rightarrow \quad \varepsilon = \frac{1}{M} \frac{\partial M}{\partial z} = \frac{1}{\rho w} \frac{\partial \rho w}{\partial z}$$



# A new convection scheme - CoMorph

Updraft dynamics:

Entrainment based on a combination of mixing (scales with  $1/r$ ) and lateral convergence forced by vertical acceleration of the updraft ( $1/w dw/dz$ ).

Vertical velocity equation;  $w$  modified by buoyancy, entrainment, and drag. Drag depends on updraft radius  $r$  and environment static stability  $N^2$ .

Rain-out of precipitation depends on updraft vertical velocity (faster updrafts shed less water).

Acceleration of updrafts leads to higher entrainment and higher water-loading, which reduce the acceleration; this naturally regulates the updraft velocities.

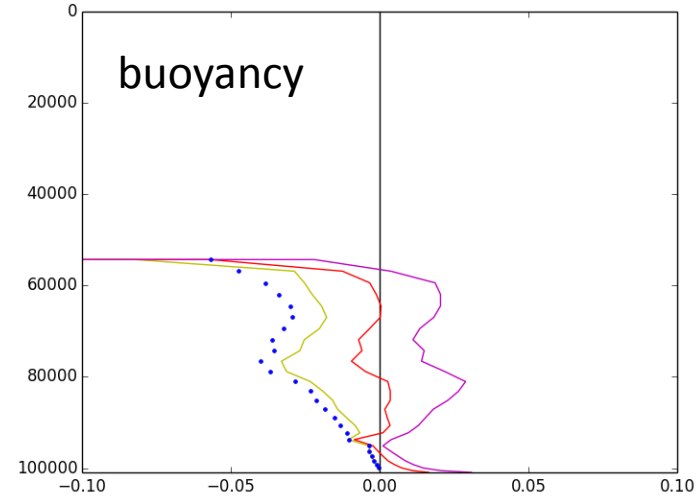
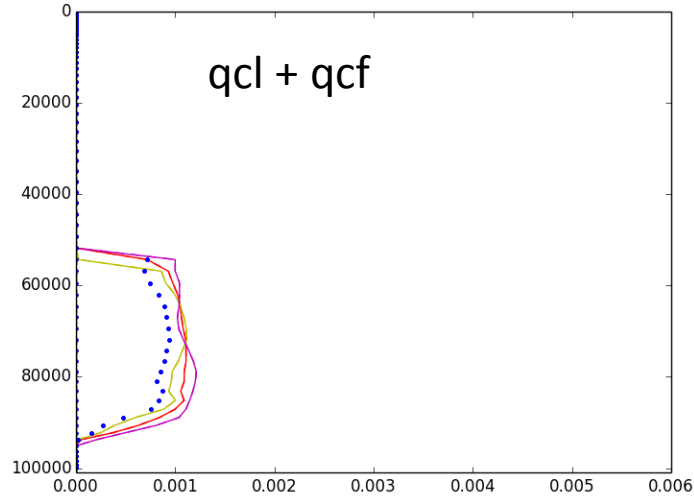
Convective Momentum Transport:  $u, v$  transported in the plume, with parameterised drag force between updraft and environment.

Other features

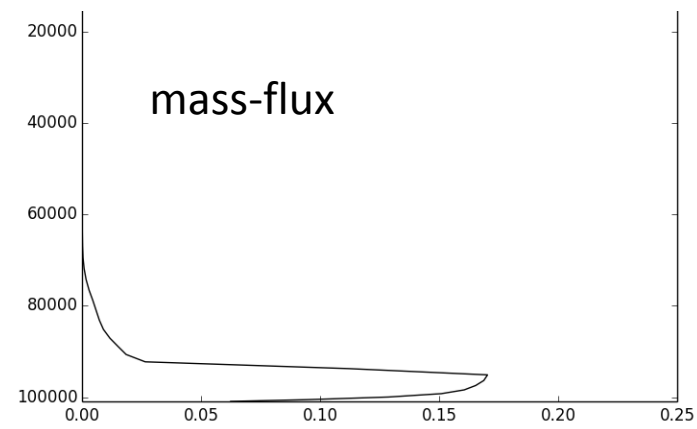
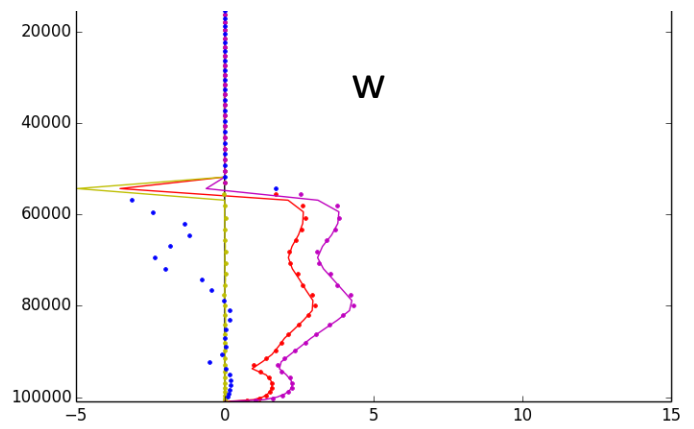
Option for convection to interact directly with microphysics prognostics (e.g precip output directly to prognostic rain and graupel fields).

Formulated in mixing ratios, with flexibility to modify thermodynamics assumptions consistently in all parts of the scheme (eg under future work on conservation).

New scheme can be made to behave like shallow, congestus, deep just by varying the updraft radius...



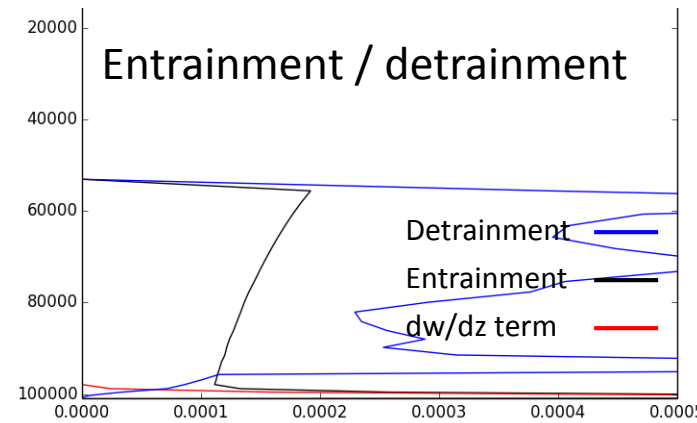
- Updraft core
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- Updraft edge



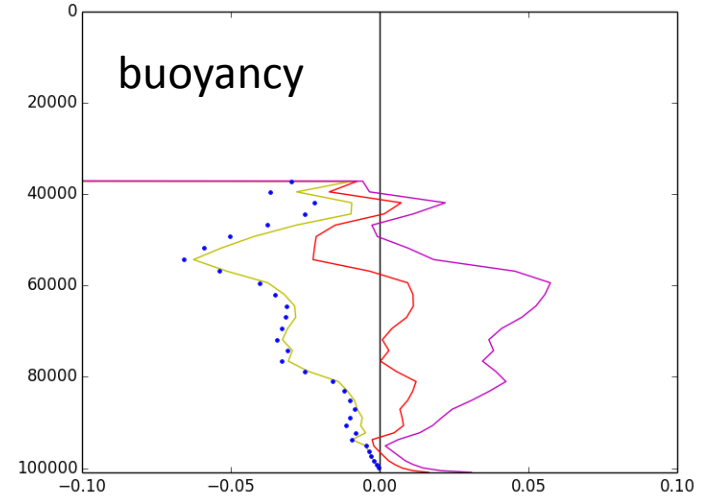
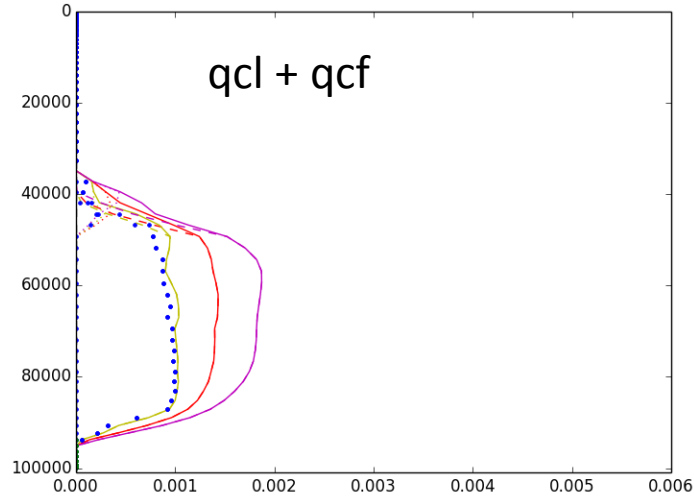
Detrainment is determined by the proportion of the updraft PDF no longer rising relative to the grid-mean flow.

Updraft radius  $r = 250\text{m}$  ("shallow" mode)

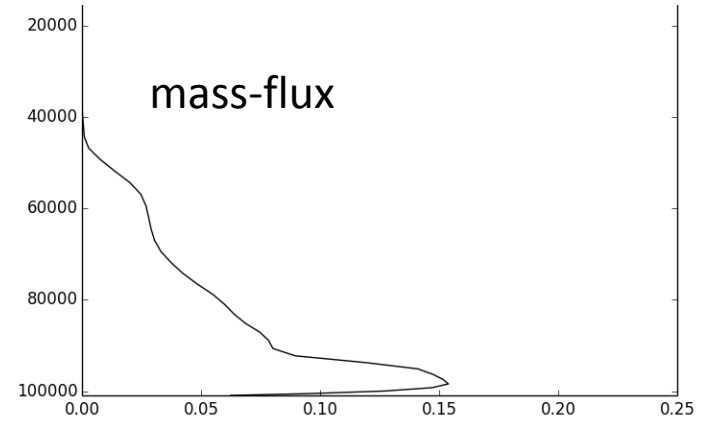
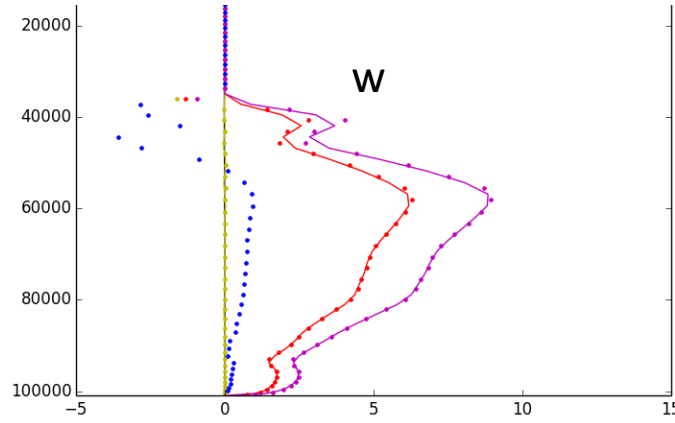
Launched from surface using TOGA-COARE sounding.



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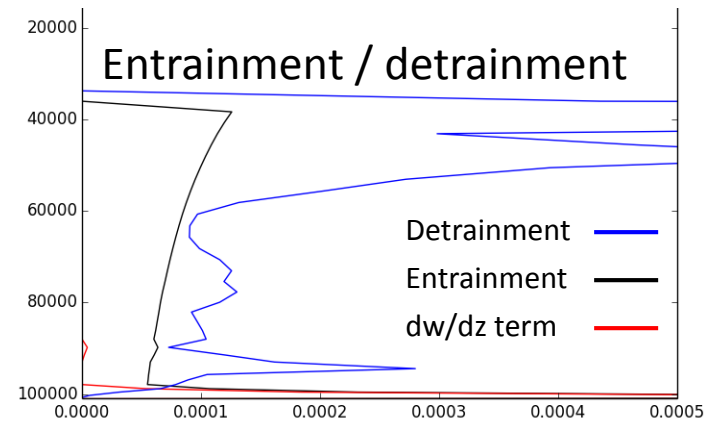
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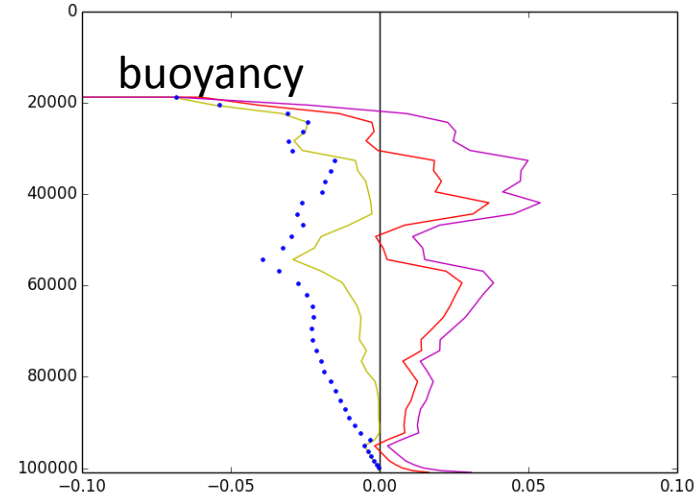
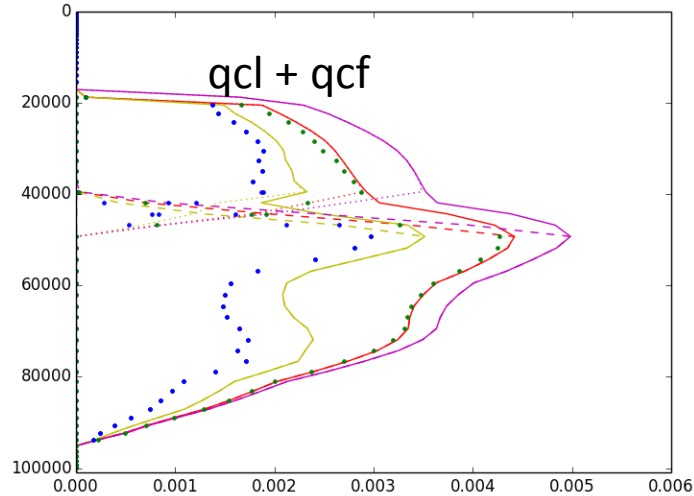
Detrainment is determined by the proportion of the updraft PDF no longer rising relative to the grid-mean flow.

Updraft radius  $r = 500\text{m}$  ("congestus" mode)

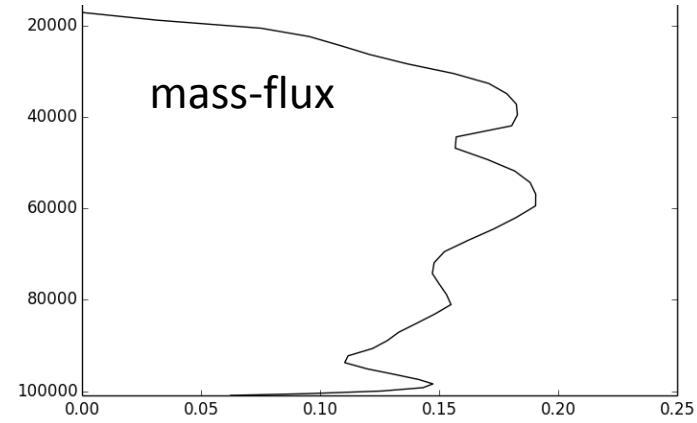
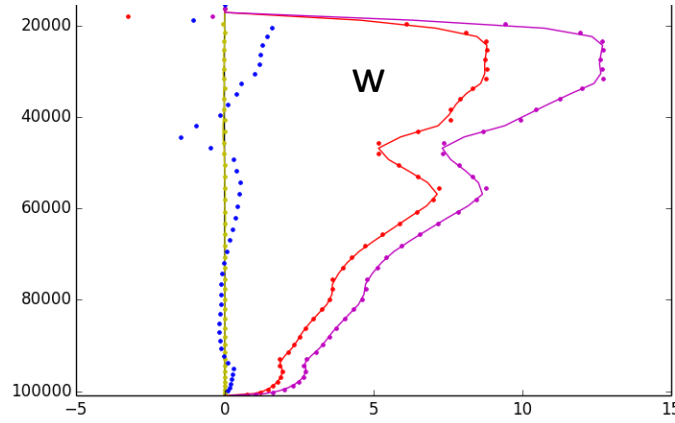
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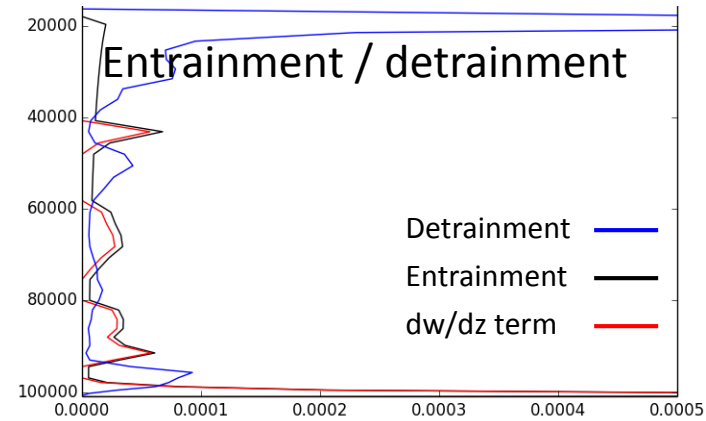
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- Updraft edge



Detrainment is determined by the proportion of the updraft PDF no longer rising relative to the grid-mean flow.

Updraft radius  $r = 2000\text{m}$  ("deep" mode)

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